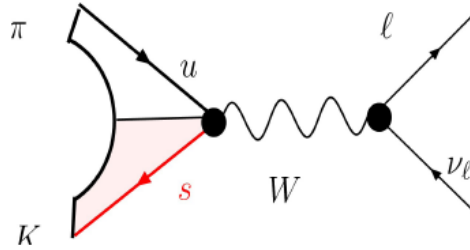


E. De Lucía (LNF-INFN)  
for the KLOE Collaboration

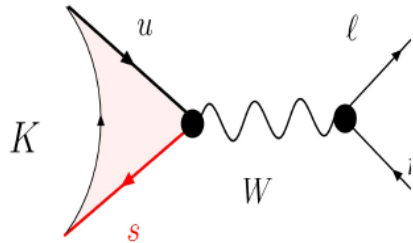
$\nu_{\mu}$  and lepton universality  
with kaons at KLOE

# Kaon Physics



$$\mathbf{K}_{\ell 3}: K \rightarrow \pi \ell \nu$$

Vector transition: only 2<sup>nd</sup> order SU(3) breaking [Ademollo-Gatto]



$$\mathbf{K}_{\ell 2}: K \rightarrow \ell \nu$$

Helicity suppressed:  
Sensitivity to NP enhanced

- ❖ Precise determination of  $V_{us}$
- ❖ Test of **Lepton universality**  $K_{e3}$  vs  $K_{\mu 3}$
- ❖ Most precise test of **CKM unitarity**

$$|V_{ud}|^2 + |V_{us}|^2 = 1 \quad |V_{ub}|^2 \text{ negligible}$$

- ❖ **Lepton-Quark universality of weak int.**

$$G_F^2 \equiv G_{\text{CKM}}^2 = (|V_{ud}|^2 + |V_{us}|^2) G_F^2$$

- ❖ Precise determination of  $V_{us}/V_{ud}$
- ❖ **Test of Physics beyond the SM**
  - right-handed contributions to charged weak currents
  - charged Higgs exchange (2 Higgs doublet scenarios)

$$\left. \begin{array}{l} \Gamma(K_{\mu 2}) / \Gamma(\pi_{\mu 2}) \\ \Gamma(K_{e 2}) / \Gamma(K_{\mu 2}) \end{array} \right\}$$

- ❖ **Lepton Flavor Violation test with  $\Gamma(K_{e 2})/\Gamma(K_{\mu 2})$**

# Kaon physics (II)

## ❖ Set bounds on New Physics from Lepton-Quark Universality

New Physics extensions of the SM can break gauge universality in the form of tree or loop level contributions to muon decays and/or semileptonic processes.

- i. *Exotic Muon Decays* would contribute to the muon lifetime

$$|\mathbf{V}_{ud}|^2 + |\mathbf{V}_{us}|^2 + |\mathbf{V}_{ub}|^2 = 1 - \mathbf{BR}(\text{exotic muon decays})$$

*Provides best limit on  $\mathbf{BR}(\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_\mu)$  better than direct search*

- ii. *Additional Z' Gauge Bosons* contributing at loop level to muons and semileptonic decays differently (*Competitive with direct search*) [PRD 35 (1987)]
- iii. SUSY particle loops affecting muon and semileptonic decays differently: constraints on *slepton-squark mass difference* (x2-3 precision needed) [PRL 75 (1995) , PRL 88 (2002)]

Present accuracy set bounds on the scale of New Physics  $\Lambda_{\text{NP}}$  at 1-2 TeV

$$|\mathbf{V}_{ud}|^2 + |\mathbf{V}_{us}|^2 + |\mathbf{V}_{ub}|^2 = 1 + \epsilon_{\text{NP}} \quad \epsilon_{\text{NP}} \approx M_W^2 / \Lambda_{\text{NP}}^2$$

# $V_{us}$ from $K_{l3}$ rates

$$\Gamma(K_{l3}(\gamma)) = \frac{C_K^2 G_F^2 M_K^5}{192\pi^3} S_{EW} |V_{us}|^2 |f_+^{K^0\pi^-}(0)|^2 \times I_{Kl}(\{\lambda\}_{Kl}) (1 + 2\Delta_K^{SU(2)} + 2\Delta_{Kl}^{EM})$$

with  $K \in \{K^+, K^0\}$ ;  $l \in \{e, \mu\}$ , and:

$C_K^2$  1/2 for  $K^+$ , 1 for  $K^0$

## Inputs from theory:

- $S_{EW}$  Universal short distance EW correction (1.0232)
- $f_+^{K^0\pi^0}(0)$  Hadronic matrix element at zero momentum transfer ( $t=0$ )
- $\Delta_K^{SU(2)}$  Form factor correction for strong SU(2) breaking
- $\Delta_{Kl}^{EM}$  Long distance EM effects

## Inputs from experiment:

- $\Gamma(K_{l3}(\gamma))$  **Branching ratios** with well determined treatment of radiative decays; **lifetimes**
- $I_{Kl}(\lambda)$  Phase space integral:  $\lambda$ s parameterize form factor dependence on  $t$ :
  - $K_{e3}$ : **only**  $\lambda_+$  (or  $\lambda_+$ ,  $\lambda_+$ )
  - $K_{\mu 3}$ : **need**  $\lambda_+$  and  $\lambda_0$

KLOE has measured all relevant inputs for charged and neutral kaons: BR's, lifetimes ( $\tau_{K^{\pm}, K^0}$ ), form factors (FFs)

