

2009
PHIPSI

International Workshop
on e⁺e⁻ Collisions from PHI to PSI

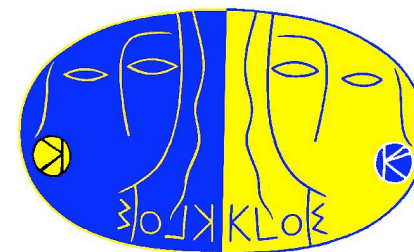


October 13–16 2009 Beijing

$\gamma\gamma$ interactions with KLOE



Federico Nguyen
INFN Roma TRE
for the KLOE Collaboration
Beijing - October, 14th 2009

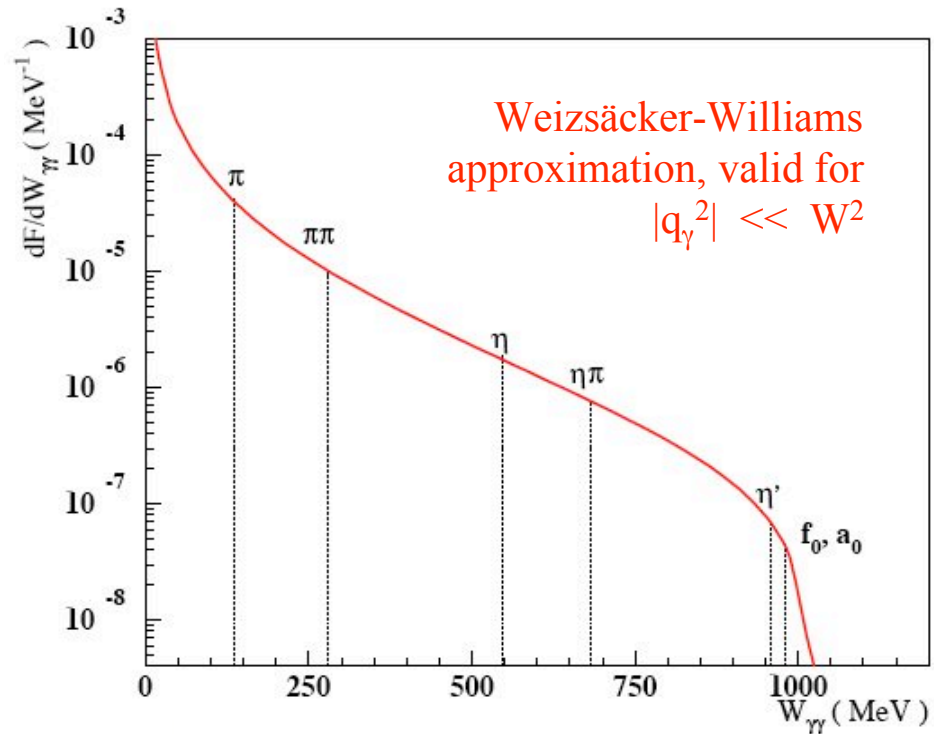
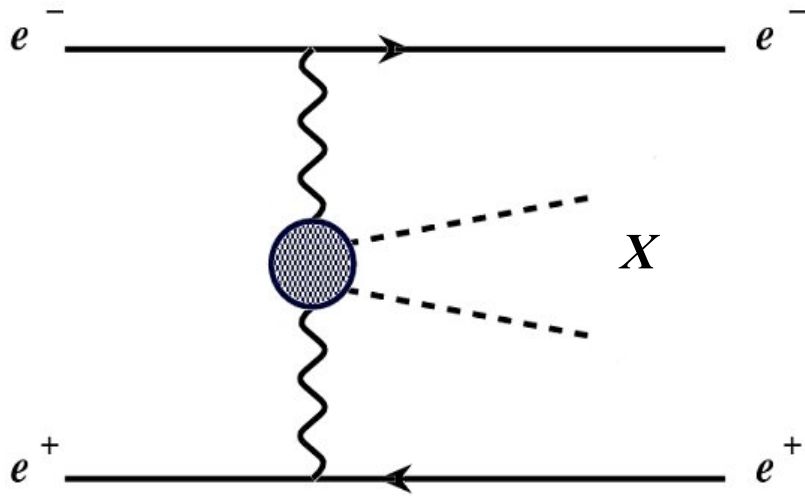


Outline

- motivations for studying $\gamma\gamma$ events:
assessment of scalar and pseudoscalar mesons
through electromagnetic properties
- observation of $\gamma\gamma \rightarrow \eta \rightarrow \pi^+\pi^-\pi^0$ events at DAΦNE
- study of $\gamma\gamma \rightarrow \pi^0\pi^0$ events, search for $\gamma\gamma \rightarrow \sigma$
- conclusions



$e^+e^- \rightarrow e^+e^- X$ or $\gamma\gamma$ interactions



$$N_{e^+e^- \rightarrow e^+e^- X} = L_{ee} \int \frac{dF_{\gamma\gamma}}{dW_{\gamma\gamma}} \sigma_{\gamma\gamma \rightarrow X}(W_{\gamma\gamma}) dW_{\gamma\gamma}$$

$$\sigma_{e^+e^- \rightarrow e^+e^- X} = \frac{16\alpha^2 \Gamma_{X\gamma\gamma}}{m_X^3} \left(\ln \frac{E_b}{m_e} \right)^2 \left((y^2 + 2)^2 \ln \frac{1}{y} - (1 - y^2)(3 + y^2) \right)$$

$$y = m_X / (2E_b)$$

\sqrt{s} (GeV) 1

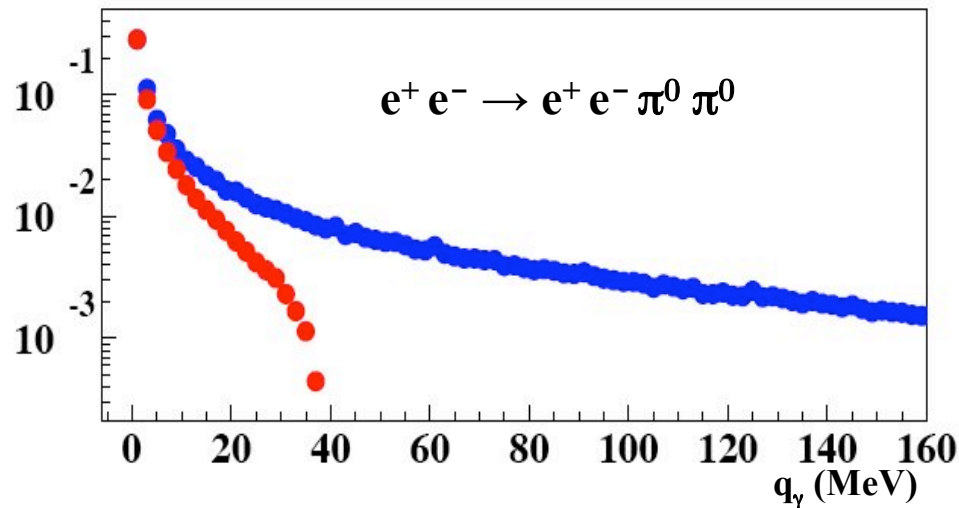
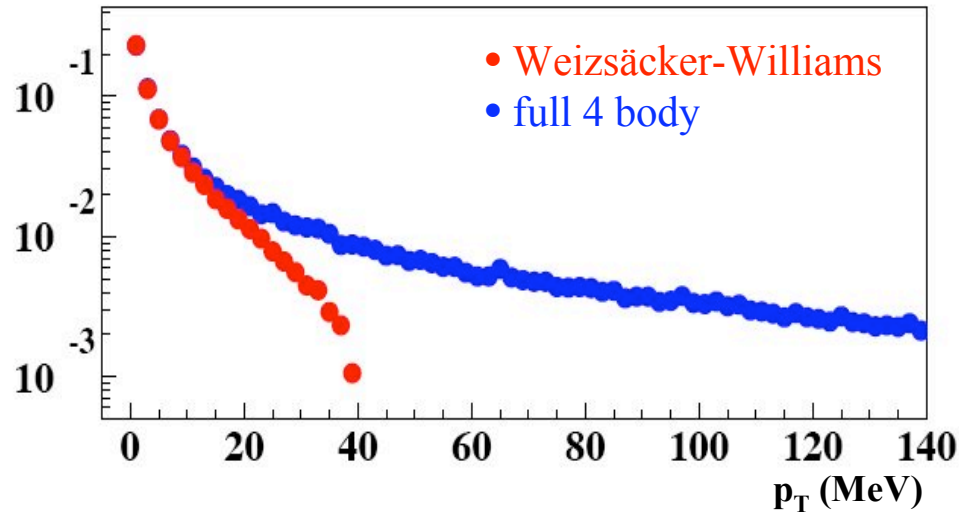
$\sigma(e^+e^- \rightarrow e^+e^- \pi^0)$ (pb) 266

