



Analysis of the gluonium content in η'

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η, η' : mixing and gluonium

The η, η' mesons wave function can be decomposed in the quark mixing base as in the following (J. L. Rosner, Phys. Rev. D 27 (1983) 1101.).

$$|\eta'\rangle = X_{\eta'} |q\bar{q}\rangle + Y_{\eta'} |s\bar{s}\rangle + Z_{\eta'} |G\rangle \quad |\eta\rangle = \cos\psi_P |q\bar{q}\rangle - \sin\psi_P |s\bar{s}\rangle \quad |q\bar{q}\rangle = \frac{|u\bar{u}\rangle + |d\bar{d}\rangle}{\sqrt{2}}$$

$$X_{\eta'} = \sin\psi_P \cos\psi_G$$

$$Y_{\eta'} = \cos\psi_P \cos\psi_G$$

$$Z_{\eta'} = \sin\psi_G$$

The $\phi \rightarrow \eta, \eta' \gamma$ transition is modelled according a spin flip transition



$$\Gamma(P \rightarrow V \gamma) = \frac{g^2}{4\pi} |p_y|^3$$

$$\Gamma(V \rightarrow P \gamma) = \frac{1}{3} \frac{g^2}{4\pi} |p_y|^3$$

Only quarks participate to the electromagnetic transition, gluonium is spectator. It appears in the η' decay amplitudes only through the normalisation to 1 ($Y_{\eta'} \sim \cos\psi_G$)



On the meaning of gluonium

$Z_{\eta'}$ can be interpreted as a mixing with a glue ball. The mass of this glue ball has been determined
[Hai-Yang Cheng, Phys. Rev. D79 (2009) 014024]

$$\theta_i = 54.7^\circ$$

$$\phi \rightarrow \Psi_P$$

$$\phi_G \rightarrow \Psi_G$$

$$\frac{c\theta(s\phi - c\theta s\theta_i\Delta_G)m_{\eta'}^2 - s\theta(c\phi + s\theta s\theta_i\Delta_G)^2m_\eta^2 - s\theta_i c\phi_G m_G^2}{c\theta(c\phi - c\theta c\theta_i\Delta_G)m_{\eta'}^2 + s\theta(s\phi - s\theta c\theta_i\Delta_G)^2m_\eta^2 - c\theta_i c\phi_G m_G^2} = \frac{\sqrt{2}f_s}{f_q},$$

$$m_G = (1.41 \pm 0.1) \text{ GeV}$$

The glue-ball is identified as $\eta(1405)$
copiously produced in $J/\psi \rightarrow \eta(1405)\gamma$

Prediction $\text{Br}(\eta(1405) \rightarrow \gamma\gamma) = 6 \pm 1 \times 10^{-5}$
Decay never observed



V P γ and P $\gamma\gamma$ transitions

KLOE [Phys. Lett. B648 (2007) 267] has fitted:

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos^2 \psi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}^2$$

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[z_q X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \cdot \tan \psi_V \cdot Y_{\eta'} \right]^2$$

together with the measured branching ratio:

$\phi \rightarrow \eta' \gamma$

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3} \quad \sim 4000 \quad \eta' \rightarrow \pi^+ \pi^- \eta, \eta \rightarrow 3\pi^0$$

$$\sim 1.7 \times 10^6 \quad \eta' \rightarrow \pi^0 \pi^0 \eta, \eta \rightarrow \pi^+ \pi^- \pi^0$$

$$\phi \rightarrow \eta \gamma, \eta \rightarrow 3\pi^0$$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \psi_P \cdot \cos^2 \psi_G \left(1 - \frac{m_s}{\bar{m}} \frac{z_q}{z_s} \cdot \frac{\tan \psi_V}{\sin 2 \psi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio: $\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_\pi} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$ E. Kou, Phys. Rev. D 63 (2001) 54027



V P γ and P $\gamma\gamma$ transitions

KLOE [Phys. Lett. B648 (2007) 267] has fitted:

Were taken from a global fit without gluonium:

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos \psi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_\rho m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}$$

A. Bramon, R. Escribano,
M.D. Scadron
Phys. Lett. B503 (2001) 271

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_\omega m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[z_q^2 X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \tan \psi_V Y_{\eta'} \right]^2$$

together with the measured branching ratio:

$$\phi \rightarrow \eta' \gamma$$

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3} \sim 4000$$

$$\eta' \rightarrow \pi^+ \pi^- \eta, \eta \rightarrow 3\pi^0$$

$$\eta' \rightarrow \pi^0 \pi^0 \eta, \eta \rightarrow \pi^+ \pi^- \pi^0$$

$$\sim 1.7 \times 10^6$$

$$\phi \rightarrow \eta \gamma, \eta \rightarrow 3\pi^0$$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \psi_P \cdot \cos^2 \psi_G \left(1 - \frac{m}{\bar{m}} \frac{z_q \tan \psi_V}{z_s \sin 2 \psi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio:

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_\pi} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$$

E. Kou, Phys. Rev. D
63 (2001) 54027



V P γ and P $\gamma\gamma$ transitions

KLOE [Phys. Lett. B648 (2007) 267] has fitted:

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos^2 \psi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}^2$$

T. Feldmann, Int. J. Mod. Phys. A 15 (2000) 159

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[z_q X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \cdot \tan \psi_V \cdot Y_{\eta'} \right]^2$$

together with the measured branching ratio:

$\phi \rightarrow \eta' \gamma$

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3} \sim 4000$$

$\eta' \rightarrow \pi^+ \pi^- \eta, \eta \rightarrow 3\pi^0$

$\eta' \rightarrow \pi^0 \pi^0 \eta, \eta \rightarrow \pi^+ \pi^- \pi^0$

$$\sim 1.7 \times 10^6$$

$\phi \rightarrow \eta \gamma, \eta \rightarrow 3\pi^0$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \psi_P \cdot \cos^2 \psi_G \left(1 - \frac{m_s}{\bar{m}} \frac{z_q}{z_s} \cdot \frac{\tan \psi_V}{\sin 2 \psi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio:

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_\pi} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$$

E. Kou, Phys. Rev. D 63 (2001) 54027



New fit trying to handle all the free parameters

- 1) Leave the z's parameter free;
- 2) Add more constraints (needed to perform the fit with larger number of parameters);
- 3) Check the contribution from $\eta' \rightarrow \gamma\gamma$ / $\pi^0 \rightarrow \gamma\gamma$

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[z_q \cos(\psi_p) - 2 \frac{m_s}{\bar{m}} z_s \tan(\psi_V) \sin(\psi_p) \right]^2 (1 - z_G^2) \left(\frac{m_\omega^2 - m_\eta^2}{m_\omega^2 - m_{\pi^0}^2} \right)^3$$

$$\frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = z_q^2 \frac{\cos^2(\psi_P)}{\cos^2(\psi_V)} \left(\frac{m_\rho^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\rho} \right)^3$$

$$\frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[z_q \tan(\psi_V) \cos(\psi_P) + 2 \frac{\bar{m}}{m_s} z_s \sin(\psi_P) \right]^2 \left(\frac{m_\phi^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\phi} \right)^3$$

$$\frac{\Gamma(\phi \rightarrow \pi^0 \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \tan^2 \psi_V \cdot \left(\frac{m_\phi^2 - m_{\pi^0}^2}{m_\omega^2 - m_{\pi^0}^2} \cdot \frac{m_\omega}{m_\phi} \right)^3, \quad \frac{\Gamma(K^{*+} \rightarrow K^+ \gamma)}{\Gamma(K^{*0} \rightarrow K^0 \gamma)} = \left(\frac{2 \frac{m_s}{\bar{m}} - 1}{1 + \frac{m_s}{\bar{m}}} \right)^2 \cdot \left(\frac{m_{K^{*+}}^2 - m_{K^0}^2}{m_{K^{*0}}^2 - m_{K^0}^2} \cdot \frac{m_{K^0}}{m_{K^{*+}}} \right)^3$$



Fit procedure.