# To extract $V_{us}$ from neutral kaons

PLB 632 (2006)

$$\text{BR}(K_{e3}) = 0.4008(15) \quad 0.37\%$$

$$\text{BR}(K_{\mu3}) = 0.2699(14) \quad 0.52\%$$

Based on  $13 \times 10^6$   $K_L$  decays tagged by  $K_S \rightarrow \pi^+ \pi^-$

PLB 626 (2005)

$$\tau_L = 50.92(30) \text{ ns} \quad 0.58\%$$

Fit the time dependence over  $0.4\tau_L$  of  $8.5 \times 10^6$   $K_L \rightarrow \pi^0 \pi^0 \pi^0$  decays tagged by  $K_S \rightarrow \pi^+ \pi^-$

*(P. de Simone talk)*

PLB 636 (2006)

$$\text{BR}(K_S \rightarrow \pi e \nu) = 7.046(91) \times 10^{-4} \quad 1.3\%$$

From tagged  $K_S$  beam  $1.2 \times 10^8$  events

PLB 636 (2006)

$$\lambda'_+ \times 10^3 \quad \lambda''_+ \times 10^3$$

$$25.5 \pm 1.8 \quad 1.4 \pm 0.8$$

Based on  $2 \times 10^6$   $K_L e3$  decays tagged by  $K_S \rightarrow \pi^+ \pi^-$

JHEP12(2007)

$$\lambda'_+ = (25.6 \pm 1.5_{\text{stat}} \pm 0.9_{\text{syst}}) \times 10^{-3}$$

$$\lambda''_+ = (1.5 \pm 0.7_{\text{stat}} \pm 0.4_{\text{syst}}) \times 10^{-3}$$

$$\lambda_0 = (15.4 \pm 1.8_{\text{stat}} \pm 1.3_{\text{yst}}) \times 10^{-3}$$

Based on  $1.8 \times 10^6$   $K_L \mu3$  decays tagged by  $K_S \rightarrow \pi^+ \pi^-$  and from combined fit with  $K_L e3$  data

# To extract $V_{us}$ from charged kaons

PLB 632 (2006)

$$\text{BR}(K^+ \rightarrow \mu^+ \nu) = 0.6366(17)$$

0.27%

From  $4.2 \times 10^6 \phi \rightarrow K^+ K^-$  tagged by  $K_{\mu 2}^-$  decays

JHEP 01 (2008)

$$\tau^\pm = 12.347(30)$$

0.24%

From  $15 \times 10^6 \phi \rightarrow K^+ K^-$  tagged by  $K_{\mu 2}$  decays

JHEP 02 (2008)

$$\text{BR}(K^\pm \rightarrow \pi^0 e^\pm \nu) = 0.04965(53)$$

1%

$$\text{BR}(K^\pm \rightarrow \pi^0 \mu^\pm \nu) = 0.03233(39)$$

1.2%

From  $6 \times 10^7 \phi \rightarrow K^+ K^-$  decays tagged by both  $K_{\mu 2}$  and  $K_{\pi 2}$  decays

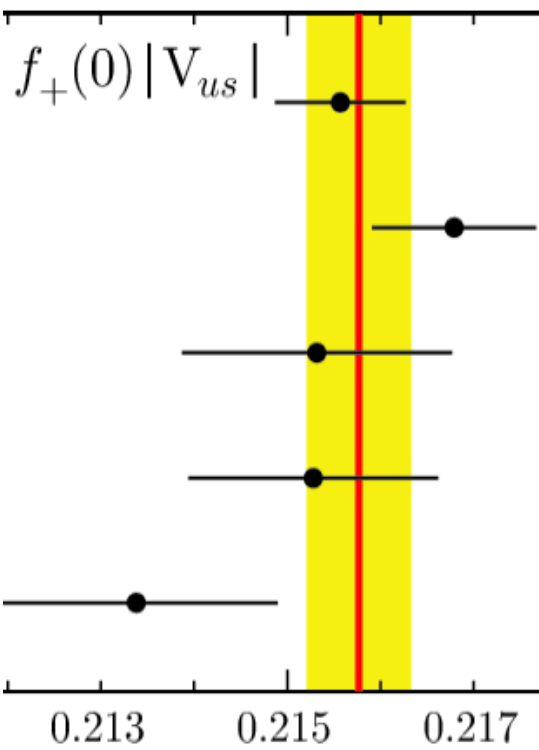
PLB 666 (2008)

$$\text{BR}(K^+ \rightarrow \pi^+ \pi^0 (\gamma)) = 0.2065(9)$$

0.43%

From  $20 \times 10^6 \phi \rightarrow K^+ K^-$  decays tagged by both  $K_{\mu 2}^-$  and  $K_{\pi 2}^-$  decays

# $|V_{us}| f_+(0)$ at KLOE



Decay Mode	Value	err %
$K_L e3$	0.2155(7)	0.3
$K_L \mu3$	0.2167(9)	0.4
$K_S e3$	0.2152(14)	0.7
$K^\pm e3$	0.2152(13)	0.6
$K^\pm \mu3$	0.2132(15)	0.7

All KLOE exp. inputs  
but  $K_S$  lifetime (*M. Dreucci talk*)