$\sigma(e^+e^- \rightarrow e^+e^- \eta)$ (pb) 43

$\sigma(e^+e^- \rightarrow e^+e^- \eta')$ (pb) 3.3



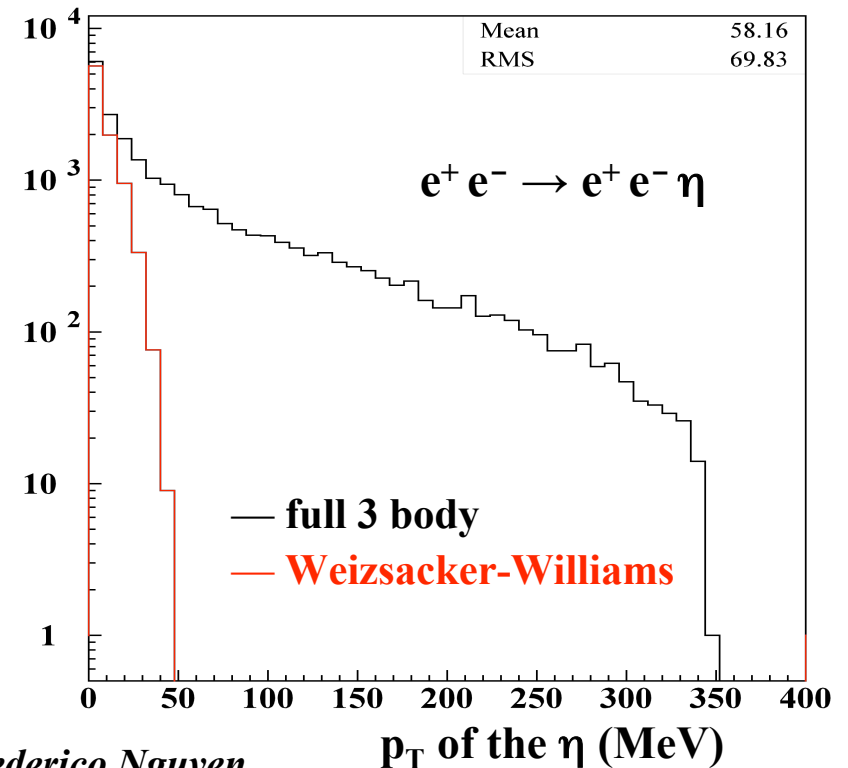
Comparison btw W.W. and phase space



F.N., F. Piccinini & A. Polosa
Eur.Phys.J.C47(2006)65

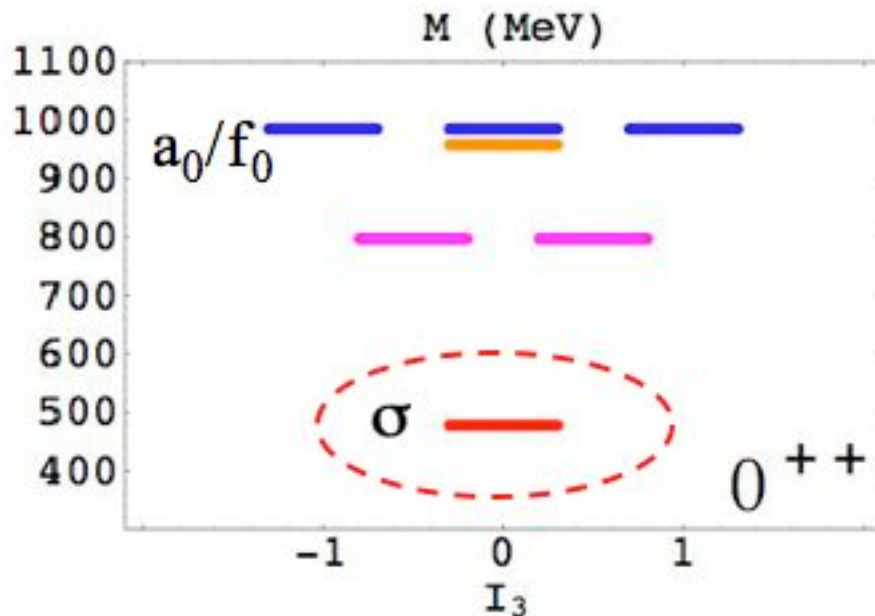
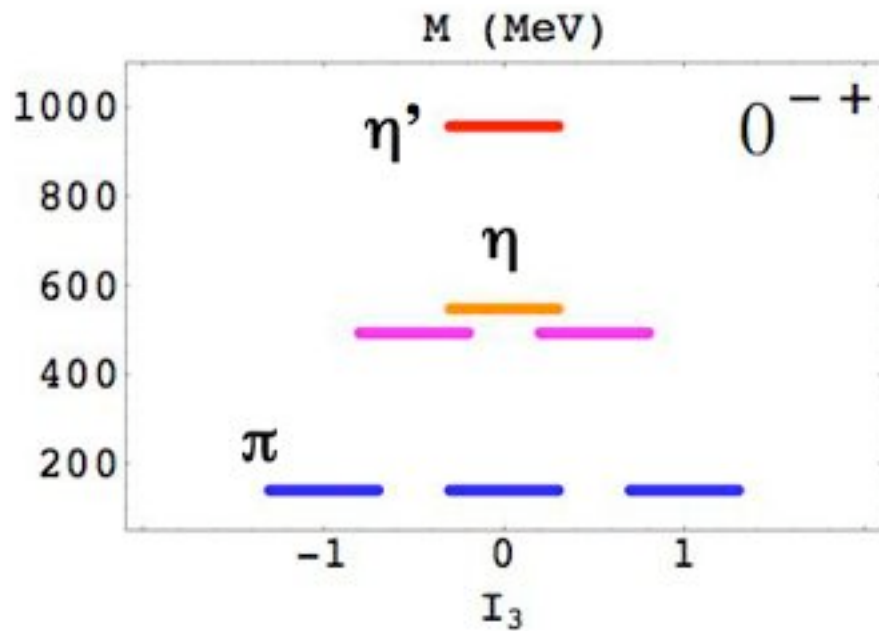


- 1) W.W. is reproduced with a cut $\theta < 5^\circ$ for final state e^+e^-
- 2) impact at the % level within cuts ($p_T < 80$ MeV)



Federico Nguyen
14-10-2009

Pseudoscalar and scalar mesons



- Is $\sigma(600)$ the lightest scalar meson?
- What structure?



VS.



Federico Nguyen
14-10-2009

The $f_0(600)$ or σ case

data come from Dalitz plot analyses,
using Breit-Wigner or T-matrix fits

$f_0(600)$ BREIT-WIGNER MASS OR K-MATRIX POLE PARAMETERS

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
(400-1200) OUR ESTIMATE			
513 ± 32	²⁶ MURAMATSU 02	CLEO	$e^+e^- \approx 10 \text{ GeV}$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$478^{+24}_{-23} \pm 17$	AITALA	01B E791	$D^+ \rightarrow \pi^- \pi^+ \pi^+$
563^{+58}_{-29}	²⁷ ISHIDA	01	$\Upsilon(3S) \rightarrow \Upsilon \pi \pi$
555	²⁸ ASNER	00	CLE2 $\tau^- \rightarrow \pi^- \pi^0 \pi^0 \nu_\tau$
540 ± 36	ISHIDA	00B	$p\bar{p} \rightarrow \pi^0 \pi^0 \pi^0$

CLEO 02: $D^0 \rightarrow K_S \pi^+ \pi^-$ Dalitz analysis

$f_0(600)$ BREIT-WIGNER WIDTH

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
(600-1000) OUR ESTIMATE			
335 ± 67	³⁷ MURAMATSU 02	CLEO	$e^+e^- \approx 10 \text{ GeV}$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$324^{+42}_{-40} \pm 21$	AITALA	01B E791	$D^+ \rightarrow \pi^- \pi^+ \pi^+$
372^{+229}_{-95}	³⁸ ISHIDA	01	$\Upsilon(3S) \rightarrow \Upsilon \pi \pi$
540	³⁹ ASNER	00	CLE2 $\tau^- \rightarrow \pi^- \pi^0 \pi^0 \nu_\tau$
372 ± 80	ISHIDA	00B	$p\bar{p} \rightarrow \pi^0 \pi^0 \pi^0$

$f_0(600)$ T-MATRIX POLE \sqrt{s}

Note that $\Gamma \approx 2 \text{Im}(\sqrt{s_{\text{pole}}})$.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
(400-1200)-i(250-500) OUR ESTIMATE			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$(455 \pm 6^{+31}_{-13}) - i(278 \pm 6^{+34}_{-43})$	1 CAPRINI	08	RVUE Compilation
$(463 \pm 6^{+31}_{-17}) - i(259 \pm 6^{+33}_{-34})$	2 CAPRINI	08	RVUE Compilation
$(552^{+84}_{-106}) - i(232^{+81}_{-72})$	3 ABLIKIM	07A	BES2 $\psi(2S) \rightarrow \pi^+ \pi^- J/\psi$
$(466 \pm 18) - i(223 \pm 28)$	4 BONVICINI	07	CLEO $D^+ \rightarrow \pi^- \pi^+ \pi^+$
$(484 \pm 17) - i(255 \pm 10)$	GARCIA-MAR.	07	RVUE $Ke4$
$(441^{+16}_{-8}) - i(272^{+9}_{-12.5})$	5 CAPRINI	06	RVUE $\pi\pi \rightarrow \pi\pi$
$(470 \pm 50) - i(285 \pm 25)$	6 ZHOU	05	RVUE
$(541 \pm 39) - i(252 \pm 42)$	7 ABLIKIM	04A	BES2 $J/\psi \rightarrow \omega \pi^+ \pi^-$
$(528 \pm 32) - i(207 \pm 23)$	8 GALLEGOS	04	RVUE Compilation
$(440 \pm 8) - i(212 \pm 15)$	9 PELAEZ	04A	RVUE $\pi\pi \rightarrow \pi\pi$
$(533 \pm 25) - i(247 \pm 25)$	10 BUGG	03	RVUE
532 - i272	BLACK	01	RVUE $\pi^0 \pi^0 \rightarrow \pi^0 \pi^0$
$(470 \pm 30) - i(295 \pm 20)$	5 COLANGELO	01	RVUE $\pi\pi \rightarrow \pi\pi$
$(535^{+48}_{-36}) - i(155^{+76}_{-53})$	11 ISHIDA	01	$\Upsilon(3S) \rightarrow \Upsilon \pi \pi$
$610 \pm 14 - i620 \pm 26$	12 SUROVTSEV	01	RVUE $\pi\pi \rightarrow \pi\pi, K\bar{K}$
$(558^{+34}_{-27}) - i(196^{+32}_{-41})$	ISHIDA	00B	$p\bar{p} \rightarrow \pi^0 \pi^0 \pi^0$



The case of $e^+e^- \rightarrow e^+e^-\eta$

$\Gamma(\gamma\gamma)$

VALUE (keV)

EVTS

DOCUMENT ID

TECN

COMMENT

\sqrt{s} (GeV)

0.510 ± 0.026 OUR FIT

0.510 ± 0.026 OUR AVERAGE

$0.51 \pm 0.12 \pm 0.05$

36

BARU

90

MD1

$e^+e^- \rightarrow e^+e^-\eta$

7.2-10.4

$0.490 \pm 0.010 \pm 0.048$

2287

ROE

90

ASP

$e^+e^- \rightarrow e^+e^-\eta$

29

$0.514 \pm 0.017 \pm 0.035$

1295

WILLIAMS

88

CBAL

$e^+e^- \rightarrow e^+e^-\eta$

9.4-10.6

$0.53 \pm 0.04 \pm 0.04$

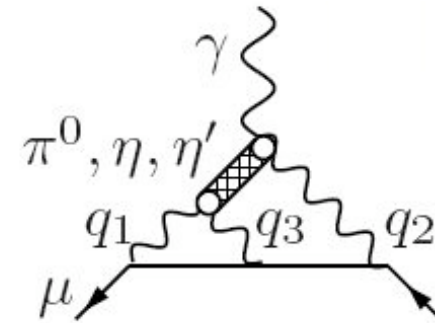
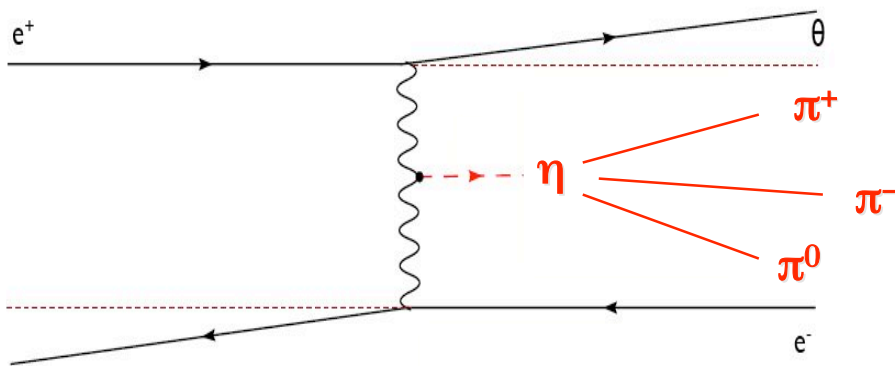
BARTEL

85E

JADE

$e^+e^- \rightarrow e^+e^-\eta$

34.6



$BR(\eta \rightarrow \pi^+\pi^-\pi^0) = 22.73\%$

major issue:

$e^+e^- \rightarrow \eta\gamma$ background

interests on the transition form factors

for LbyL contributions (A. Nyffeler, J. Prades) to

$g-2$...but need more statistics

\rightarrow KLOE-2 (see G. Venanzoni)