The χ^2 is defined as follows:

$$\chi^2 = \sum_{i,j=1,3} (y_i - y_i^{th}) \times V_{ij}^{-1} (y_j - y_j^{th})$$

$$V_{ij} = [B_{ij} + (A_{ik} \times C_{kl} \times A_{lj}^T)]$$

Experimental
covariance matrix

Theoretical parameters
covariance matrix

$$B_{ij} =$$

Full covariance matrix
(correlation comes from the
constrained fit to η' Br)

$$C_{kl} = \begin{pmatrix} \sigma_{f_q}^2 & 0 \\ 0 & \sigma_{f_s}^2 \end{pmatrix}$$

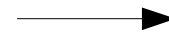
$$A_{ik} = \begin{pmatrix} \frac{\partial y_1^{th}}{\partial f_q} & \frac{\partial y_1^{th}}{\partial f_s} \\ \frac{\partial y_2^{th}}{\partial f_q} & \frac{\partial y_2^{th}}{\partial f_s} \\ \dots & \dots \end{pmatrix}$$

Re-evaluated at
each minimization
step



The experimental covariance matrix **B** contains correlation among common used quantities in the fitted relations:

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}$$



Introduces a correlation in the fitted quantities

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{Br(\eta' \rightarrow \gamma \gamma) \Gamma_{\eta'}}{\Gamma(\pi^0 \rightarrow \gamma \gamma)}, \quad \frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{Br(\eta' \rightarrow \rho \gamma) \Gamma_{\eta'}}{\Gamma(\omega \rightarrow \pi^0 \gamma)}$$

PDG-2006

$x_i = \Gamma_i / \Gamma$

x_2	-34					
x_3	-78	-29				
x_4	-35	-24	32			
x_5	-26	-12	26	8		
x_6	-28	-11	35	11	9	
Γ	32	-2	-24	-5	-88	-8
	x_1	x_2	x_3	x_4	x_5	x_6

Br and Γ strongly correlated (above all $\Gamma(\eta' \rightarrow \gamma \gamma)$)

the Γ is measured using:

$$e^+ e^- \rightarrow \eta' e^+ e^-$$

New preliminary measurement of the η' total width: update in this presentation.

Mode	Rate (MeV)	Scale factor
Γ_1 $\pi^+ \pi^- \eta$	0.090 ± 0.008	1.2
Γ_2 $\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$)	0.060 ± 0.005	1.2
Γ_3 $\pi^0 \pi^0 \eta$	0.042 ± 0.004	1.6
Γ_4 $\omega \gamma$	0.0062 ± 0.0008	1.2
Γ_5 $\gamma \gamma$	0.00430 ± 0.00015	1.1
Γ_6 $3\pi^0$	(3.2 ± 0.6) × 10 ⁻⁴	1.1



USING PDG06 DATA

Parameter	KLOE published	KLOE New fit	K. New fit (no $P\gamma\gamma$)	R.Escribano, J. Nadal
				JHEP 05 (2007) 6
$Z_{\eta'}^2$	0.14 ± 0.04	0.105 ± 0.037	0.03 ± 0.06	0.04 ± 0.09
Ψ_P	$(39.7 \pm 0.7)^\circ$	$(40.7 \pm 0.7)^\circ$	$(41.6 \pm 0.8)^\circ$	$(41.4 \pm 1.3)^\circ$
Z_{NS}	0.91 ± 0.05	0.866 ± 0.025	0.85 ± 0.03	0.86 ± 0.03
Z_S	0.89 ± 0.07	0.79 ± 0.05	0.78 ± 0.05	0.79 ± 0.05
Ψ_V	3.2°	$(3.15 \pm 0.10)^\circ$	$(3.16 \pm 0.10)^\circ$	$(3.2 \pm 0.1)^\circ$
m_s/m	1.24 ± 0.07	1.24 ± 0.07	1.24 ± 0.07	1.24 ± 0.07
$P(\chi^2)$	49%	17%	41%	38%

Glunium only with $\eta' \rightarrow \gamma\gamma$

Glunium content @ $\sim 3\sigma$ level confirmed ($Z_{\eta'} = 0$: $\Psi_P = (41.6 \pm 0.5)^\circ$, $P(\chi^2) = 1\%$)

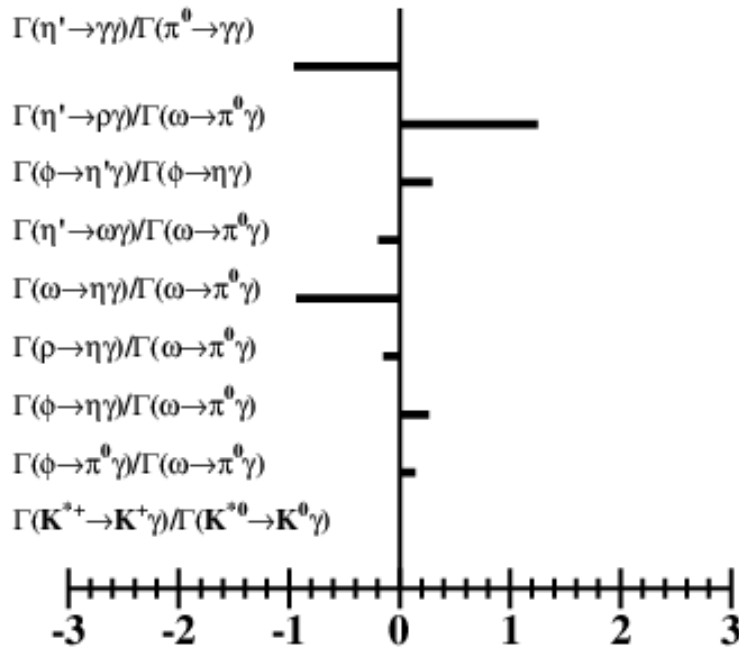
$\eta' \rightarrow \gamma\gamma$ is the only measurement sensitive to the glunium



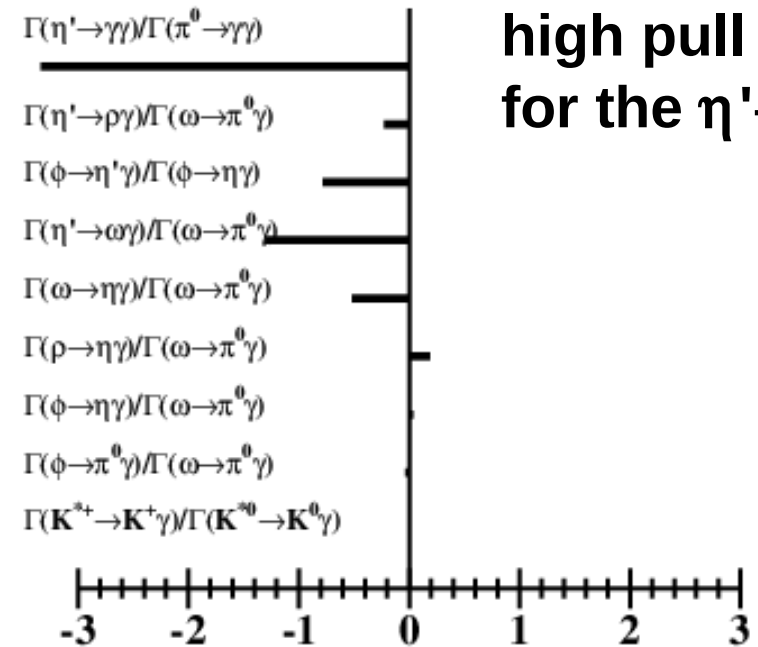
The $\eta' \rightarrow \gamma\gamma$ role.