## Lepton universality

$$r_{\mu e} \equiv \frac{|f_+(0) V_{us}|_{\mu 3, \text{exp}}^2}{|f_+(0) V_{us}|_{e 3, \text{exp}}^2} = \frac{g_\mu^2}{g_e^2}$$

$$r_{\mu e} = 1.000(8)$$

$\tau$  decays:  $(r_{\mu e})_\tau = 1.0005(41)$  (PDG06)  
 $\pi$  decays:  $(r_{\mu e})_\pi = 1.0042(33)$

JHEP04(2008)059

KLOE average  $|V_{us}| f_+(0) = 0.2157(6)$   $\chi^2/\text{ndf}=7/4$  (13%) World Average 0.2166(5)

$$|V_{us}| = 0.2237(13)$$

$$1 - |V_{ud}|^2 - |V_{us}|^2 = 9(8) \times 10^{-4}$$

$$f_+(0) = 0.964(5)$$

PRL 100 (2008)

$$|V_{ud}| = 0.97418(26)$$

PRC 77 (2008)

# $V_{us}, V_{ud}$ and $V_{us}/V_{ud}$

$$|V_{us}/V_{ud}| = 0.2323(15) \quad \left\{ \begin{array}{l} \text{BR}(K^\pm \rightarrow \mu^\pm \nu) = 0.6366(17) \\ f_K/f_\pi = 1.189(7) \end{array} \right. \quad \begin{array}{l} \text{PLB 632 (2006)} \\ \text{PRL 100 (2008)} \end{array}$$

$$|V_{us}| = 0.2237(13) \text{ from Kl3 decays}$$

$$|V_{ud}| = 0.97418(26)$$

- Fit to  $|V_{ud}|^2$ ,  $|V_{us}|^2$  and  $|V_{us}/V_{ud}|^2$

JHEP 04 (2008)

$$|V_{ud}|^2 = 0.9490(5)$$

$$|V_{us}|^2 = 0.0506(4)$$

$$\chi^2 = 2.3/1 \text{ (13\%)}$$

- Agreement with unitarity

$$1 - |V_{ud}|^2 - |V_{us}|^2 = 4(7) \times 10^{-4} \text{ @ } 0.6\sigma$$

- Universality of lepton and quark weak coupling to W

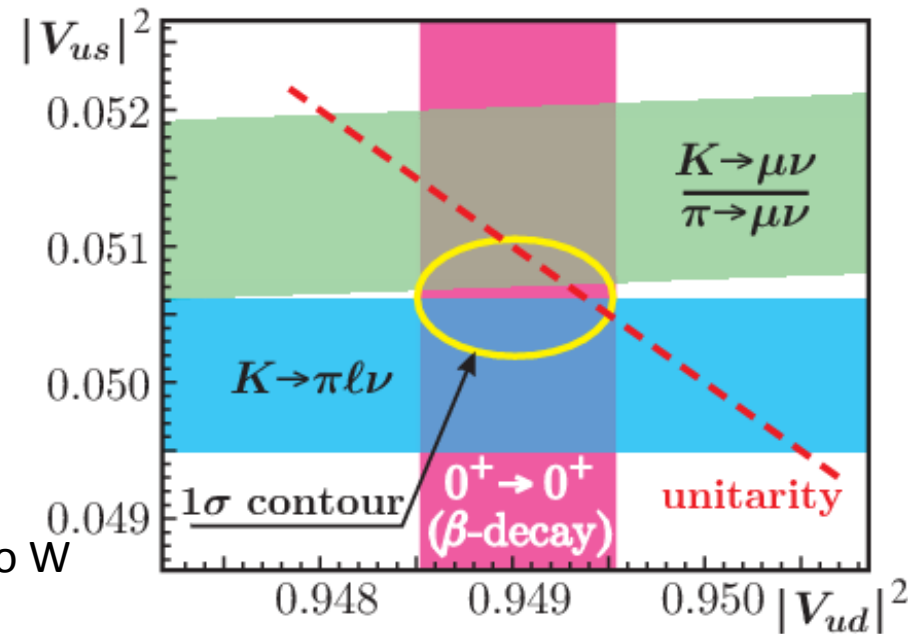
$$G_F = 1.166371(6) \times 10^{-5} \text{ GeV}^{-2}$$

$$G_{\text{CKM}} = 1.16604(40) \times 10^{-5} \text{ GeV}^{-2}$$

$$G_{\text{ew}} = 1.1655(12) \times 10^{-5} \text{ GeV}^{-2}$$

$$G_F^2 \equiv G_{\text{CKM}}^2 = (|V_{ud}|^2 + |V_{us}|^2) G_F^2$$

from ew precision tests





# Lepton Flavor Violation:

$$R_K = \Gamma(Ke2(\gamma_{IB})) / \Gamma(K\mu2(\gamma_{IB}))$$

- ❖  $R_K = \Gamma(Ke2(\gamma_{IB})) / \Gamma(K\mu2(\gamma_{IB}))$  inclusive of IB only
- ❖ DE (or SD)  $\approx$  IB presently known with 15% accuracy