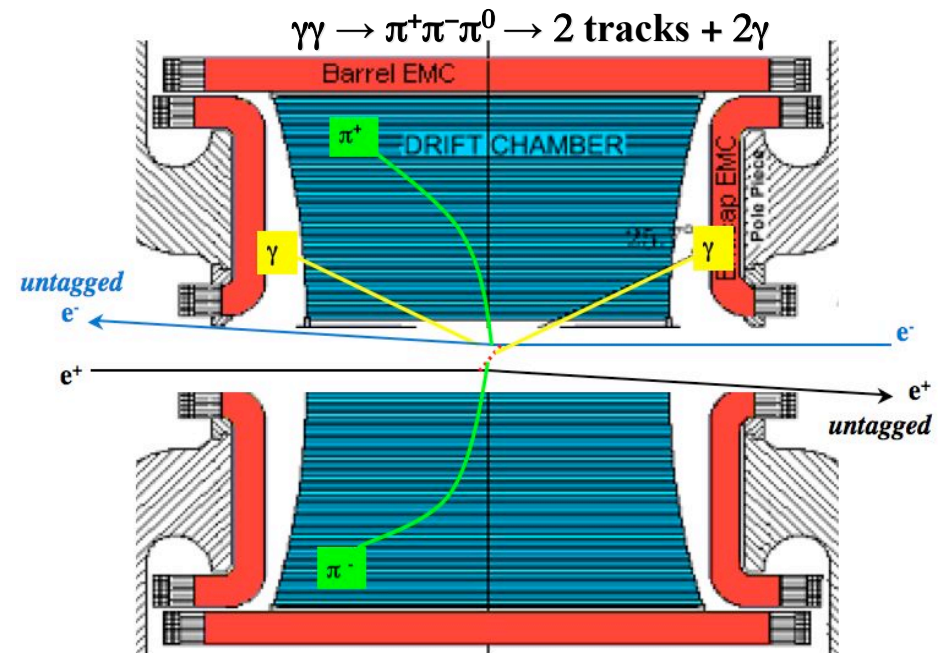
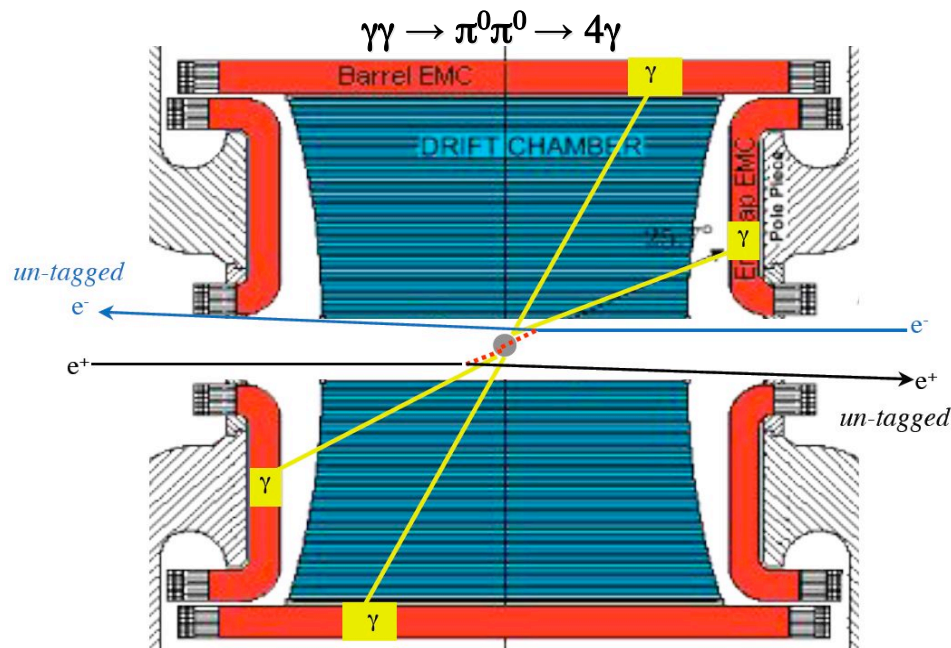
$$\sigma_{\gamma\gamma \rightarrow R}(q_1, q_2) \propto \Gamma_{R \rightarrow \gamma\gamma} \frac{8\pi^2}{M_R} \delta((q_1 + q_2)^2 - M_R^2) |F(q_1^2, q_2^2)|^2$$



$\gamma\gamma$ interactions at DAΦNE

- ✓ data collected at $\sqrt{s} = 1 \text{ GeV}$ (see S. Müller), suppressed ϕ decays
- ✓ instant luminosity = $7 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$, $\int \mathcal{L} dt \sim 250 \text{ pb}^{-1}$
- ✓ data processing with dedicated filter:

- at least 2 photons with energy $> 15 \text{ MeV}$, acceptance 20° - 160°
- the most energetic photon with energy $> 50 \text{ MeV}$
- total calorimetric energy $200 \text{ MeV} < E_{\text{calo}} < 900 \text{ MeV}$
- $R = (\sum_{\gamma} E_{\gamma}) / E_{\text{calo}} > 0.3$



Selection of $e^+e^- \rightarrow e^+e^-\pi^+\pi^-\pi^0$ events

- ✓ 2 tracks w/ opposite charge
- ✓ 2 and only 2 γ from the π^0 decay \rightarrow imposes the $\eta\gamma$ photon ($E_\gamma \sim 350$ MeV) to be lost in the beam pipe
- ✓ kinematic fit χ^2_η based on Lagrange multipliers
- ✓ for $\eta\gamma$ events, η system constrained in a small cone around $p_L \sim 350$ MeV and with $M_{miss} \sim 0$

$$M_{miss}^2 \approx s + M_\eta^2 - 2E_T\sqrt{s} - \frac{p_L^2}{E_T}\sqrt{s}$$

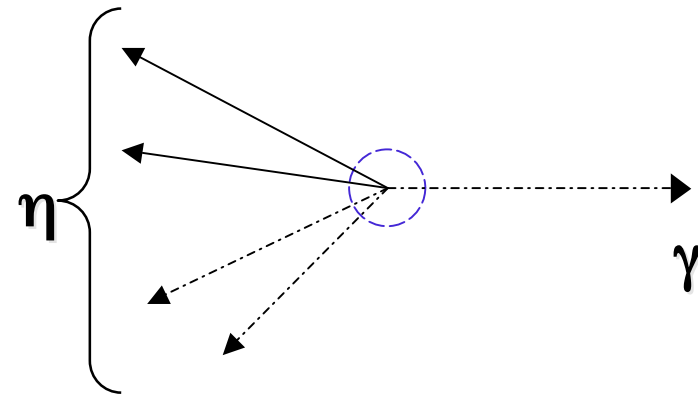
$$E_T = \sqrt{p_T^2 + M_\eta^2} \approx M_\eta$$

χ^2_η : 5 variables \times 2 γ
4 constraints

$$m_{\gamma\gamma}^2 = m_{\pi^0}^2$$

$$m_{\pi^+\pi^-\gamma\gamma}^2 = m_\eta^2$$

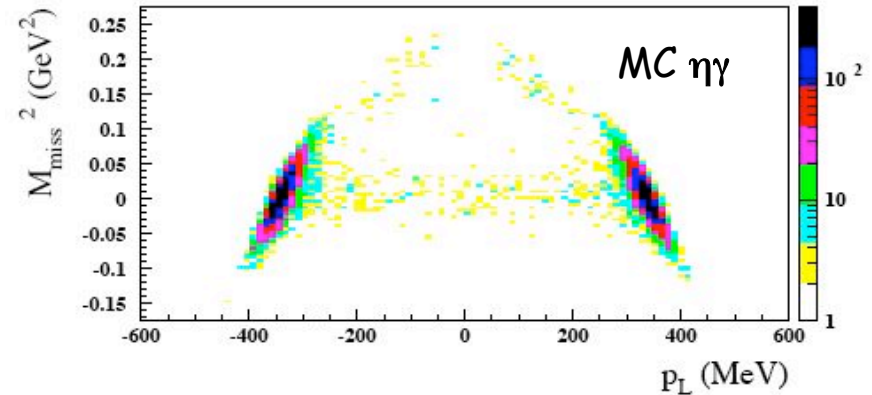
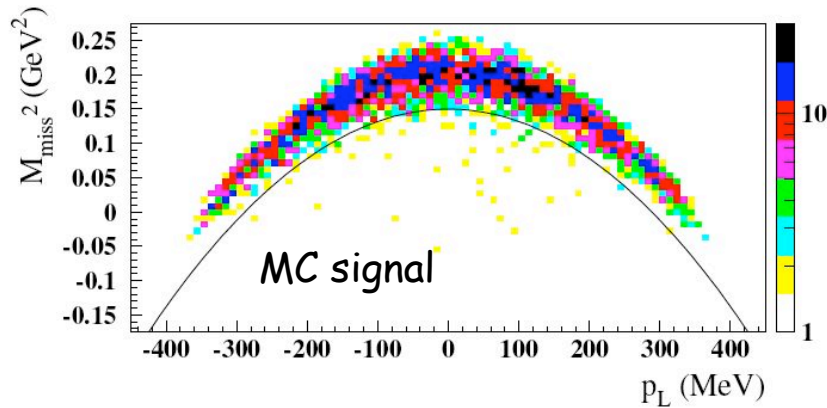
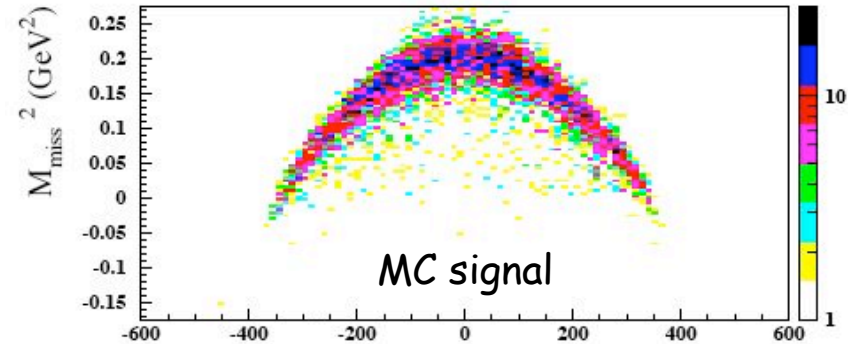
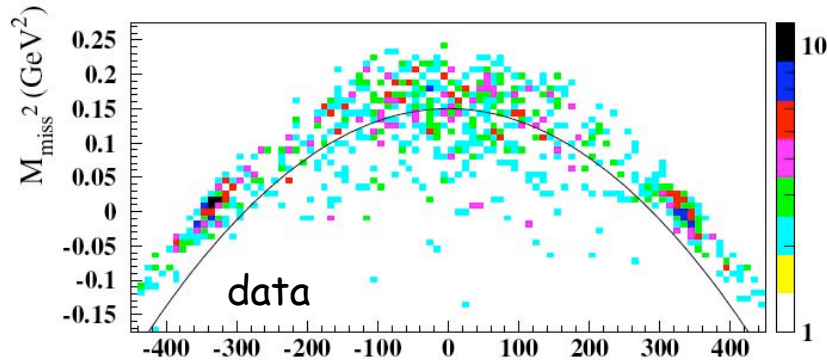
$$t_\gamma - |\underline{r}_\gamma| / c = 0 \text{ for } 2\gamma$$



from 239.6 pb⁻¹
1576 events survive selection



$e^+e^- \rightarrow e^+e^-\pi^+\pi^-\pi^0$: efficiencies and background



	$\eta\gamma$ $\eta \rightarrow \pi^+\pi^-\pi^0$	$\omega\pi^0$ $\omega \rightarrow \pi^+\pi^-\pi^0$	$\pi^+\pi^-\pi^0$	K^+K^- $\mu\nu, \pi^\pm\pi^0$	$K_S K_L$	$e^+e^-\gamma$
σ (nb)	0.23	5.7	30	8.6	2.0	400
ϵ	9.2×10^{-3}	6.3×10^{-5}	1.5×10^{-5}	1.9×10^{-5}	1.7×10^{-5}	$\mathcal{O}(10^{-7})$