Fit pulls

gluonium allowed



gluonium at zero





Updates...

Fit redone using:

- 1) new PDG-2008 measurements;
- 2) $\Gamma(\omega \rightarrow \pi^0 \gamma)$ from KLOE;
- 3) Lattice evaluation of f_K and f_π ;
- 4) New preliminary measurement of the η' total width.



Fit redone using PDG-2008.

$$x_i = \Gamma_i / \Gamma$$

x_2	-35					
x_3	-77	-28				
x_4	-35	-24	33			
x_5	-23	-10	23	7		
x_6	-28	-11	35	11	8	
Γ	29	-5	-21	-4	-85	-7
	x_1	x_2	x_3	x_4	x_5	x_6

	Mode	Rate (MeV)	Scale factor
Γ_1	$\pi^+ \pi^- \eta$	0.091 \pm 0.008	1.1
Γ_2	$\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$)	0.060 \pm 0.005	1.2
Γ_3	$\pi^0 \pi^0 \eta$	0.042 \pm 0.004	1.5
Γ_4	$\omega \gamma$	0.0062 \pm 0.0008	1.2
Γ_5	$\gamma \gamma$	0.00430 \pm 0.00015	1.1
Γ_6	$3\pi^0$	(3.2 \pm 0.6) $\times 10^{-4}$	1.1

	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	7.9/3 (5 %)	15/4 (5×10^{-3})
Z_C^2	0.097 \pm 0.037	0 fixed
$\langle \Psi_P \rangle$	(41.0 \pm 0.7) $^\circ$	(41.7 \pm 0.5) $^\circ$
Z_q	0.86 \pm 0.02	0.858 \pm 0.021
Z_s	0.79 \pm 0.05	0.78 \pm 0.05
Ψ_V	(3.17 \pm 0.09) $^\circ$	(3.19 \pm 0.09) $^\circ$
m_s/\bar{m}	1.24 \pm 0.07	1.24 \pm 0.07

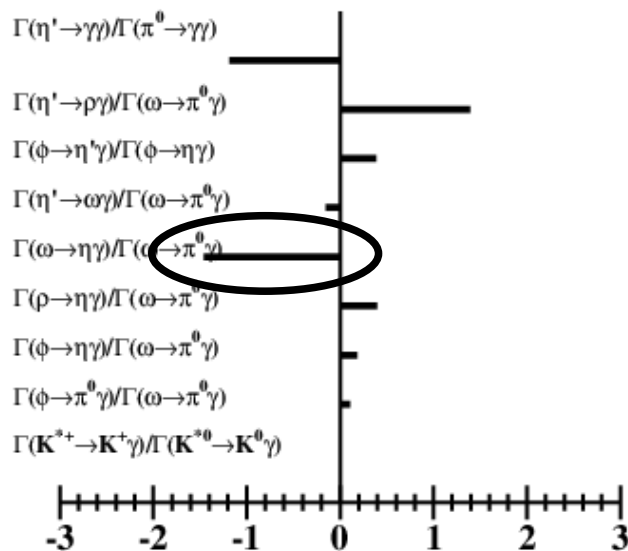
PDG08

The same gluonium content but unsatisfying fit quality.

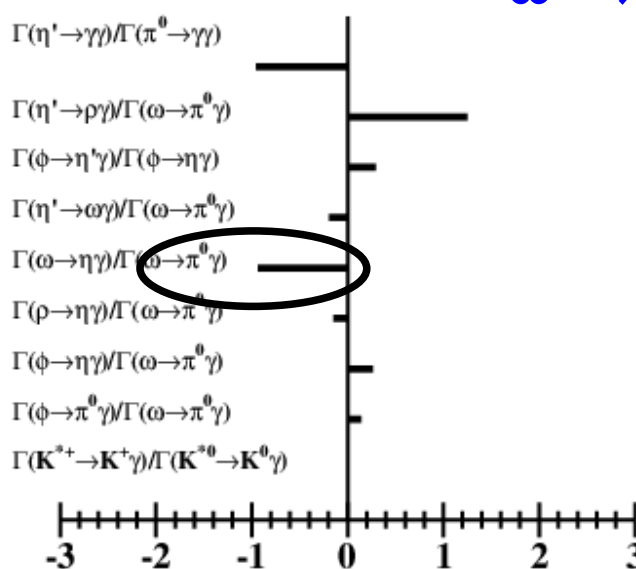
Table 5: Fit results using the PDG-2008 values.



PDG08



PDG06



$\omega \rightarrow \eta\gamma$ pull has increased

The $\omega \rightarrow \eta\gamma$ branching ratio changed from

$$(4.9 \pm 0.5) \times 10^{-4}$$

to

$$(4.6 \pm 0.4) \times 10^{-4}$$

This value is determined by the global PDG fit, and it is mainly determined by:

$$\Gamma(e^+e^-) \times \Gamma(\eta\gamma) / \Gamma_{\text{total}}^2$$

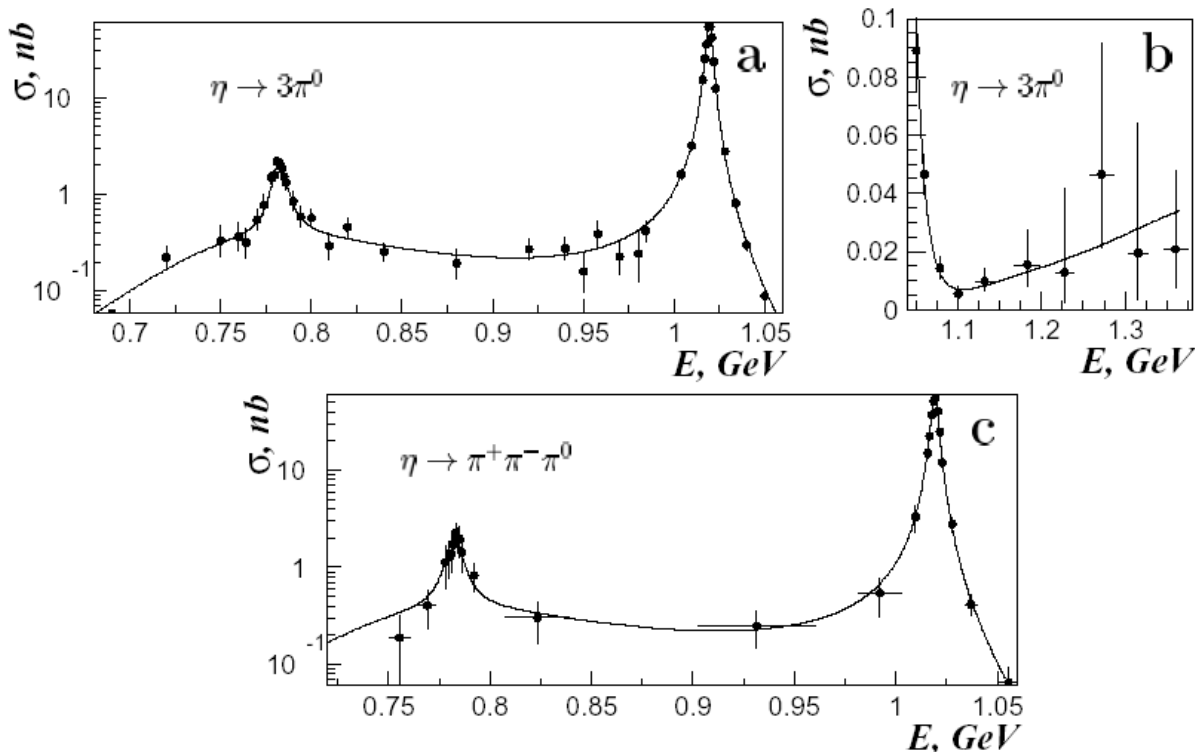
$$\Gamma_9 \Gamma_5 / \Gamma^2$$

VALUE (units 10^{-8})	EVTS	DOCUMENT ID	TECN	COMMENT
3.31 ± 0.28 OUR FIT	Error includes scale factor of 1.1.			
3.18 ± 0.28 OUR AVERAGE	Phys. Rev. D76 (2007) 077101			
$3.10 \pm 0.31 \pm 0.11$	33k	²⁴ ACHASOV 07B	SND	0.6–1.38 $e^+e^- \rightarrow \eta\gamma$
$3.17^{+1.85}_{-1.31} \pm 0.21$	17.4k	²⁵ AKHMETSHIN 05	CMD2	0.60–1.38 $e^+e^- \rightarrow \eta\gamma$
$3.41 \pm 0.52 \pm 0.21$	23k	^{26,27} AKHMETSHIN 01B	CMD2	$e^+e^- \rightarrow \eta\gamma$



$\omega \rightarrow \eta\gamma$ branching ratio measurement from SND

The branching ratio is extracted with a global fit to the $e^+e^- \rightarrow \eta\gamma$ with a VMD model with $\rho, \omega, \phi, \rho'$ included (ρ' parameters varied to compute systematics and constrained from $e^+e^- \rightarrow \eta\rho$).



ω contribution overwhelmed by the $\rho \rightarrow \eta\gamma$ contribution
no correlation matrix is given in the paper



Direct $\omega \rightarrow \eta \gamma$ branching ratio measurement

The fit is dominated by the SND measurement

$$\Gamma(\eta\gamma)/\Gamma_{\text{total}}$$

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN	COMMENT
4.6 ± 0.4 OUR FIT	Error includes scale factor of 1.1.			
6.3 ± 1.3 OUR AVERAGE	Error includes scale factor of 1.2.			
6.6 ± 1.7	53	ABELE	97E CBAR	0.0 $\bar{p}p \rightarrow 5\gamma$
8.3 ± 2.1		ALDE	93 GAM2	38 $\pi^- p \rightarrow \omega n$
3.0 $^{+2.5}_{-1.8}$	54	ANDREWS	77 CNTR	6.7–10 γCu

In Crystal Barrel the channel $\bar{p}p \rightarrow \eta \omega$ is used that is 6 times larger than $\bar{p}p \rightarrow \eta \rho$, the $\omega \rightarrow \eta \gamma$ Br was normalized to the $\omega \rightarrow \pi^0 \gamma$ Br

using $\omega \rightarrow \eta \gamma$ from PDG average

	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	3.9/3 (27.5 %)	13/4 (1.1 %)
Z_G^2	0.111 ± 0.036	0 fixed
Ψ_P	(40.6 ± 0.7)°	(41.5 ± 0.5)°
Z_q	0.890 ± 0.025	0.882 ± 0.023
$Z_{\tilde{s}}$	0.79 ± 0.05	0.78 ± 0.05
Ψ_V	(3.15 ± 0.10)°	(3.18 ± 0.09)°
m_s/\bar{m}	1.24 ± 0.07	1.24 ± 0.07



Direct $\omega \rightarrow \eta \gamma$ branching ratio measurement

The fit is dominated by the SND measurement

$$\Gamma(\eta\gamma)/\Gamma_{\text{total}}$$

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN	COMMENT
4.6 ± 0.4 OUR FIT	Error includes scale factor of 1.1.			
6.3 ± 1.3 OUR AVERAGE	Error includes scale factor of 1.2.			
6.6 ± 1.7	⁵³	ABELE	97E CBAR	0.0 $\bar{p}p \rightarrow 5\gamma$
8.3 ± 2.1		ALDE	93 GAM2	38 $\pi^- p \rightarrow \omega n$
3.0 ^{+2.5} _{-1.8}	⁵⁴	ANDREWS	77 CNTR	6.7–10 γCu

In Crystal Barrel the channel $n\bar{n} \rightarrow \omega \gamma$ is used that is 6 times larger than $p\bar{p} \rightarrow \omega \gamma$

Important discrepancy in the experimental determination.
A new measurement is welcome!!!

using $\omega \rightarrow \eta \gamma$ from PDG average

Z_q	0.890 ± 0.025	0.882 ± 0.023
Z_s	0.79 ± 0.05	0.78 ± 0.05
ψ_V	$(3.15 \pm 0.10)^\circ$	$(3.18 \pm 0.09)^\circ$
m_s/\bar{m}	1.24 ± 0.07	1.24 ± 0.07