To achieve  $\sim 1\%$  accuracy on  $R_K$  improve knowledge of DE

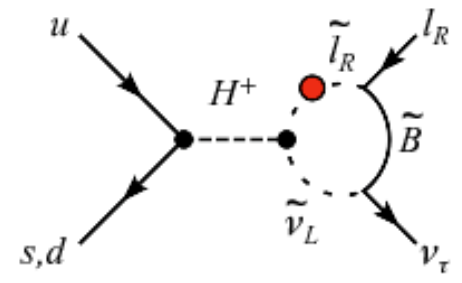
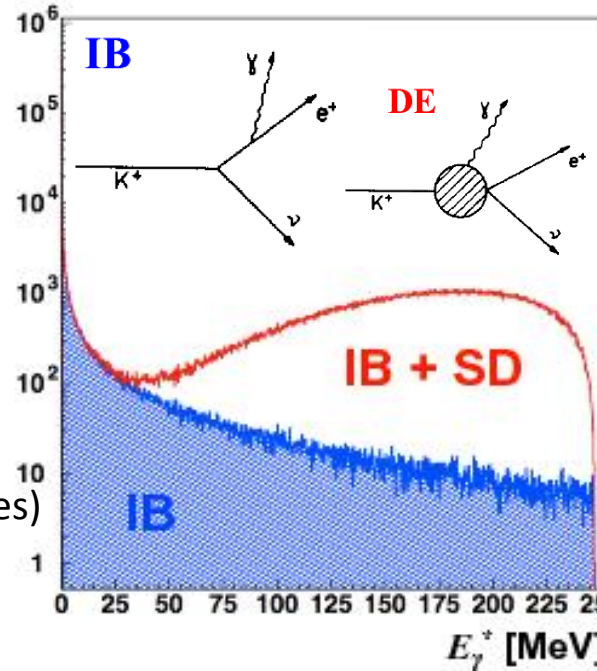
- ❖ In the SM  $R_K$  calculated at 0.04% (no hadronic uncertainties)

$$R_K^{SM} = 2.477(1) \cdot 10^{-5} \text{ [Cirigliano, Rossell JHEP10(2007)005]}$$

- ❖ Lepton Flavor Violation in the MSSM would enhance  $R_K$  up to 1%  
LFV appears at 1-loop level via an effective  $H^+ \ell \nu_\tau$  Yukawa interaction dominated by  $e \nu_\tau$

$$R_K^{LFV} \approx R_K^{SM} \left[ 1 + \left( \frac{m_K^4}{M_{H^\pm}^4} \right) \left( \frac{m_\tau^2}{m_e^2} \right) |\Delta_{13}|^2 \tan^6 \beta \right]$$

[Masiero-Paradisi-Petronzio PRD74 (2006) 011701]



# $R_K$ : analysis strategy

- Perform **Direct search** for  $K_{e2}$  and  $K_{\mu2}$ , no tag: **gain  $\times 4$  of statistics**
- Select 1-prong kinks in DC, K track from IP & secondary  $P > 180$  MeV  
Signal events with  $E_\gamma < 10$  MeV (no explicit photon detection)
- **Exploit tracking** of K and secondary: assuming  $m_\nu = 0$  get  $M^2_{lep}$  (S/B  $\sim 1/10$ )
- **Particle Identification** by Neural Network based on EMC information (training with KLe3)

**Signal count from fit in NN-  $M^2_{lep}$**

*Free parameters:*

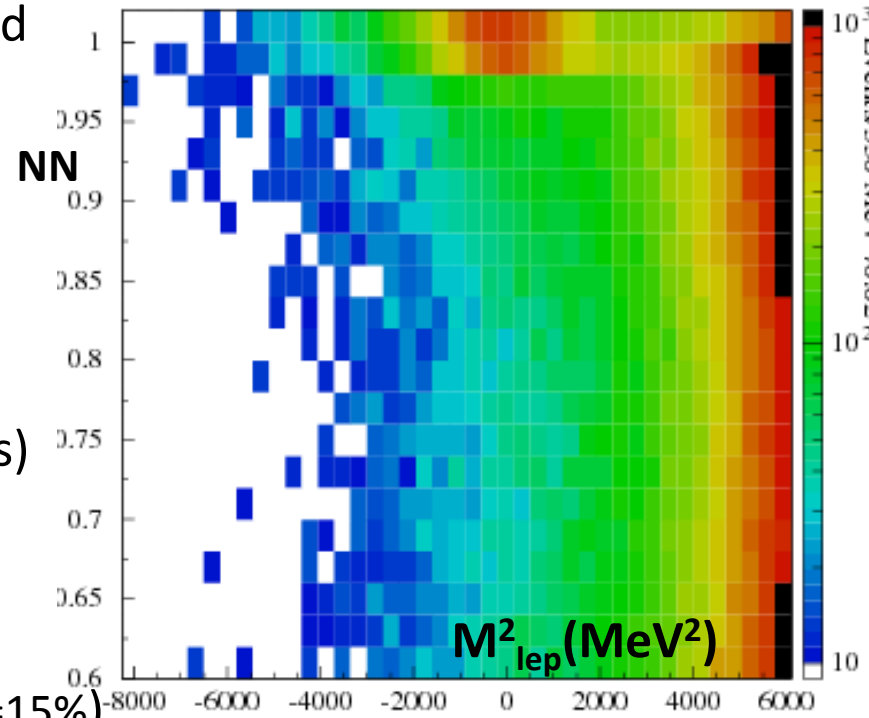
normalization factors for  $K_{\mu2}$  and  $Ke2(\gamma)$  including only IB with  $E_\gamma < 10$  MeV (to  $O(\alpha_{em})$  and resummation of leading logs)

*Fixed parameter:*

$f_{DE} = 10.2\%$  (Ke2 contamination from  $Ke2(\gamma)$  with  $E_\gamma > 10$  MeV)