signal: $\sigma = 0.043$ nb

Federico Nguyen
14-10-2009

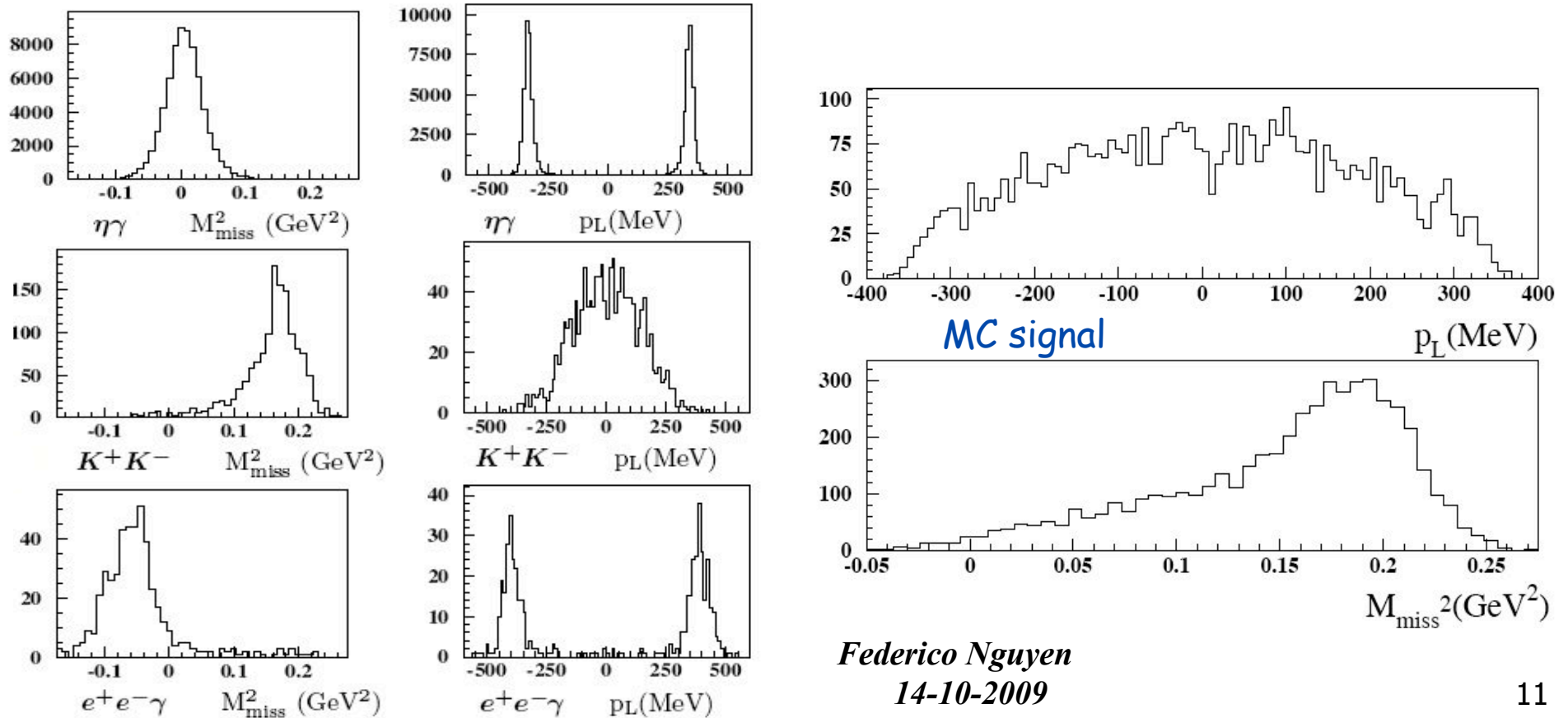
signal: $\epsilon_{\text{global}} = 20\%$

$e^+e^- \rightarrow e^+e^-\pi^+\pi^-\pi^0$: fit method

$$L = \prod_i P(d_i | w_S S_i + w_B B_i) P(s_i | S_i) P(b_i | B_i) \rightarrow \chi_{\text{fit}}^2 = -2 \ln L$$

w_S S_i w_B B_i s_i B_i
 ↑ ↑ ↑ ↑
 parameters generated MC statistics

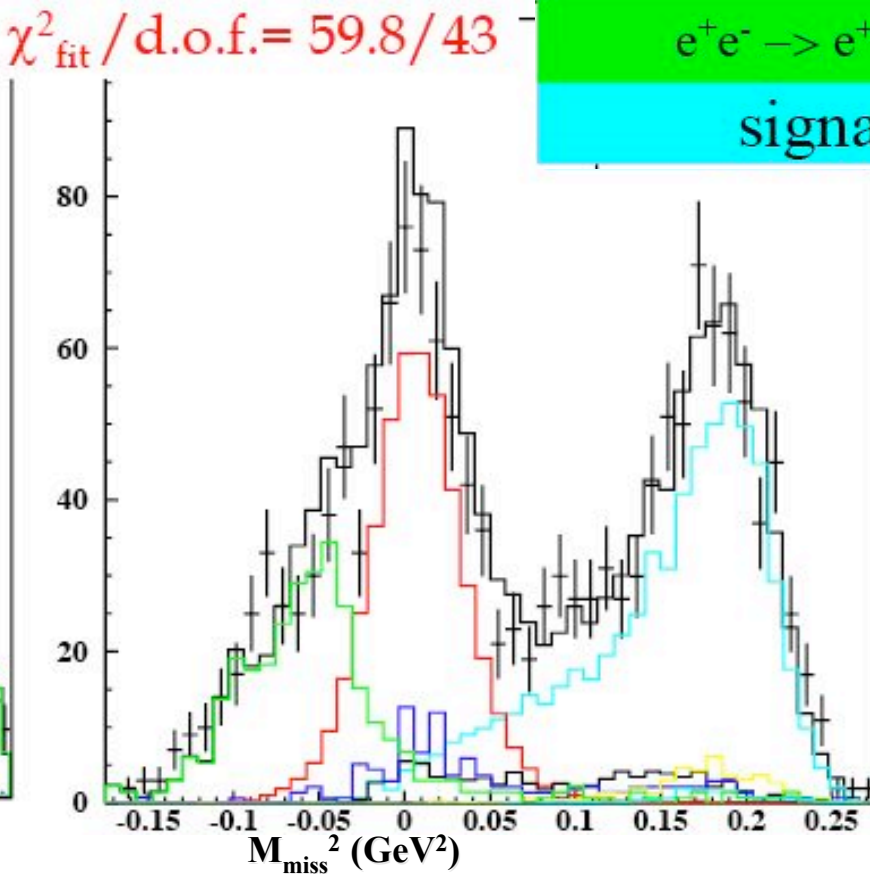
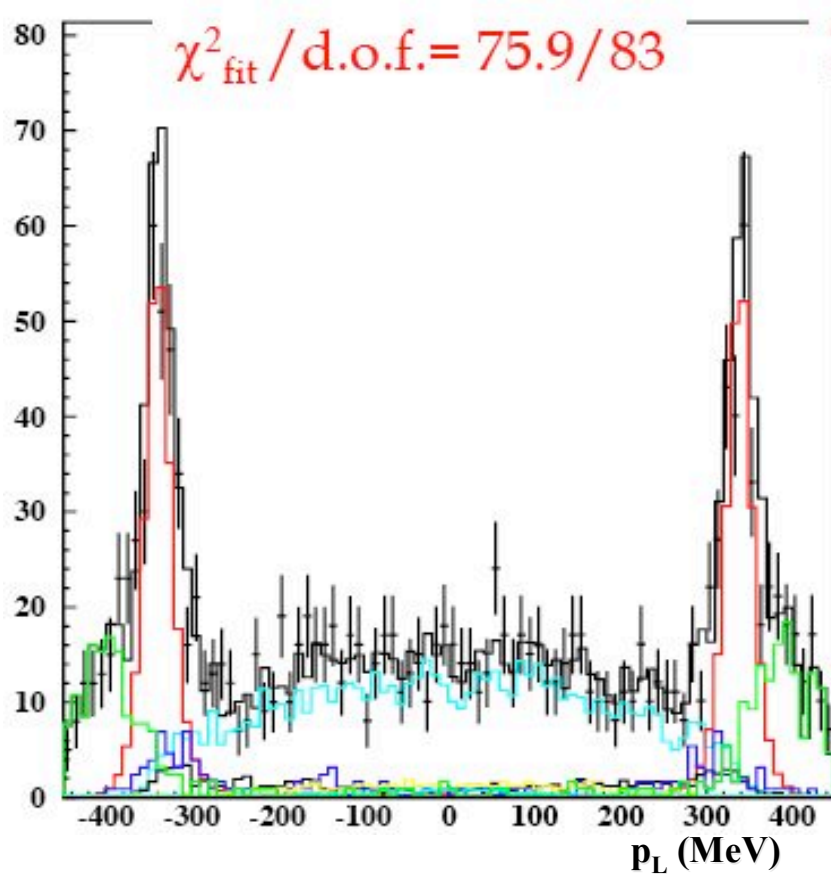
background yields constrained by present knowledge on cross sections



$e^+e^- \rightarrow e^+e^-\pi^+\pi^-\pi^0$: preliminary result

observation of $\gamma\gamma$ collisions @ 1 GeV

	signal	$\eta\gamma$	$\omega\pi^0$	$\pi^+\pi^-\pi^0$	K^+K^-	$K_S K_L$	$e^+e^-\gamma$
range variation	free	$\pm 15\%$	$\pm 1\%$	$\pm 7\%$	$\pm 25\%$	± 15	free
$N_{fit}(p_L)$	646	442	87	101	46	14	286
$N_{fit}(M_{miss}^2)$	625	442	87	101	46	14	303