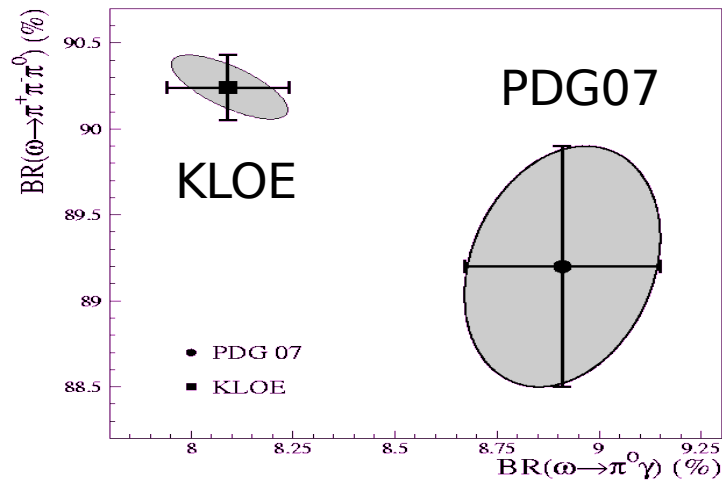
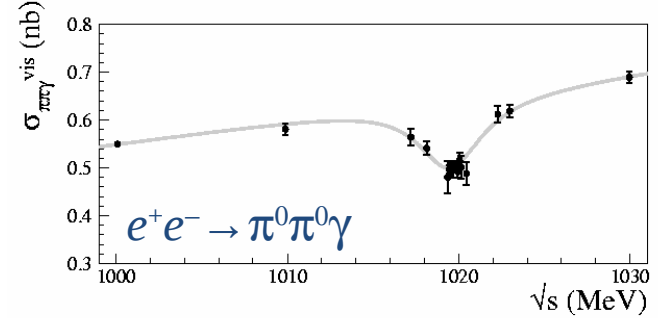
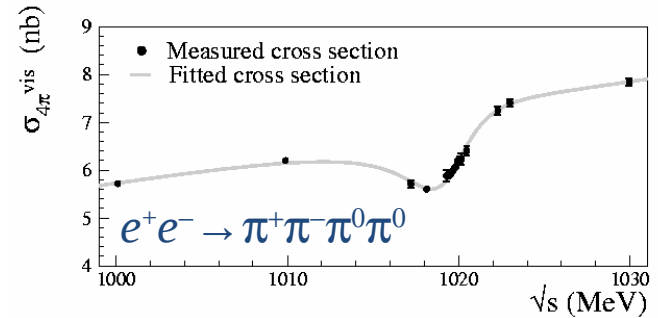
Interference pattern between non-resonant $e^+e^- \rightarrow \omega \pi^0$ and ϕ decays:

$$\sigma(\sqrt{s}) = \sigma_0(\sqrt{s}) \cdot \left| 1 - Z \frac{M_\phi \Gamma_\phi}{D_\phi} \right|^2$$

model independent $\Rightarrow \sigma_0(\sqrt{s}) = \sigma_0 + \sigma'(\sqrt{s} - M_\phi)$

$\Gamma(\omega \rightarrow \pi^0 \gamma) / \Gamma(\omega \rightarrow \pi^+ \pi^- \pi^0)$ & assuming $\sum_i \text{Br}_i = 1$ $\text{Br}(\omega \rightarrow \pi^+ \pi^-)$ from PDG average

$\text{BR}(\omega \rightarrow \pi^+ \pi^- \pi^0) = (90.24 \pm 0.19) \%$
 $\text{BR}(\omega \rightarrow \pi^0 \gamma) = (8.09 \pm 0.14) \%$



3 σ discrepancy



Estimate of f_q and f_s – old KLOE

Estimates used in our previous paper

$$\frac{\Gamma(\eta' \rightarrow \gamma\gamma)}{\Gamma(\pi^0 \rightarrow \gamma\gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_\pi} \right)^3 \left(\frac{f_\pi}{f_q} 5 \sin(\psi_P) \cos(\psi_G) + \sqrt{2} \frac{f_\pi}{f_s} \cos(\psi_P) \cos(\psi_G) \right)^2$$

T. Feldmann, Int. J. Mod. Phys. A 15 (2000) 159

source	f_q/f_π	f_s/f_π	ϕ_q	ϕ_s
Mass matrix and radiative decays ^{16,17}	[1.0]	[1.4]	44°	
$U(1)_A$ anomaly & meson masses ¹⁸	1.0	1.4	[42°]	
Phenomenology ^{2,19,20,21}	[1.1 – 1.2]	[1.1 – 1.3]	[28°-34°]	[35°-41°]
NJL quark model & phenom. ²²	[1.07]	[1.36]	[44.1°]	[40.6°]
Current mixing model & phenom. ⁴³	[0.98]	[0.66]	[35.9°]	[26.2°]
Phenomenology ²³	[1.00]	[1.45]		39.2°
GMO mass formula ⁴²	[1.13]	[1.16]	[31.2°]	[35.4°]
χ PT & $1/N_C$ expansion & phenom. ²⁴	[1.08]	[1.43]	[44.8°]	[40.5°]
FKS scheme & theory ²⁶	1.00	1.41	42.4°	
FKS scheme & phenom. ²⁶	1.07	1.34		39.3°
Vector meson dominance & phenom. ⁴⁴	[1.09]	[1.55]	[47.5°]	[42.1°]
Energy dependent scheme & phenom. ⁴⁵	[1.10]	[1.46]	[38.9°]	[41.0°]

Value used up to now, 1% error assumed.

Reasonable if compared to $U(1)_A$ anomaly and meson masses.



In the Isospin symmetry limit:

$$f_q = f_\pi; \quad f_s = \sqrt{f_K^2 - f_\pi^2}$$

$$f_q/f_\pi = 1 \quad \text{with no error} \quad \frac{f_s}{f_\pi} = \sqrt{2 \frac{f_K^2}{f_\pi^2} - 1}$$

$$f_K/f_\pi = 1.189(7)$$

Lattice-UKQCD:

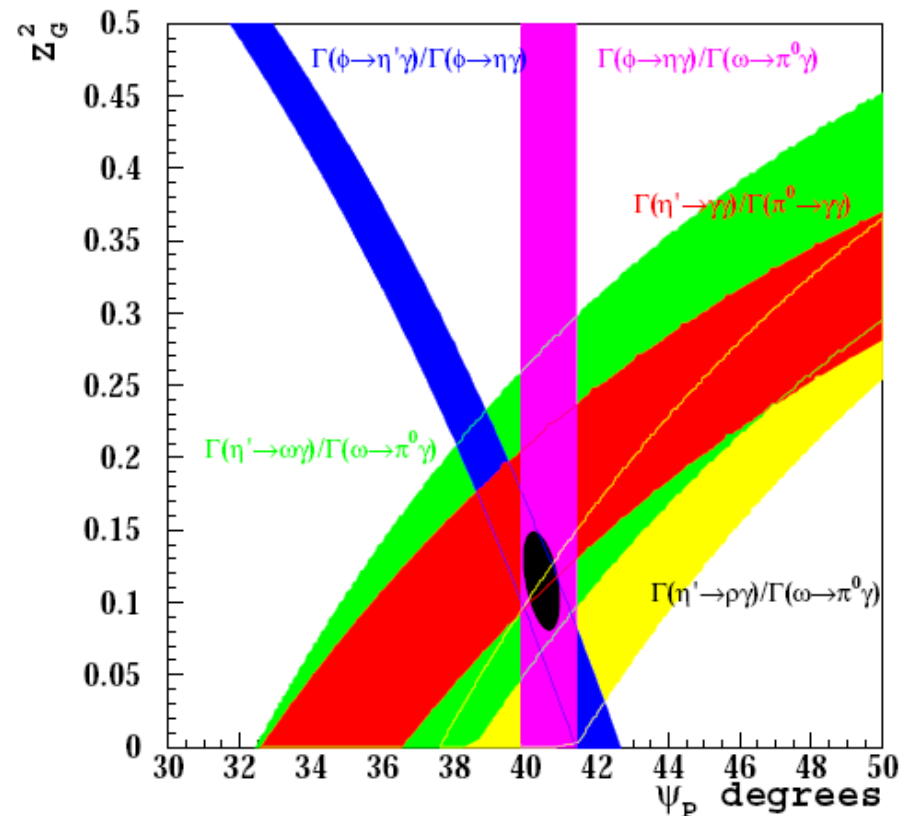
Follana et al., Phys. Rev. Lett.
100 (2008) 062002

$$\frac{f_s}{f_\pi} = 1.352 \pm 0.007$$

**0.5% error
but 4% difference
with our previous
value.**



	Z_G free	$Z_G = 0$ fixed
χ^2/ndf (CL)	4.6/3 (20%)	14.7/4 (0.5%)
Z_G^2	0.115 ± 0.036	0
ψ_P	$(40.4 \pm 0.6)^\circ$	$(41.4 \pm 0.5)^\circ$
Z_q	0.936 ± 0.025	0.927 ± 0.023
Z_s	0.83 ± 0.05	0.82 ± 0.05
ψ_V	$(3.32 \pm 0.09)^\circ$	$(3.34 \pm 0.09)^\circ$
m_s/\bar{m}	1.24 ± 0.07	1.24 ± 0.07