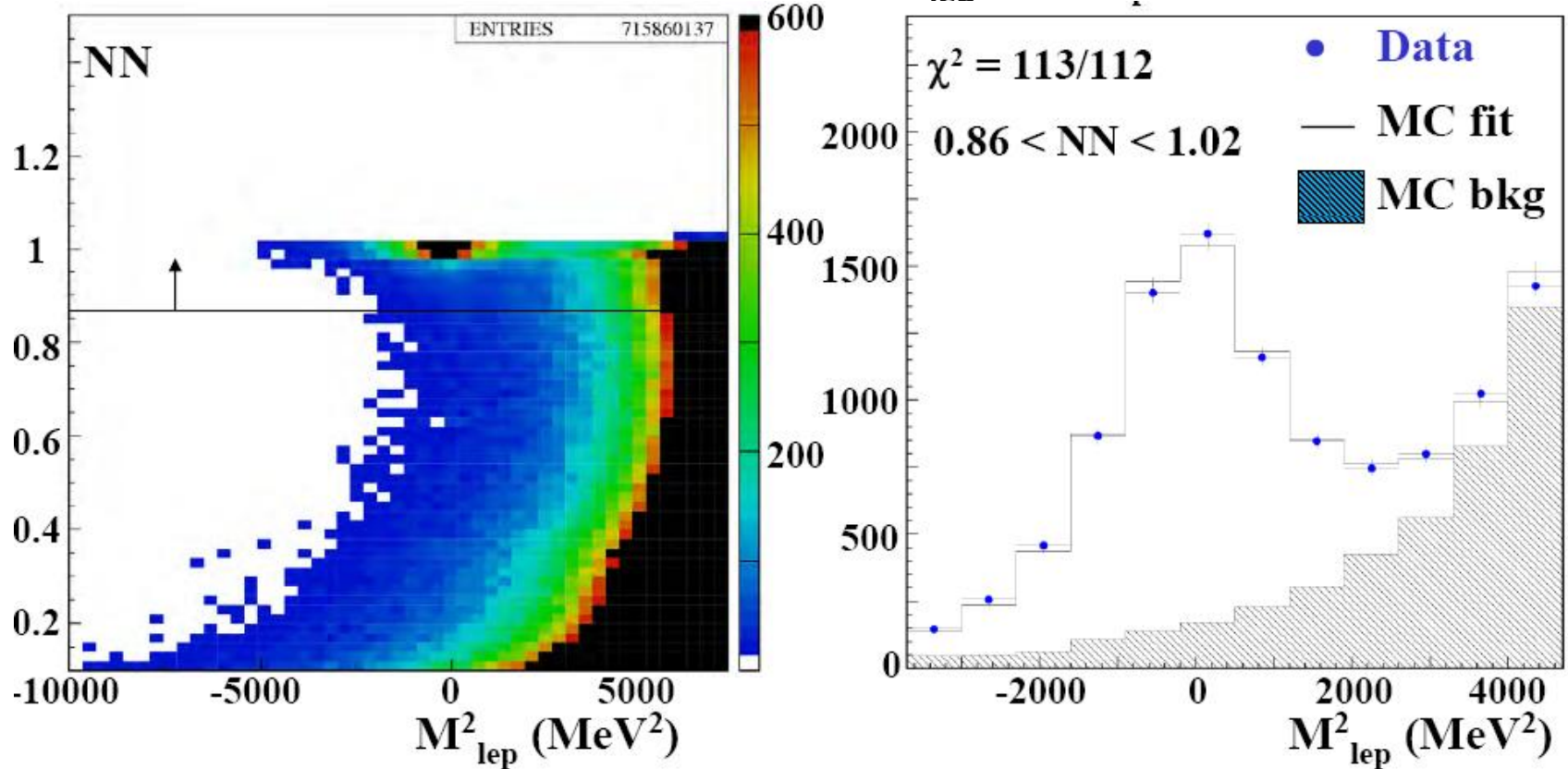
But 0.5% systematics on  $R_K$  from  $f_{DE}$  ( $\delta(DE)/DE = 15\%$ )

$\Rightarrow$  **dedicated measurement of  $Ke2(\gamma)$  with  $E_\gamma > 10$  MeV**



# $R_K$ : fitting for $K_{e2}$ and $K_{\mu2}$ counting

- Ke2 counts from two-dimensional binned likelihood fit in the NN-  $M^2_{lep}$  plane with  $0.86 < NN < 1.02$  and  $-3700 < M^2_{lep} < 6100$



Using the whole statistics:  $N_{Ke2}(e^+) = 7064(102)$  ,  $N_{Ke2}(e^-) = 6750(101)$