$e^+e^- \rightarrow \eta\gamma \rightarrow \pi^+\pi^-\pi^0\gamma$

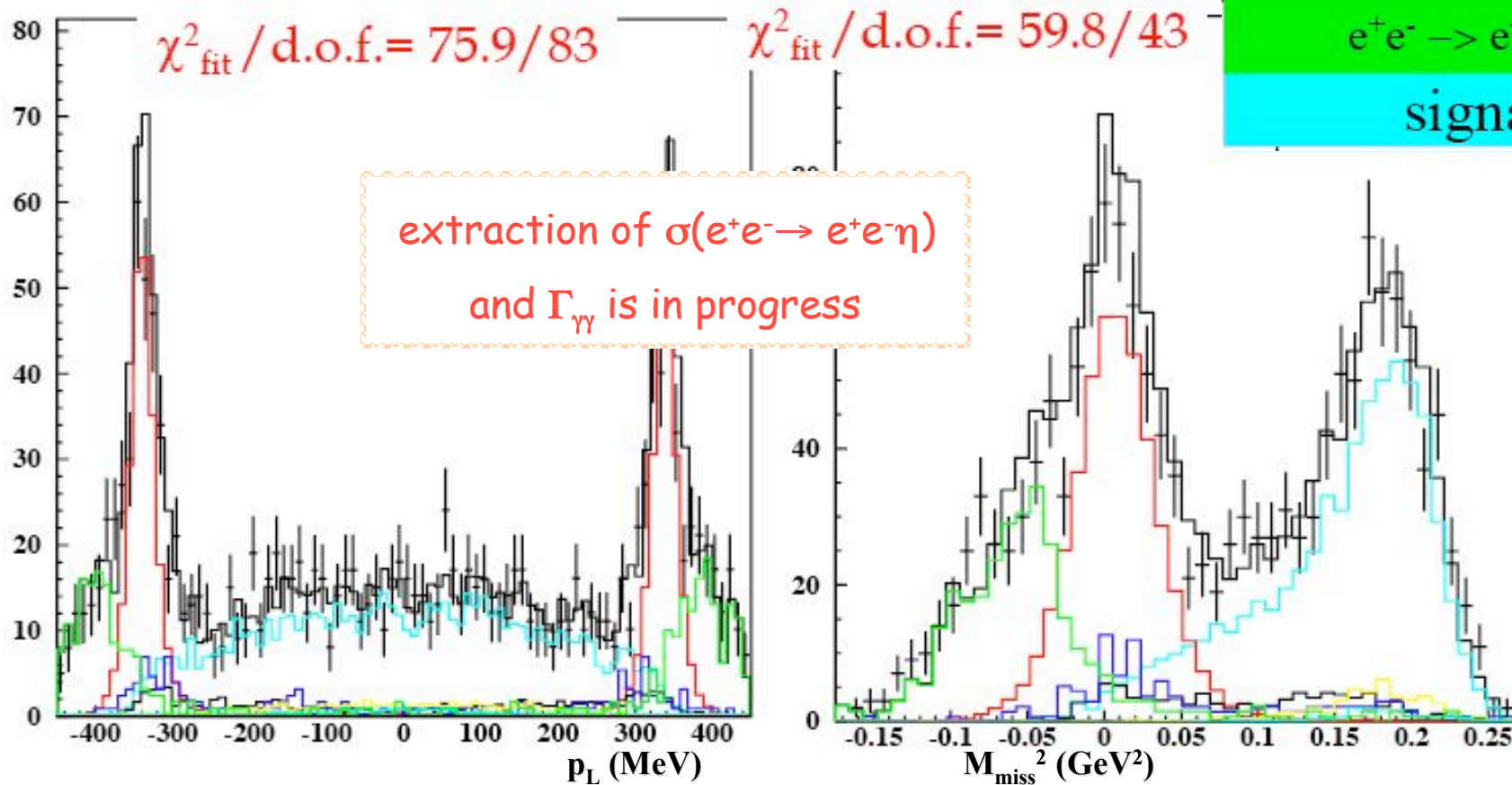
$e^+e^- \rightarrow e^+e^-\gamma$

signal

$e^+e^- \rightarrow e^+e^-\pi^+\pi^-\pi^0$: preliminary result

	signal	$\eta\gamma$	$\omega\pi^0$	$\pi^+\pi^-\pi^0$	K^+K^-	$K_S K_L$	$e^+e^-\gamma$
range variation	free	$\pm 15\%$	$\pm 1\%$	$\pm 7\%$	$\pm 25\%$	± 15	free
$N_{fit}(p_L)$	646	442	87	101	46	14	286
$N_{fit}(M_{miss}^2)$	625	442	87	101	46	14	303

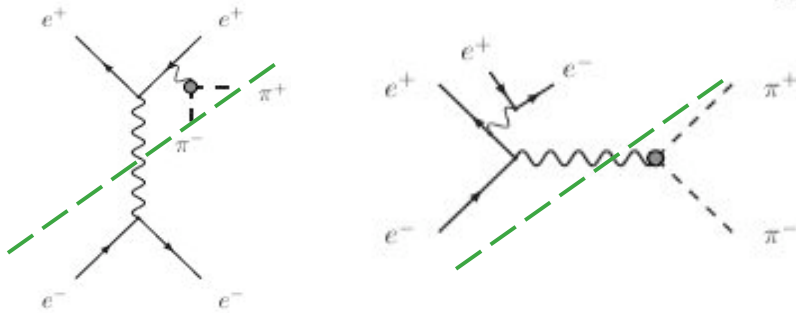
observation of $\gamma\gamma$ collisions @ 1 GeV



Search for $e^+e^- \rightarrow e^+e^-\pi^0\pi^0$

✓ only process to measure directly the $\sigma_{\gamma\gamma}$ coupling
 → infer structure

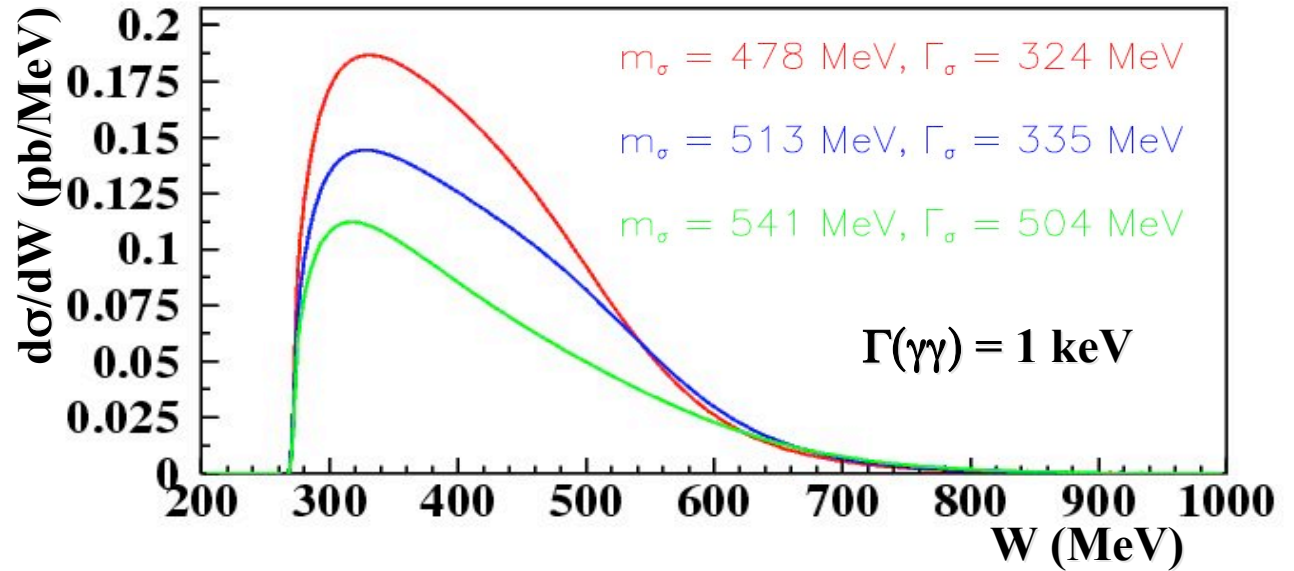
✓ $\pi^0\pi^0$ preferred wrt $\pi^+\pi^-$
 → vector states exchange switched off



and no background from $e^+e^- \rightarrow e^+e^-\mu^+\mu^-$



BW shape folded with $\gamma\gamma$ flux function



$f_0(600)$ PARTIAL WIDTHS

$\Gamma(\gamma\gamma)$	VALUE (keV)	DOCUMENT ID	TECN	COMMENT
•••	We do not use the following data for averages, fits, limits, etc. •••			
	1.2 ± 0.4	48 BERNABEU 08	RVUE	
	3.9 ± 0.6	49 MENNESSIER 08	RVUE	$\gamma\gamma \rightarrow \pi^+\pi^-, \pi^0\pi^0$
	4.1 ± 0.3	50 PENNINGTON 06	RVUE	$\gamma\gamma \rightarrow \pi^0\pi^0$
	3.8 ± 1.5	51,52 BOGLIONE 99	RVUE	$\gamma\gamma \rightarrow \pi^+\pi^-, \pi^0\pi^0$
	5.4 ± 2.3	51 MORGAN 90	RVUE	$\gamma\gamma \rightarrow \pi^+\pi^-, \pi^0\pi^0$
	10 ± 6	COURAU 86	DM1	$e^+e^- \rightarrow \pi^+\pi^-e^+e^-$

Identification of the $2\pi^0$ signal

- 4 γ with energy > 15 MeV, in acceptance
- no tracks

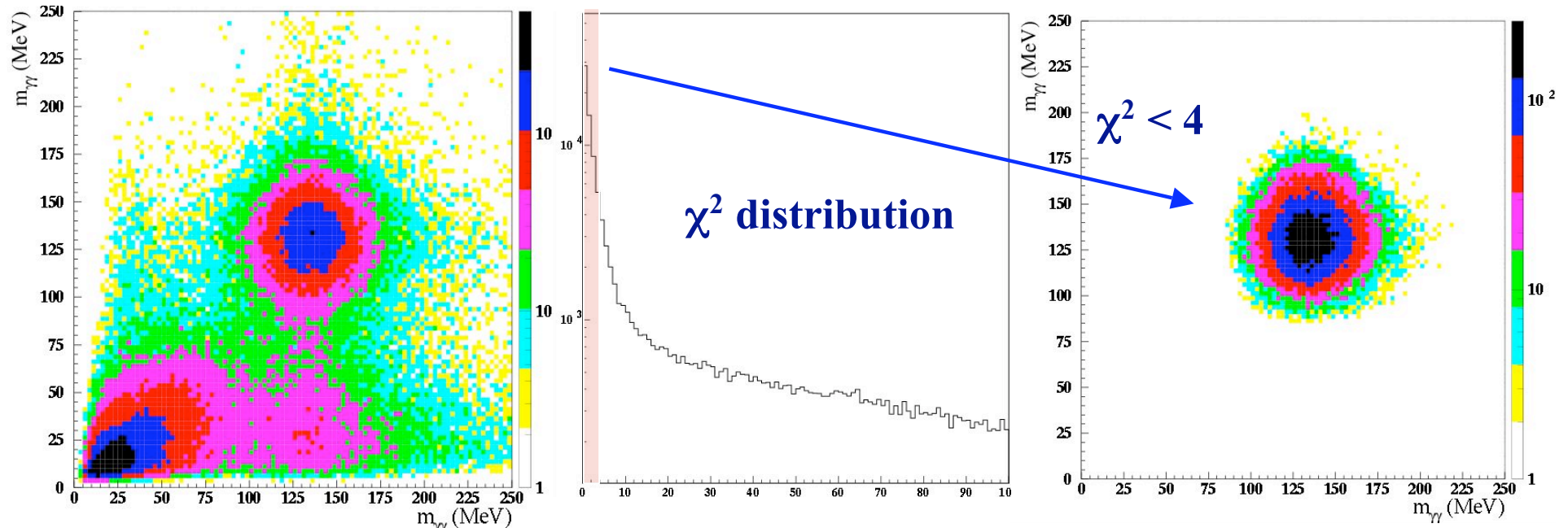
$$\chi_{pair}^2 = \left(\frac{M_{ij} - m_{\pi^0}}{\sigma(E_i, E_j)} \right)^2 + \left(\frac{M_{lk} - m_{\pi^0}}{\sigma(E_l, E_k)} \right)^2$$

$$\frac{\sigma_E}{E} \sim \frac{0.06}{\sqrt{E(\text{GeV})}}$$

$$\frac{\sigma(E_i, E_j)}{M_{ij}} = \frac{1}{2} \left(\frac{\sigma_{E_i}}{E_i} \oplus \frac{\sigma_{E_j}}{E_j} \right)$$