ψ_P	-0.507				
Z_q	0.063	-0.018			
Z_s	0.092	-0.189	0.013		
ψ_V	-0.059	-0.012	0.045	0.028	
m_s/\bar{m}	-0.002	0.003	0.001	0.949	0.000
	Z_G^2	ψ_P	Z_q	Z_s	ψ_V

Update with the preliminary η' width measurement from COSY-11

The width is dominated by $\eta'(958)$ WIDTH



$G(\eta' \rightarrow \gamma\gamma)$ and $\text{Br}(\eta' \rightarrow \gamma\gamma)$

PDG 08

<u>VALUE (MeV)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>	<u>COMMENT</u>
0.205 ± 0.015 OUR FIT	Error includes scale factor of 1.2.				
0.30 ± 0.09 OUR AVERAGE					
0.40 ± 0.22	4800	WURZINGER 96	SPEC		1.68 $p d \rightarrow {}^3\text{He} \eta'$
0.28 ± 0.10	1000	BINNIE 79	MMS	0	$\pi^- p \rightarrow n \text{MM}$
• • • We do not use the following data for averages, fits, limits, etc. • • •					
0.20 ± 0.04		BAI 04J	BES2		$J/\psi \rightarrow \gamma\gamma \pi^+ \pi^-$

New measurement from COSY-11 E. Czerwiński PDG thesis arXiv:0909.2781

$$\Gamma_{\eta'} = (0.226 \pm 0.017 \pm 0.014) \text{ MeV}$$

Error just two times larger than PDG fit.

Let's try to include this measurement in the fit.

Global fit to branching ratio and decay widths

Lagrange multiplier method: free minimization of χ^2 and constraint equation times a Lagrange multiplier parameter.

$$F = \sum_{l=1}^r \sum_{k=1}^{n_l} \frac{(R_{lk} - R_l(x_j, \Gamma))^2}{\delta_{lk}^2} + \lambda \left(\sum x_j - 1 \right)$$

number of measurements \nearrow
 number of experimental determinations \nearrow
 constraint equation \nearrow
 δ_{lk}^2 \searrow errors, square sum of statistic and systematic error

$R_l(x_j, \Gamma)$ Measurements as a function of the fitting parameters

x_j 6 main η' branching ratios Γ η' total width

Fit done with: 7 parameters, 20 measurements, 51 experimental determinations

Fit results.

PDG 08

$\eta'(958)$ DECAY MODES

Mode	Fraction (Γ_i/Γ)	Scale factor Confidence level
Γ_1 $\pi^+\pi^-\eta$	$(44.6 \pm 1.4) \%$	S=1.
Γ_2 $\rho^0\gamma$ (including non-resonant $\pi^+\pi^-\gamma$)	$(29.4 \pm 0.9) \%$	S=1.
Γ_3 $\pi^0\pi^0\eta$	$(20.7 \pm 1.2) \%$	S=1.
Γ_4 $\omega\gamma$	$(3.02 \pm 0.31) \%$	
Γ_5 $\gamma\gamma$	$(2.10 \pm 0.12) \%$	S=1.
Γ_6 $3\pi^0$	$(1.54 \pm 0.26) \times 10^{-3}$	

$$\Gamma = 0.205 \pm 0.015 \text{ keV} \quad (S= 1.2)$$

x_2	-35					
x_3	-77	-28				
x_4	-35	-24	33			
x_5	-23	-10	23	7		
x_6	-28	-11	35	11	8	
Γ	29	-5	-21	-4	-85	-7
	x_1	x_2	x_3	x_4	x_5	x_6

$$\chi^2 = 36.9/44 \text{ (77 \%)}$$

This Fit (no scale factors)

$\eta'(958)$ DECAY MODES

Mode	Fraction (Γ_i/Γ)
Γ_1 $\pi^+\pi^-\eta$	$(44.8 \pm 1.2) \%$
Γ_2 $\rho^0\gamma$ (including non-resonant $\pi^+\pi^-\gamma$)	$(29.4 \pm 0.8) \%$
Γ_3 $\pi^0\pi^0\eta$	$(20.5 \pm 1.0) \%$
Γ_4 $\omega\gamma$	$(3.01 \pm 0.29) \%$
Γ_5 $\gamma\gamma$	$(2.06 \pm 0.09) \%$
Γ_6 $3\pi^0$	$(1.53 \pm 0.25) \times 10^{-3}$

$$\Gamma = 0.210 \pm 0.011 \text{ keV}$$

x_2	-40					
x_3	-74	-28				
x_4	-33	-21	27			
x_5	-42	-21	55	15		
x_6	-23	-9	29	7	16	
Γ	45	-3	-42	-9	-78	-12
	x_1	x_2	x_3	x_4	x_5	x_6

$$\chi^2 = 37.6/45 \text{ (77 \%)}$$

Glueonium fit results.

	PDG 08	new $\Gamma_{\eta'}$
χ^2/ndf (CL)	4.6/3 (20%)	5.7/3 (13%)
Z_G^2	0.115 ± 0.036	0.101 ± 0.031
ψ_P	$(40.4 \pm 0.6)^\circ$	$(40.7 \pm 0.6)^\circ$
Z_q	0.936 ± 0.025	0.943 ± 0.023
Z_s	0.83 ± 0.05	0.83 ± 0.05
ψ_V	$(3.32 \pm 0.09)^\circ$	$(3.32 \pm 0.09)^\circ$
m_s/\bar{m}	1.24 ± 0.07	1.24 ± 0.07



PERSPECTIVES



η, η' : mixing and gluonium at KLOE-2

1 fb⁻¹

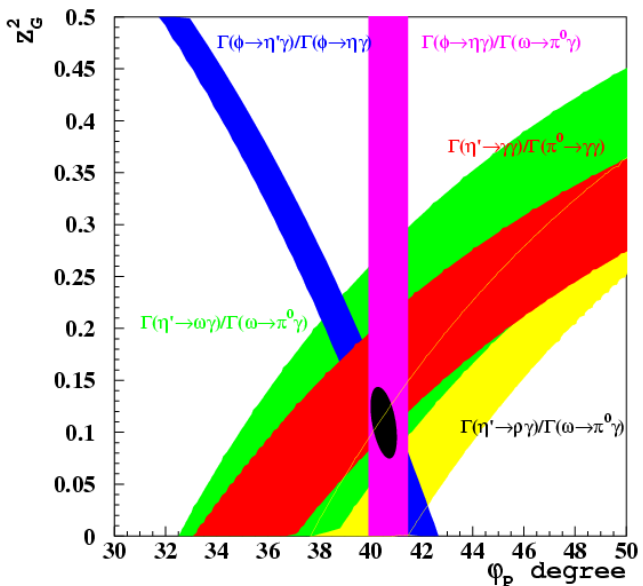
KLOE-2
 expected integrated
 luminosity 8 fb⁻¹