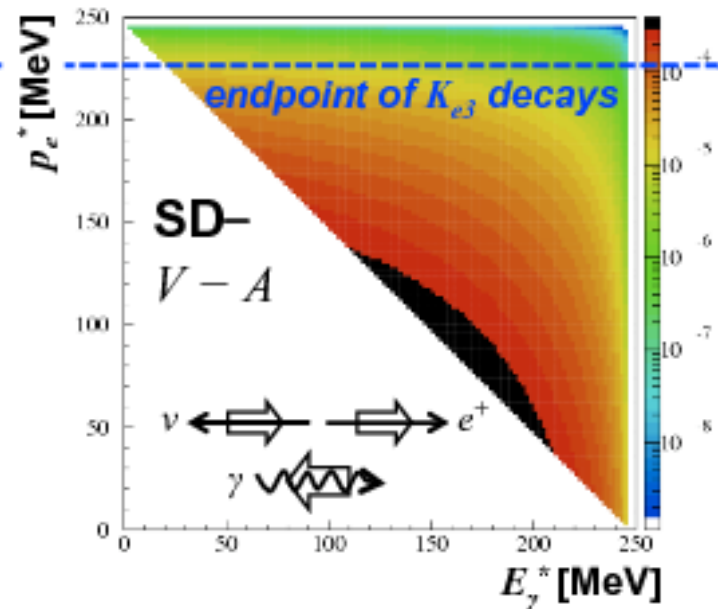
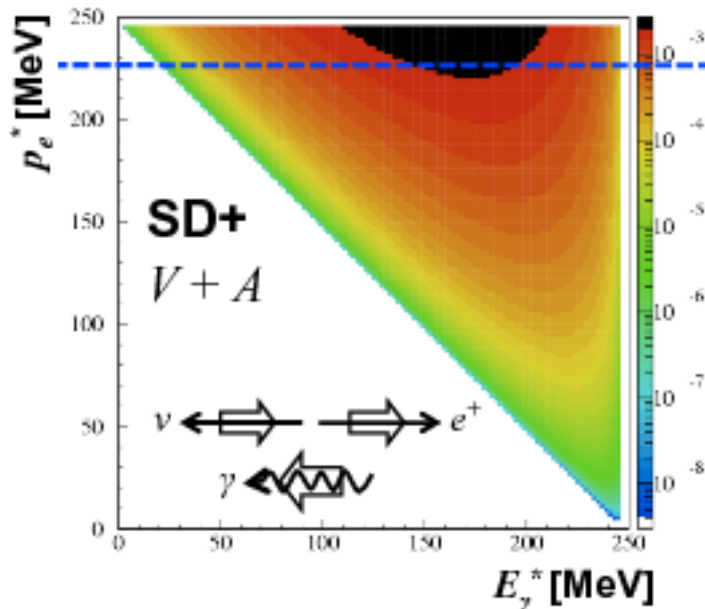
- $K_{\mu2}$  counting from 1-dimensional fit of  $M^2_{lep}$  distribution without PID

# $K_{e2\gamma}$ amplitudes

$$\frac{d\Gamma(K \rightarrow e\nu\gamma)}{dx dy} = \rho_{\text{IB}}(x, y) + \rho_{\text{SD}}(x, y) + \rho_{\text{INT}}(x, y) \quad \begin{array}{l} \text{negligible} \\ x = 2E_\gamma^*/m_K \\ y = 2E_e^*/m_K \end{array}$$

$$\rho_{\text{SD}}(x, y) = \frac{G_F^2 |V_{us}|^2 \alpha}{64\pi^2} m_K^5 \left( (V+A)^2 f_{\text{SD}+}(x, y) + (V-A)^2 f_{\text{SD}-}(x, y) \right)$$

$V, A$ : effective vector and axial couplings



# Ke2 $\gamma$ : signal selection

- 1-prong selection --  $NN > 0.98$  -- 1 photon cluster with  $E_\gamma > 20$  MeV in time with K
- Cluster times for photon and electron must be compatible

With this selection we measure Ke2 $\gamma$  with:

$$E_\gamma^* > 10 \text{ MeV}$$

$$\cos\theta_{e\gamma}^* > 0.9$$

$$p_e^* > 200 \text{ MeV}$$

No sensitivity for Ke2 $\gamma$  with  $p_e < 200$  MeV (SD-)

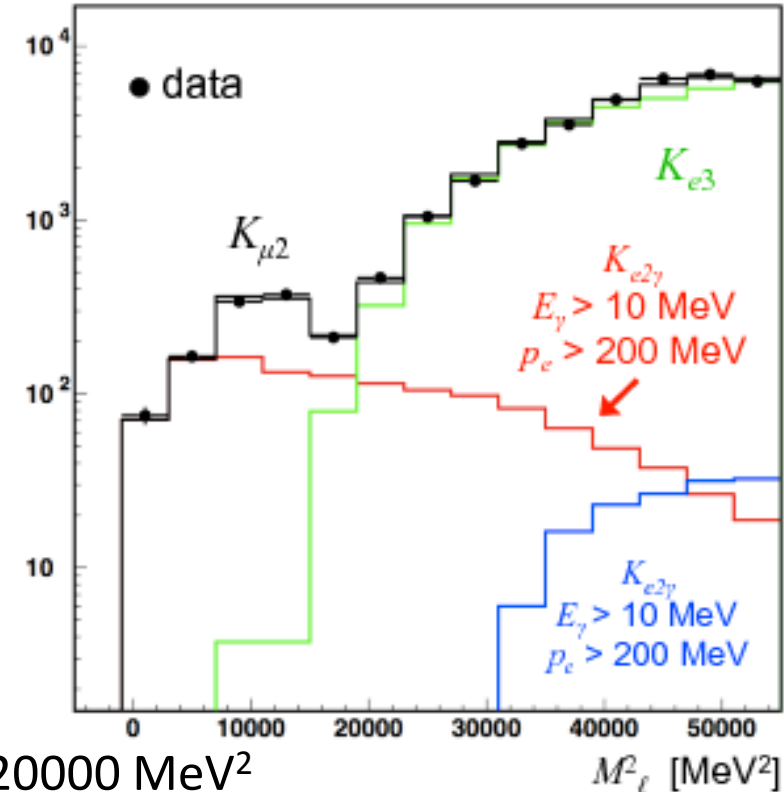
Acceptance for SD+ events  $\sim 90\%$

SD- events  $\sim 2\%$

Residual IB events  $\sim 1\%$

Dominant backgrounds:

$K\mu 2$  for  $M_{lep}^2 < 20000 \text{ MeV}^2$  and  $Ke 3$  for  $M_{lep}^2 > 20000 \text{ MeV}^2$



- Further reject Ke3 decays with  $\Delta E_\gamma = E_\gamma^{\text{LAB}} - E_\gamma^{\text{CAL}}$  ( $\sigma_E^{\text{LAB}} \approx 12 \text{ MeV}$ ,  $\sigma_E^{\text{CAL}} \approx 30 \text{ MeV}$ )
- Signal count from 2-dimensional binned likelihood fit in  $M_{lep}^2$ ,  $\Delta E_\gamma / \sigma$  in 5 bins of  $E_\gamma^*$

# $K_{e2\gamma}$ spectrum vs $O(p^4)$ ChPT

We measure

$$\frac{1}{\Gamma(K_{\mu 2(\gamma)})} \frac{d\Gamma_{SD+}(K_{e2\gamma})}{dE_\gamma}$$

where "SD+" means:

$$E_\gamma^* > 10 \text{ MeV}$$

$$\cos \theta_{e\gamma}^* < 0.9$$

$$p_e^* > 200 \text{ MeV}$$

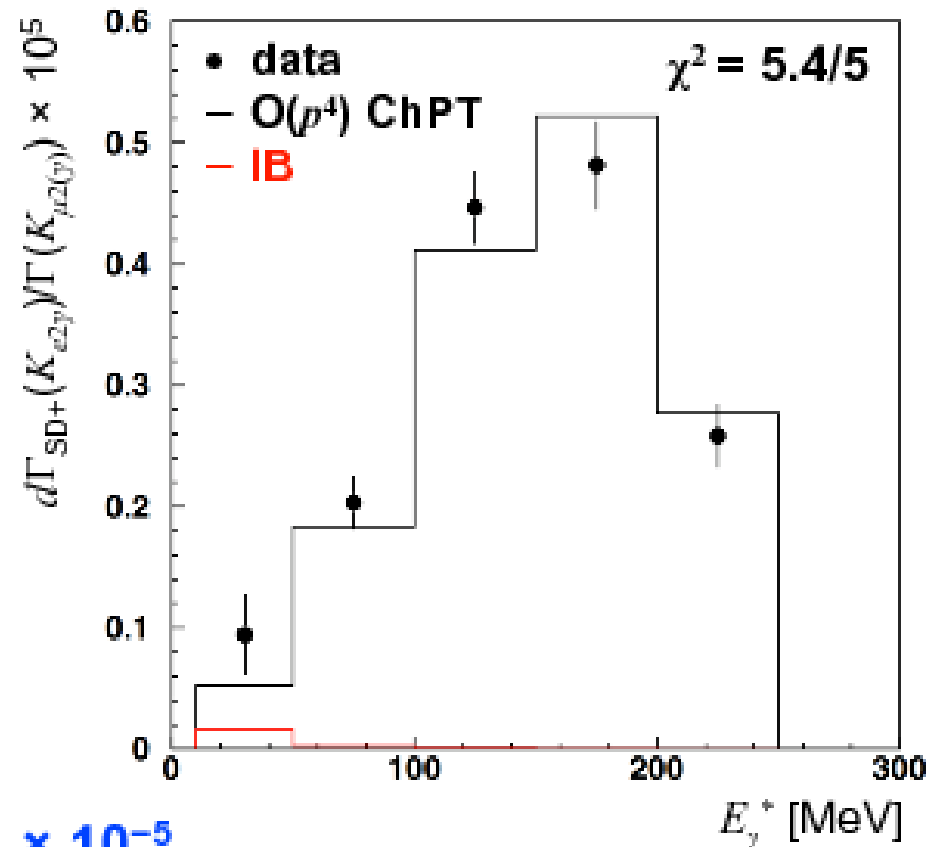
Summed over all bins in  $E_\gamma^*$ :

$$N_{SD+}(K_{e2\gamma}) = 1378 \pm 63$$

$$\frac{\Gamma_{SD+}(K_{e2\gamma})}{\Gamma(K_{\mu 2(\gamma)})} = 1.484(66)_{st}(16)_{sy} \times 10^{-5}$$

in agreement with ChPT  $O(p^4)$  prediction,  $1.447 \times 10^{-5}$  [Bijnens, Ecker, Gasser '93]

**KLOE MC implements  $O(p^4)$  ChPT for SD – used in analysis of  $R_K$**   
**Validated to within 4.6% - systematic error on  $R_K$  from SD = 0.2%**



# $R_K$ : the final result

Using the complete KLOE data set ( $2.2 \text{ fb}^{-1}$ ) we obtain: *Draft paper under collaboration's revision*