$$M_{ij}^2 = 2E_i E_j (1 - \cos\theta_{ij})$$

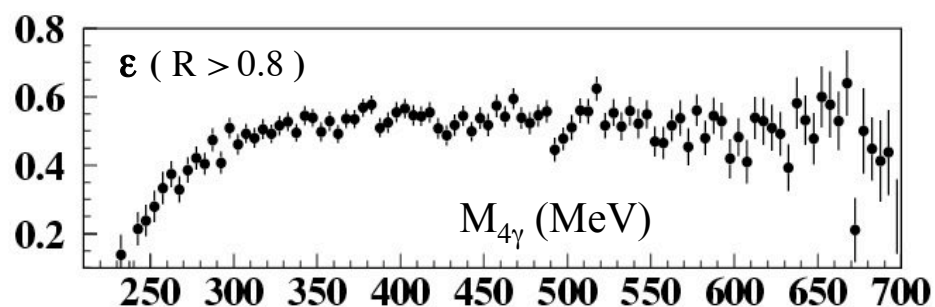
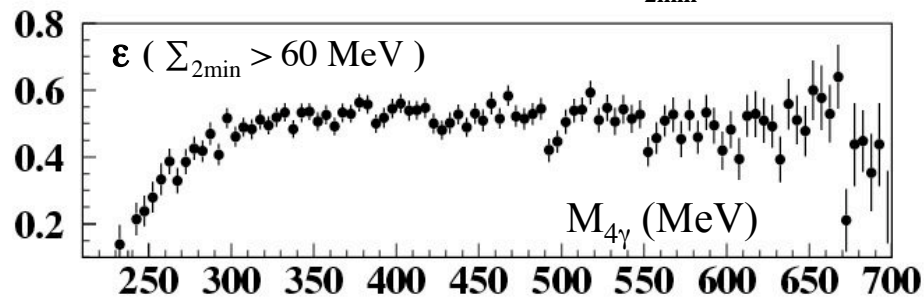
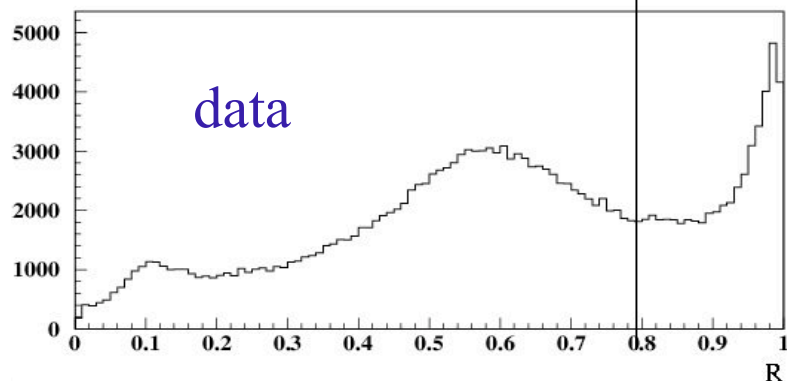
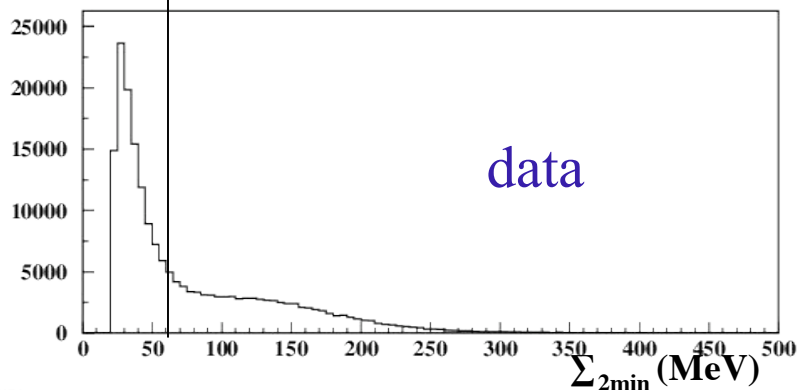
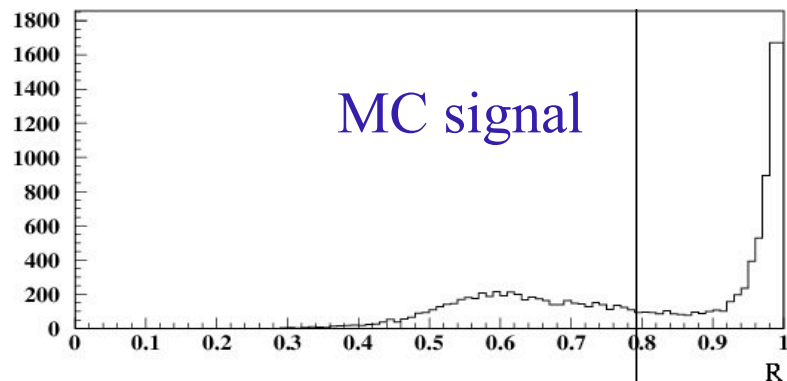
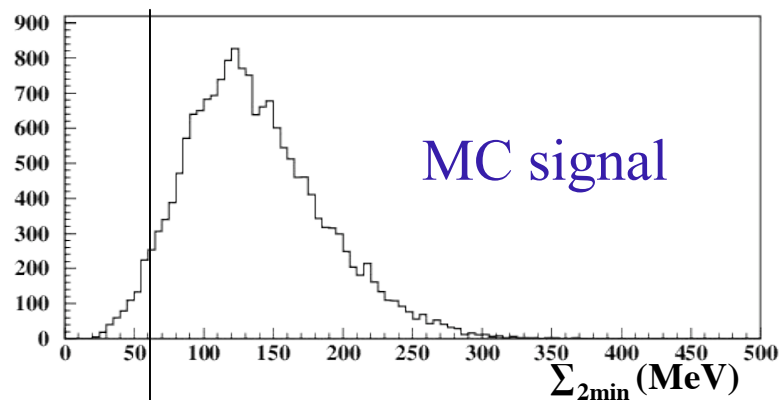
$m_{\gamma_1\gamma_2}$ vs. $m_{\gamma_3\gamma_4}$



$e^+e^- \rightarrow e^+e^-\pi^0\pi^0$: analysis cuts

$\Sigma_{2\min}$: sum of the energies of the two least energetic clusters

$$R = \frac{\sum_{i=1}^4 E_i}{E_{calo}}$$



$e^+e^- \rightarrow e^+e^-\pi^0\pi^0$: background shapes

4 and only 4 γ

$\chi^2 < 4$

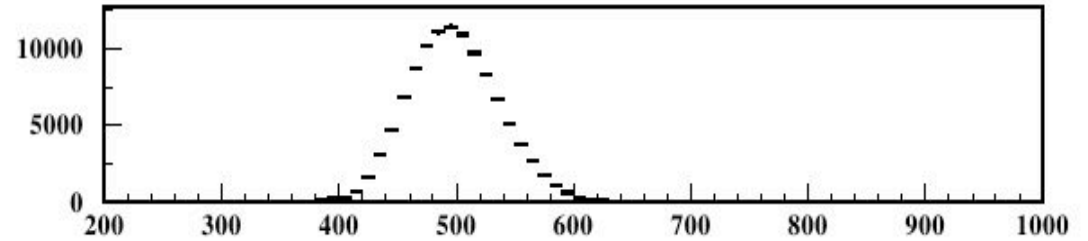
$R > 0.8$

$\sum_{2\min} > 60$ MeV

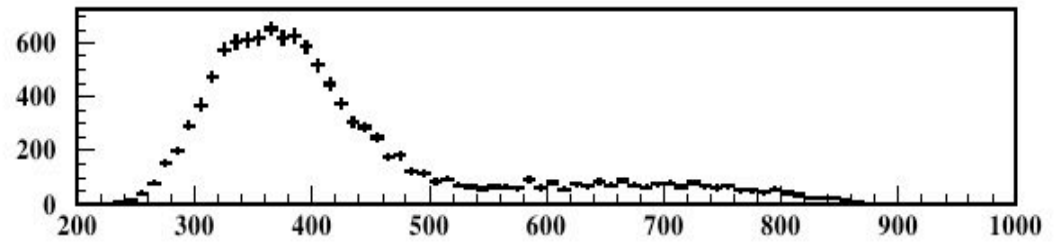
$p_T < 80$ MeV

no tracks

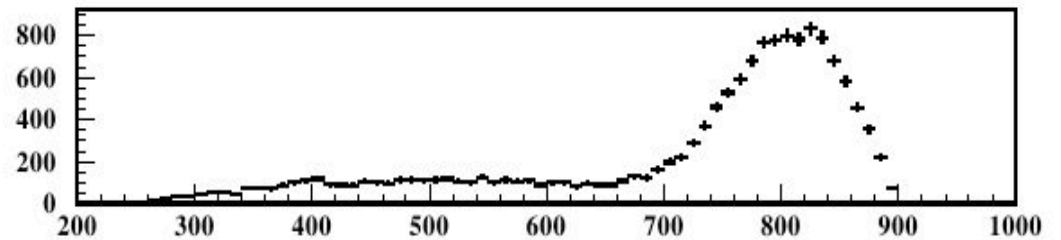
signal: $\epsilon_{\text{global}} \sim 0.23-0.29$



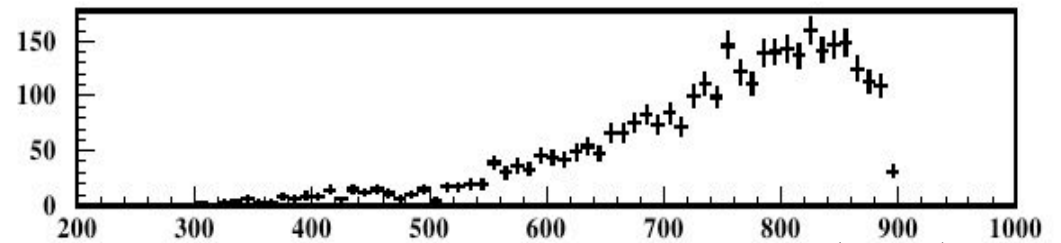
$K_S K_L \rightarrow \pi^0 \pi^0 K_L$



$\eta \rightarrow 3\pi^0$

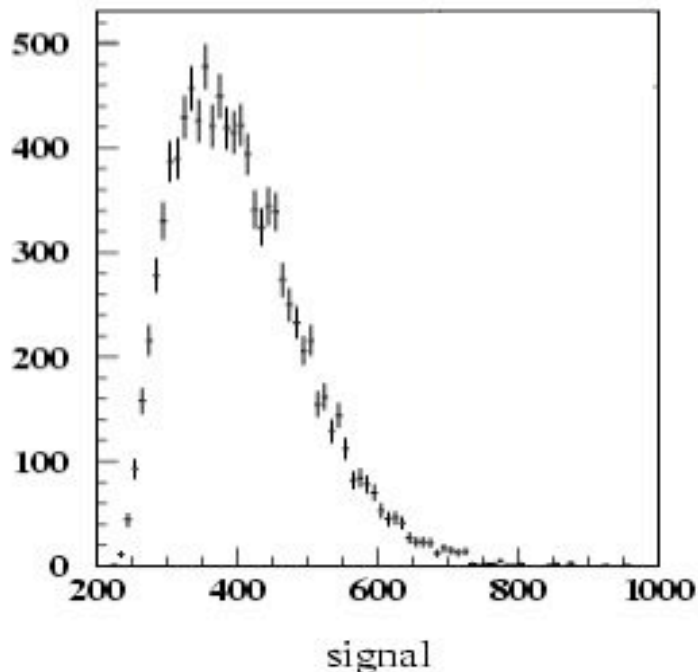


$\omega \pi^0 \rightarrow \gamma \pi^0 \pi^0$



$f_0 \rightarrow 2\pi^0$

$M_{4\gamma}$ (MeV)