$\eta'(958)$ DECAY MODES	Fraction (Γ_i/Γ)	events	main bkg
$\pi^+ \pi^- \eta$	(44.6 ± 1.4) %	730k	—
$\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$)	(29.4 ± 0.9) %	480k	$\phi \rightarrow \pi^+ \pi^- \pi^0$
$\pi^0 \pi^0 \eta$	(20.7 ± 1.2) %	340k	$\eta\gamma$ or KsKI
$\omega \gamma$	(3.02 ± 0.31) %	50k	$e^+e^- \rightarrow \omega \pi^0$
$\gamma\gamma$	(2.10 ± 0.12) %	34k	$e^+e^- \rightarrow \gamma(\gamma)$

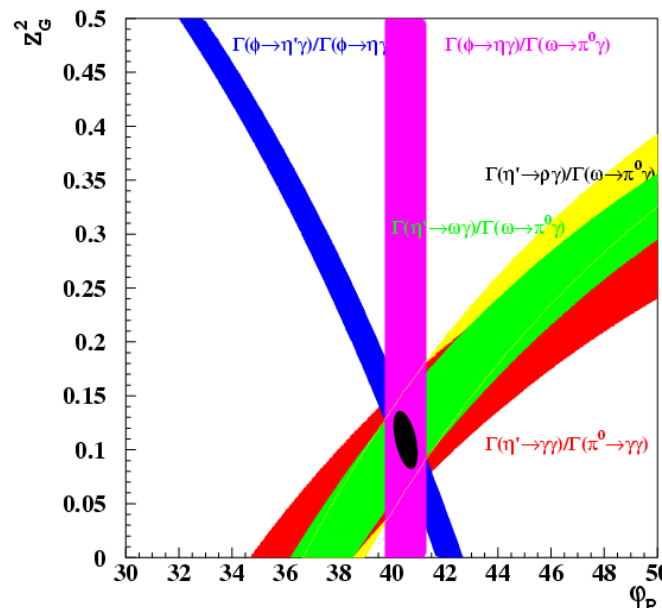
If all Br can be measured at ~1%

Sensitivity to the
 gluonium also
 without the $\eta' \rightarrow \gamma\gamma$

NOW



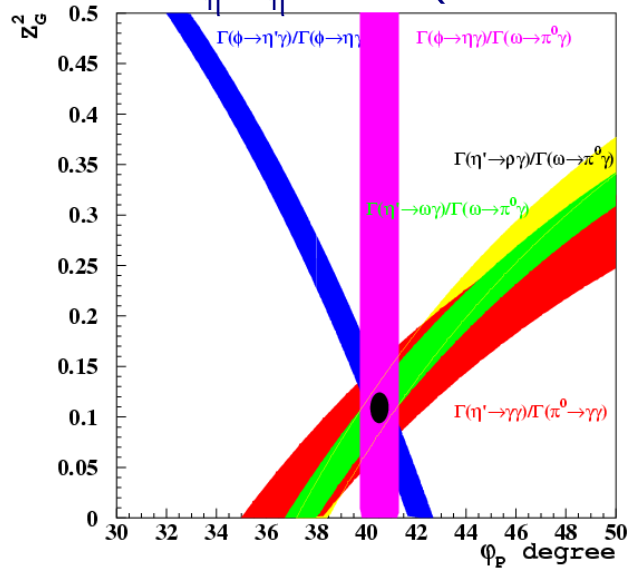
KLOE-2



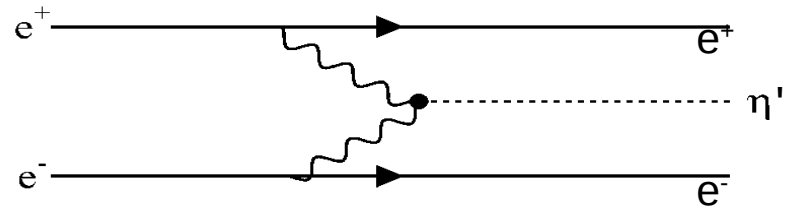


Measurement of the η' width

$\delta\Gamma_{\eta'}/\Gamma_{\eta'} \sim 1\%$ (5.5% now)



$$\Gamma_{\eta'} = \frac{\Gamma_{\eta' \rightarrow \gamma\gamma}}{Br(\eta' \rightarrow \gamma\gamma)}$$



$$\sigma_{e^+e^- \rightarrow e^+e^-\eta'}(s) = \frac{8\alpha^2\Gamma_{\eta' \rightarrow \gamma\gamma}}{m_{\eta'}^3} \times \left[f\left(\frac{m_{\eta'}^2}{s}\right) \left(\ln\frac{m_V^2 s}{m_e^2 m_{\eta'}^2} - 1\right)^2 - \frac{1}{3} \left(\ln\frac{s}{m_{\eta'}^2}\right)^3 \right]$$

background

$\sqrt{s} GeV$	$e^+e^- \rightarrow \eta' e^+e^-$		$e^+e^- \rightarrow \phi(\gamma) \rightarrow \eta' \gamma(\gamma)$		S/\sqrt{B}
	σ (pb)	events at 1 fb ⁻¹	σ (pb)	events at 1 fb ⁻¹	
0.987 ($2m_{K^+}$)	2.3	2300	0.23	230	152
0.995 ($2m_{K^0}$)	2.9	2900	0.67	670	112
1.020 (m_ϕ)	5.1	5100	190	190000	12
1.2	20	20000	1.2	1200	578
1.4	39	39000	5.8	5800	512

→ Very long run at low energy would be required.

→ 34 @ 8fb⁻¹

Feasible with 1 fb⁻¹ at the ϕ peak with $\gamma\gamma$ tagger.

→ Possible at higher energies if the luminosity is at least 1/8 of the ϕ peak luminosity.