signal

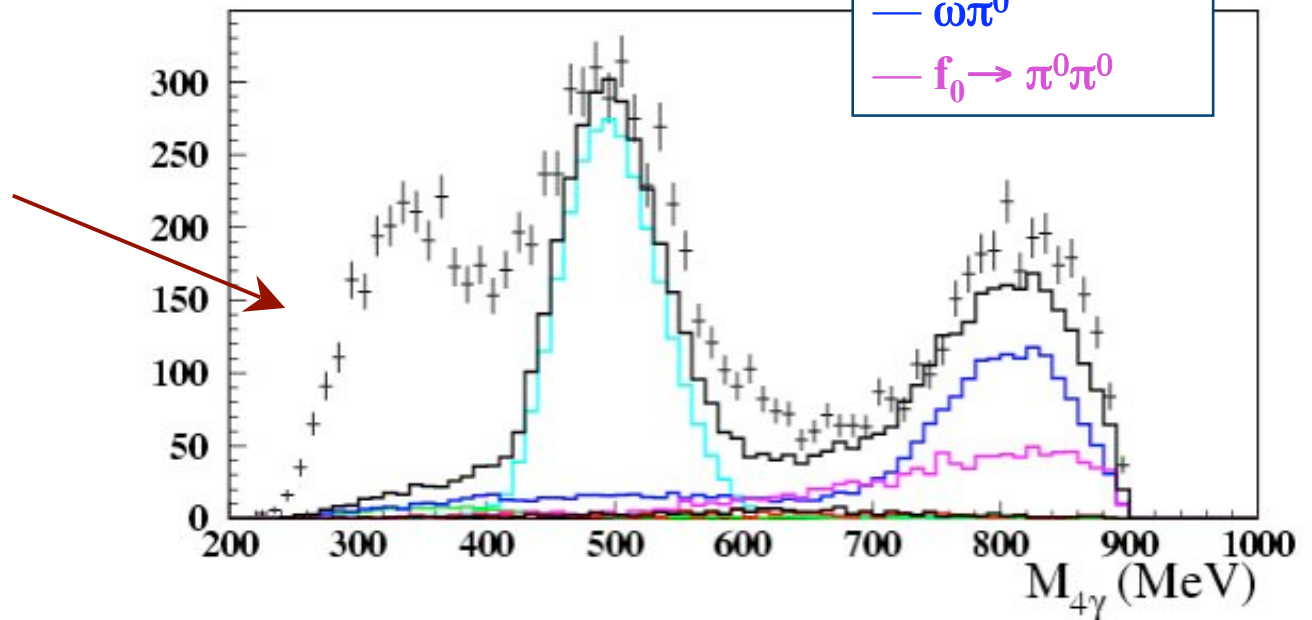
$e^+e^- \rightarrow e^+e^-\pi^0\pi^0$: expected background yields

	ϵ	σ (nb)	$n = \epsilon L \sigma$	$n/10188$
$K_S K_L$	5.60×10^{-3}	2.0	2 682	0.26
$\eta \rightarrow 3\pi^0$	1.79×10^{-3}	0.33	142	0.014
$\omega\pi^0$	1.55×10^{-2}	0.55	2 045	0.2
$f_0 \rightarrow 2\pi^0$	2.58×10^{-2}	0.17	1 052	0.10
$a_0 \rightarrow \eta\pi^0$	4.55×10^{-3}	0.11	120	0.012
$e^+e^- \rightarrow \gamma\gamma$	1.92×10^{-5}	360	166	0.016
$\eta \rightarrow \gamma\gamma$	1.57×10^{-4}	0.39	15	0.0014

from 239.6 pb⁻¹
10188 events after selection

we observe a clear evidence of $e^+e^- \rightarrow e^+e^-\pi^0\pi^0$ events at low $M_{4\gamma}$

the precise yield estimate depends on assumptions for the background processes



$e^+e^- \rightarrow e^+e^-\pi^0\pi^0$: expected background yields

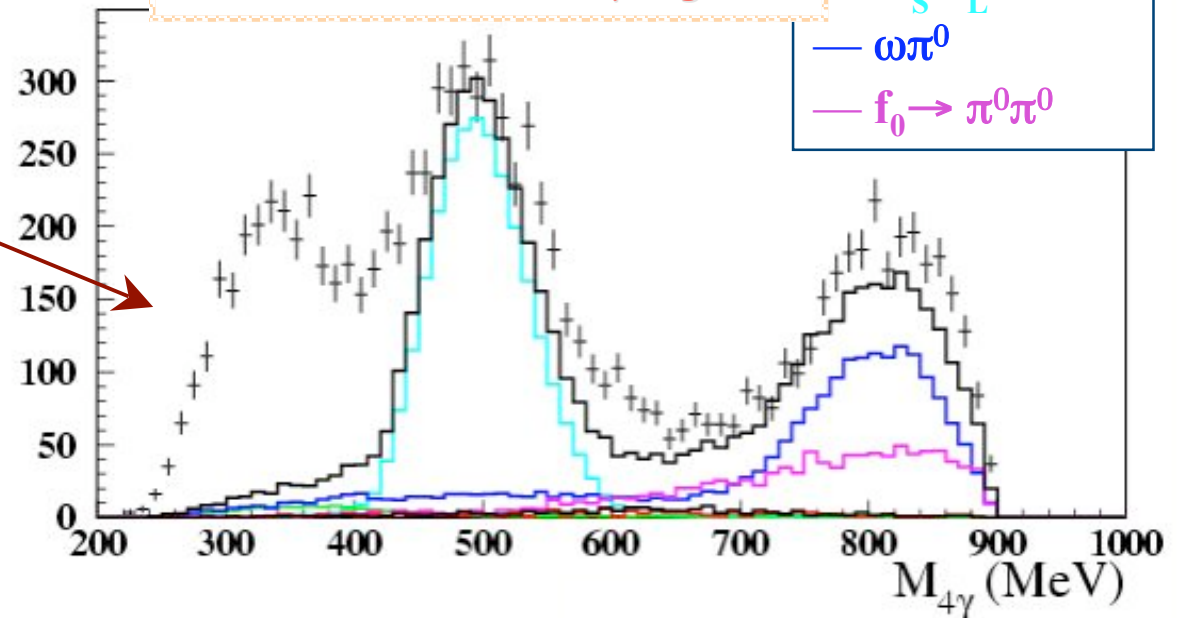
	ϵ	σ (nb)	$n = \epsilon L \sigma$	$n/10188$
$K_S K_L$	5.60×10^{-3}	2.0	2 682	0.26
$\eta \rightarrow 3\pi^0$	1.79×10^{-3}	0.33	142	0.014
$\omega\pi^0$	1.55×10^{-2}	0.55	2 045	0.2
$f_0 \rightarrow 2\pi^0$	2.58×10^{-2}	0.17	1 052	0.10
$a_0 \rightarrow \eta\pi^0$	4.55×10^{-3}	0.11	12	
$e^+e^- \rightarrow \gamma\gamma$	1.92×10^{-5}	360	16	
$\eta \rightarrow \gamma\gamma$	1.57×10^{-4}	0.39	1	

from 239.6 pb⁻¹
10188 events after selection

subtraction of backgrounds
and study of differential
cross section are in progress

we observe a clear evidence
of $e^+e^- \rightarrow e^+e^-\pi^0\pi^0$ events at
low $M_{4\gamma}$

the precise yield estimate
depends on assumptions for
the background processes



Conclusions

- ✓ unambiguous signature of both $\gamma\gamma \rightarrow \eta$ and $\gamma\gamma \rightarrow \pi^0\pi^0$ events, without any tagger and at $\sqrt{s} = 1 \text{ GeV}$
- ✓ $\gamma\gamma \rightarrow \eta$ observed through the $e^+e^- \rightarrow e^+e^- \eta$ process, with the $\eta \rightarrow \pi^+\pi^-\pi^0$ channel
- ✓ collected statistics allows to measure $\Gamma_{\gamma\gamma}(\eta)$ with accuracy comparable with existing measurements
- ✓ an exploratory research shows a structure (~ 4000 events) in the 4 γ invariant mass, where the process $e^+e^- \rightarrow e^+e^- \sigma \rightarrow e^+e^- \pi^0\pi^0$ is expected
- ✓ studies are under way to describe the $e^+e^- \rightarrow e^+e^- \pi^0\pi^0$ differential cross section to understand the σ meson contribution



KLOE and DAΦNE

- ✓ data collected at $\sqrt{s} = 1 \text{ GeV}$, suppressed ϕ decays
- ✓ instant luminosity = $7 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$, $\int \mathcal{L} dt = 239.6 \text{ pb}^{-1}$

Calorimeter, EmC:

Pb/Scint. Fiber, 4880 PMTs

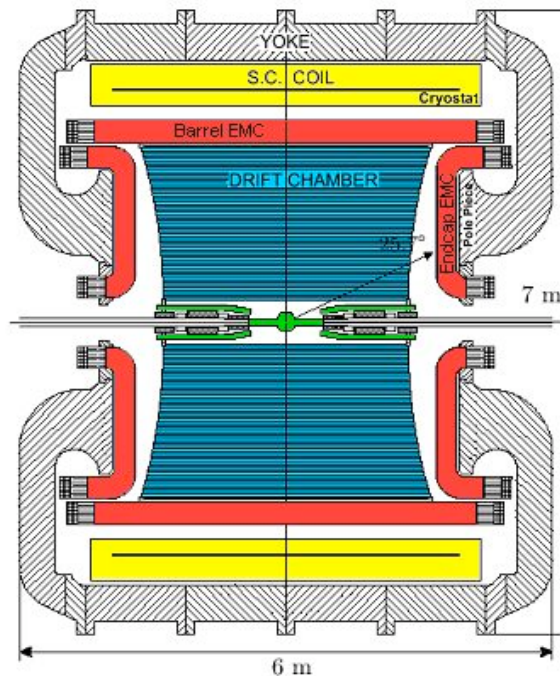
98% of solid angle

$$\sigma_E / E = 0.057 / \sqrt{E} \text{ (GeV)}$$

$$\sigma_t = 57 \text{ ps} / \sqrt{E} \text{ (GeV)} \oplus 50 \text{ ps}$$

$$\sigma_{\perp} = 1.3 \text{ cm}$$

both detectors
w/ trigger decision



Drift Chamber, DC:
4 m \varnothing \times 3.3 m length
90% He, 10% $i\text{-C}_4\text{H}_{10}$
12582 stereo sense wires

$$\sigma_p / p = 0.4\% \text{ for } \theta > 45^\circ$$

$$\sigma_{r\varphi} = 0.150 \text{ mm}, \sigma_z = 2 \text{ mm}$$

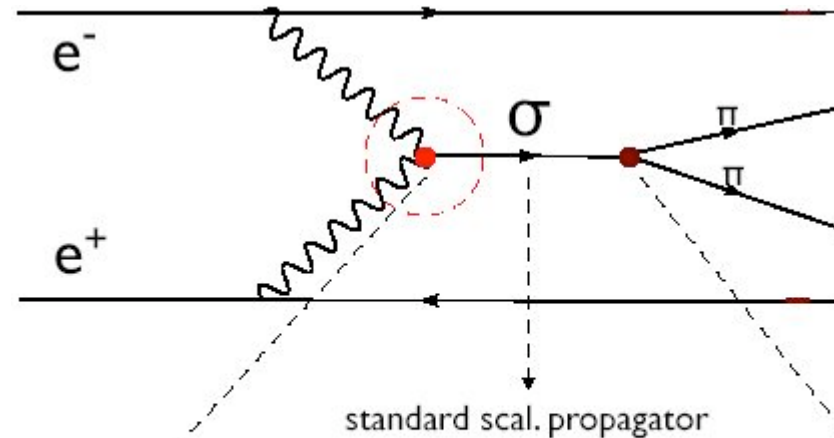
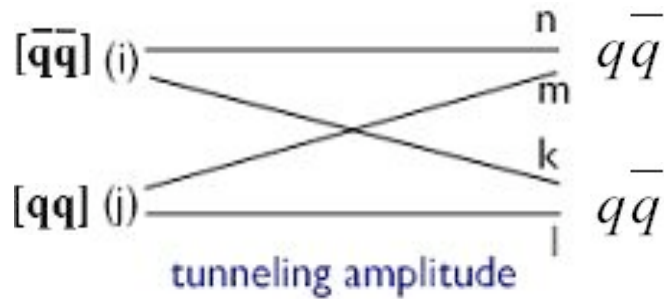
$$\sigma(m_{\pi\pi}) \sim 1 \text{ MeV}$$