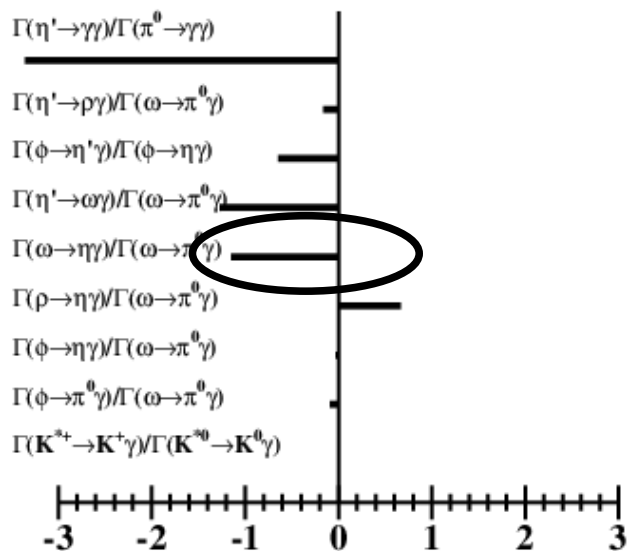
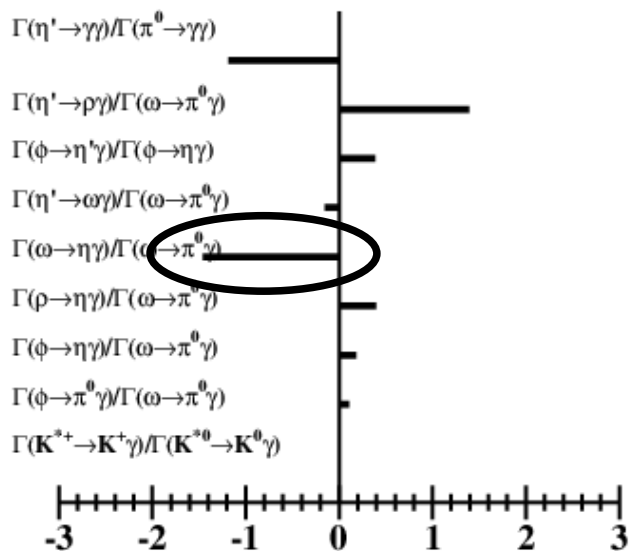


Conclusion

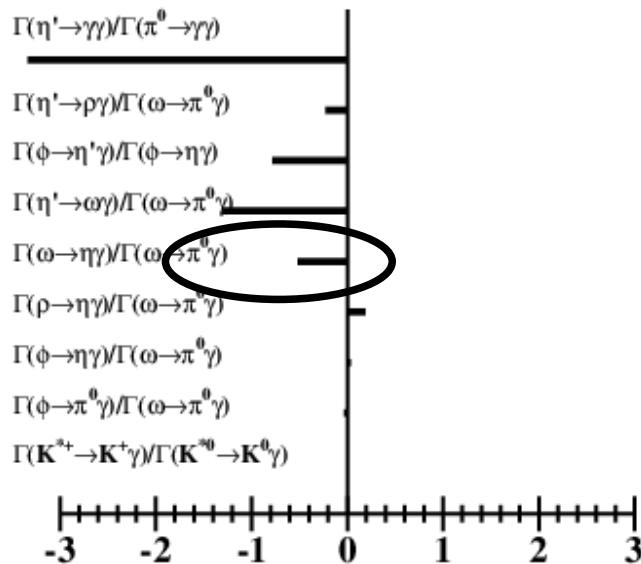
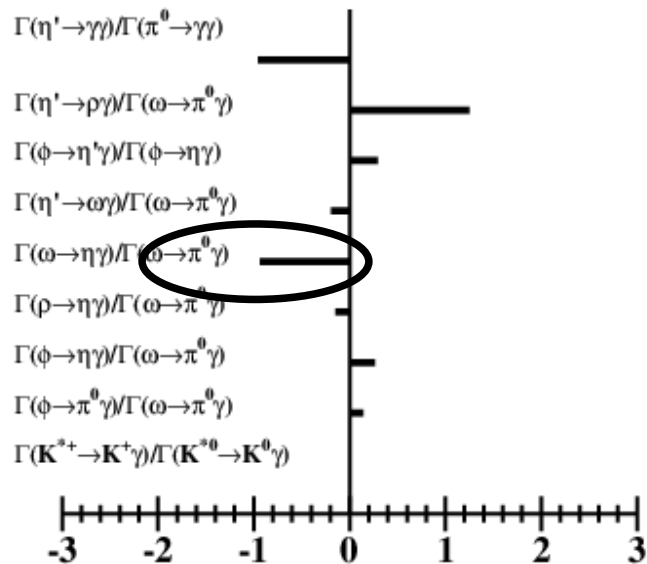
- Gluonium at 3σ also with recent measurements;
- Measurement of $\omega \rightarrow \eta\gamma$ Br is welcome to clarify experimental situation (but small effect on gluonium);
- Still only one measurement is sensitive to the gluonium ($\eta' \rightarrow \gamma\gamma$);
- KLOE-2 with the copious number of η' will allow to give further independent determination of the gluonium content;
- The mixed glue-ball candidate is the $\eta(1405)$



Pulls of the fit



PDG08



PDG06

$\omega \rightarrow \eta\gamma$ pull has increased in both gluonium hypothesis

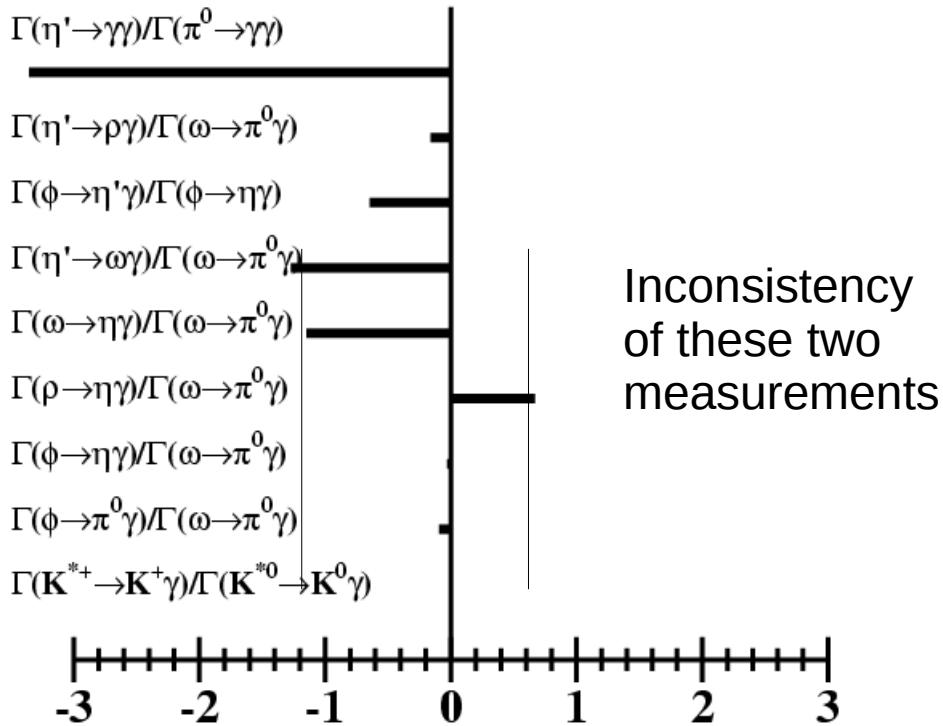


Check if the $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$ introduces any distortion

$$\frac{\Gamma(\omega \rightarrow \eta\gamma)}{\Gamma(\omega \rightarrow \pi^0\gamma)} = \frac{1}{9} \left[Z_q \cos(\psi_P) - 2 \frac{\bar{m}}{m_s} Z_s \tan(\psi_V) \sin(\psi_P) \right]^2 \left(\frac{m_\omega^2 - m_\eta^2}{m_\omega^2 - m_{\pi^0}^2} \right)^3$$

$$\frac{\Gamma(\rho \rightarrow \eta\gamma)}{\Gamma(\omega \rightarrow \pi^0\gamma)} = Z_q^2 \frac{\cos^2(\psi_P)}{\cos^2(\psi_V)} \left(\frac{m_\rho^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\rho} \right)^3$$

with $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$



without $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$