✓ no e^\pm tagging device



Federico Nguyen
14-10-2009

The model for the σ produced in $\gamma\gamma$ (I)



$$\frac{\mathcal{A}}{M_\sigma^2} \phi_\sigma F^{\mu\nu} F_{\mu\nu}$$

leading SU_3 coupling

$$\mathcal{A} \epsilon_{jlm} \epsilon^{ikn} S_i^j \Pi_k^l \Pi_n^m$$

- 1) the σ is a bound state made up of 2 diquarks, each diquark being a $[qq]_{\bar{3}_c, 1_s, \bar{3}_f}$

$$S = \begin{pmatrix} \frac{f_0+a^0}{\sqrt{2}} & a^+ & \kappa^+ \\ a^- & \frac{f_0-a^0}{\sqrt{2}} & \kappa^0 \\ \kappa^- & \bar{K}^0 & \sigma_0 \end{pmatrix}$$

- 2) the decay into 2 mesons is described by the probability of breaking each diquark shell, the coupling \mathcal{A}

$$\Pi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta_8 \end{pmatrix}$$



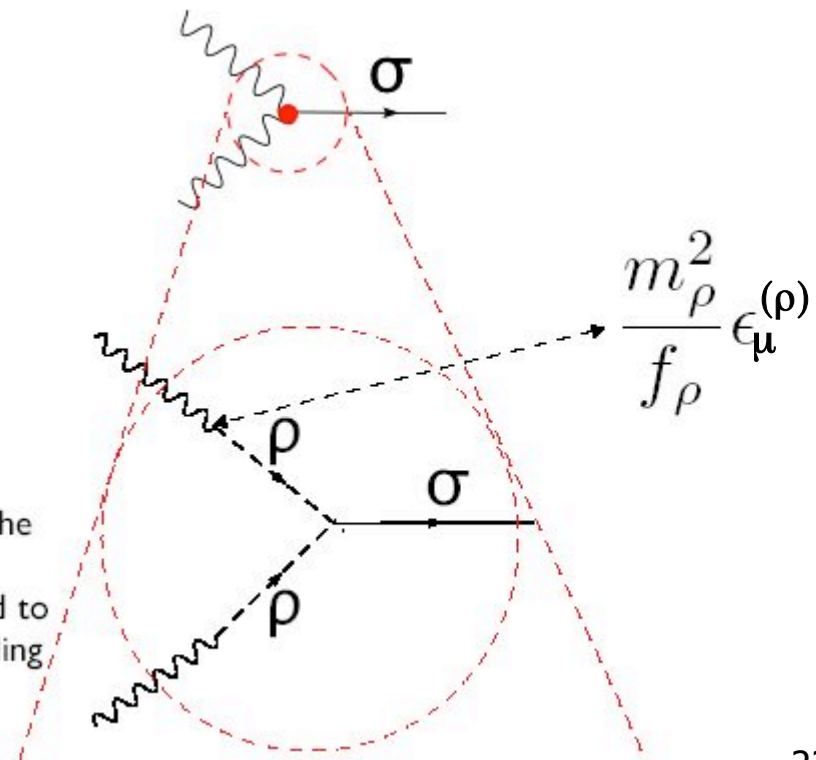
The model for the σ produced in $\gamma\gamma$ (II)

$$\mathbf{V} = \begin{pmatrix} \frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & \rho^+ & K^{*+} \\ \rho^- & -\frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & K^{*0} \\ K^{*-} & \bar{K}^{*0} & \phi \end{pmatrix}$$

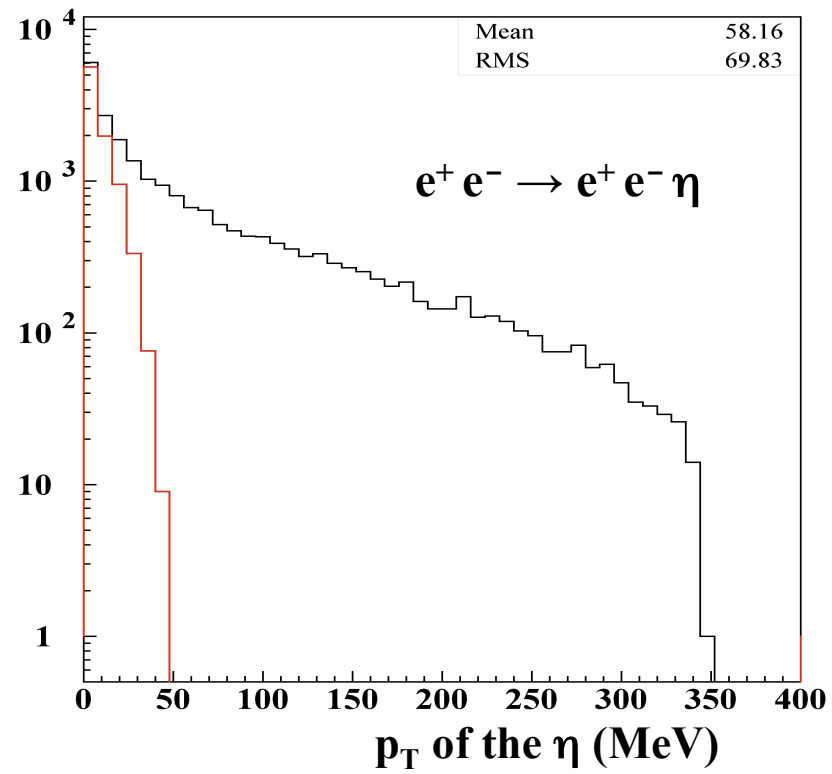
1) the $\sigma\gamma\gamma$ coupling is parameterized by a similar dynamics, i. e. the breaking of the diquark shells into 2 ordinary $q\bar{q}$, but vector mesons, again the coupling A

2) the vector meson-photon transition is described by the standard **VMD**

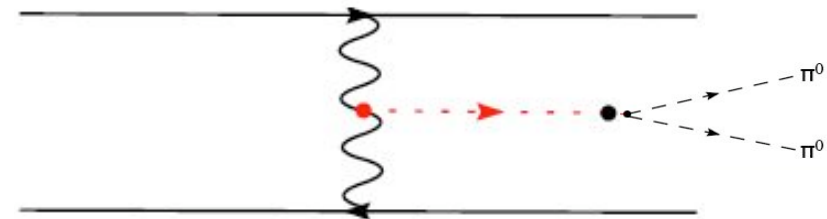
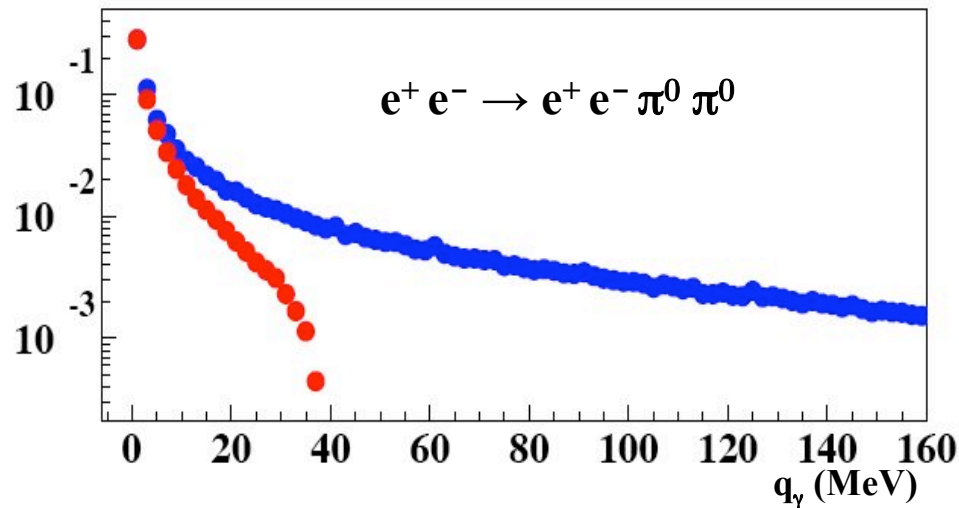
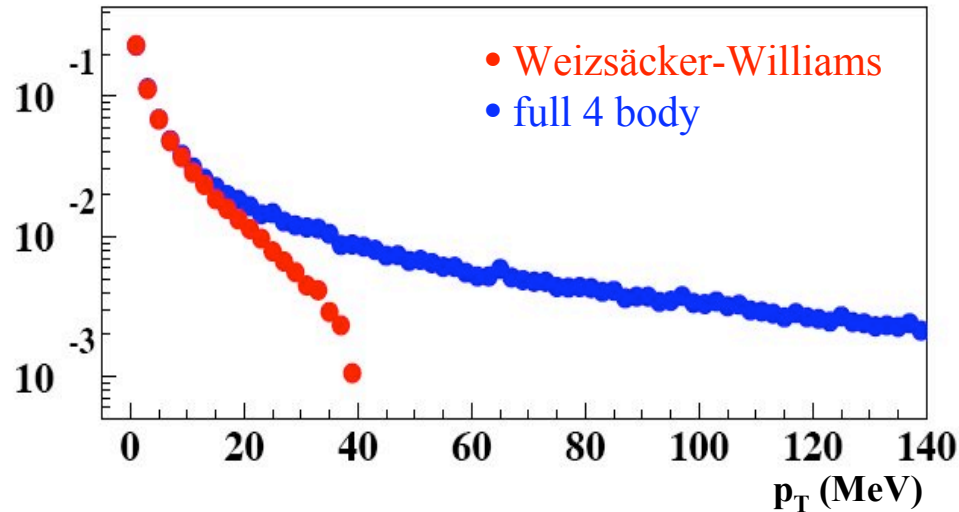
This is why we use again A on the 2-photon vertex.
The SU_3 of vectors V_j is assumed to be controlled by the same coupling



Spares



Comparison btw W.W. and phase space



1) the σ is a bound state made up of 2 diquarks, each diquark being a $[qq]_{\bar{3}_c, 1_s, \bar{3}_f}$

2) the decay into 2 mesons or 2 photons is described by the probability of breaking each diquark shell

F.N., F. Piccinini & A. Polosa
Eur.Phys.J.C47(2006)65

W.W. is reproduced with a cut
 $\theta < 5^\circ$ for both e^+e^- in the final state

Federico Nguyen
14-10-2009