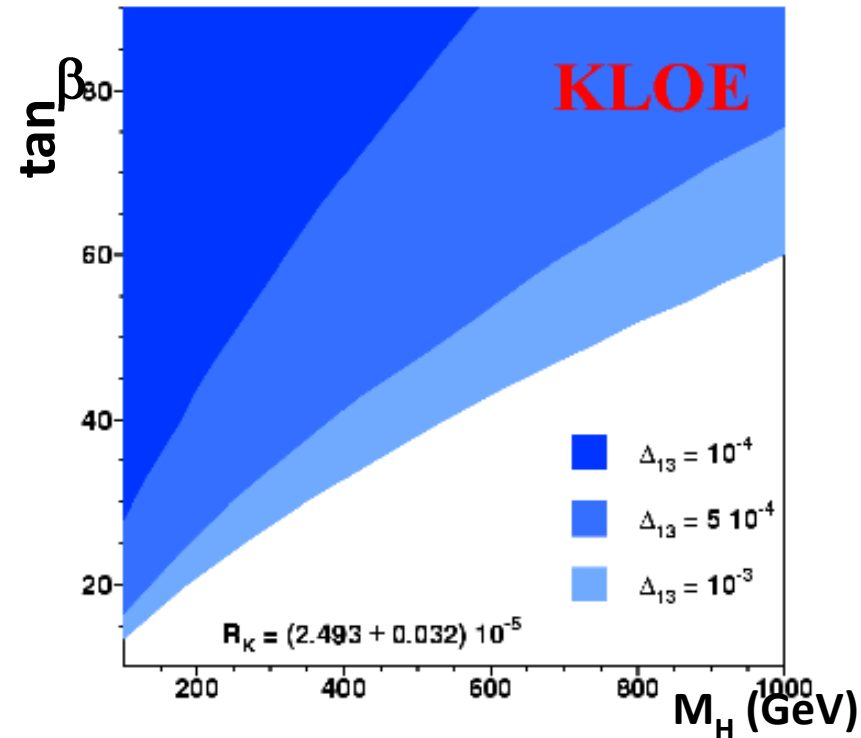
$$R_K = (2.493 \pm 0.025_{\text{stat}} \pm 0.019_{\text{syst}}) \times 10^{-5}$$

1.0%                  0.8%

$$R_K^{\text{SM}} = (2.477 \pm 0.001) \times 10^{-5}$$

Sensitivity shown as 95%-CL excluded regions in the  $\tan\beta - M_H$  plane, for fixed values of the 1-3 slepton-mass matrix element,  $\Delta_{13} = 10^{-3}, 0.5 \times 10^{-3}, 10^{-4}$

Systematic errors %	stat	syst
Reconstruction	0.4	0.4
Trigger efficiency	0.4	-
Background sub	-	0.3
Ke2(DE) comp.	0.2	-
Clustering	0.2	-
<b>Total</b>	<b>0.6</b>	<b>0.5</b>



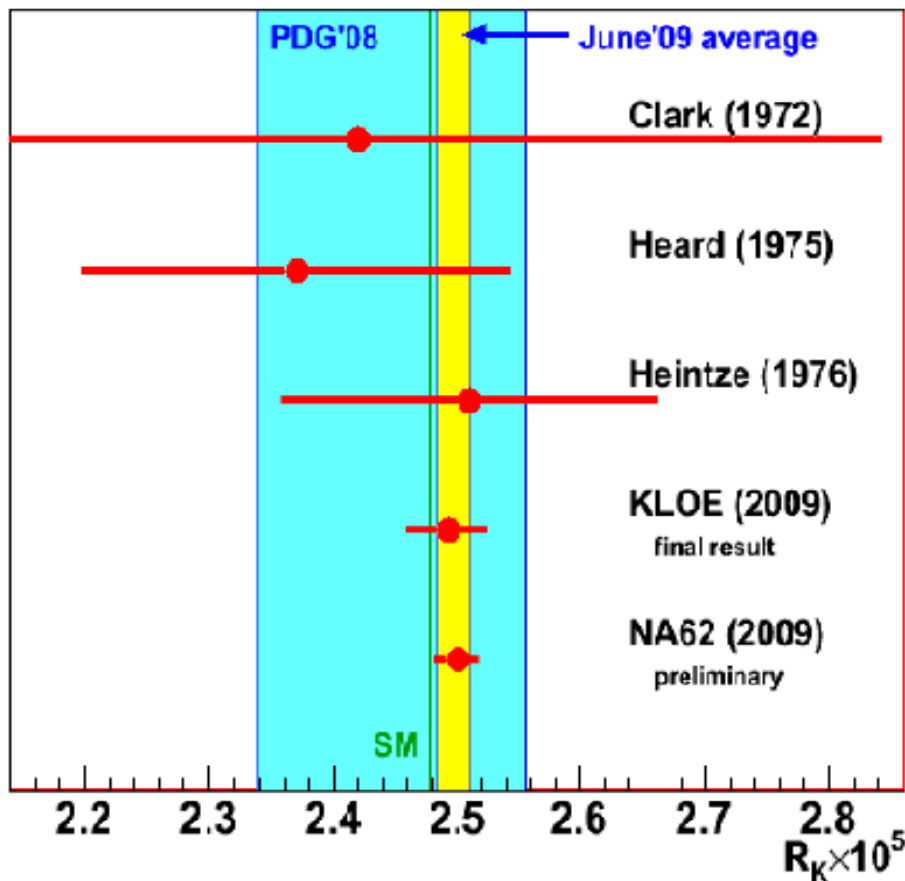
❖ Main contribution to systematic uncertainty from control-sample statistics (0.6%)

# $R_K$ : World Average

World average:  $R_K = 2.498(14) \times 10^{-5}$  (0.56%)

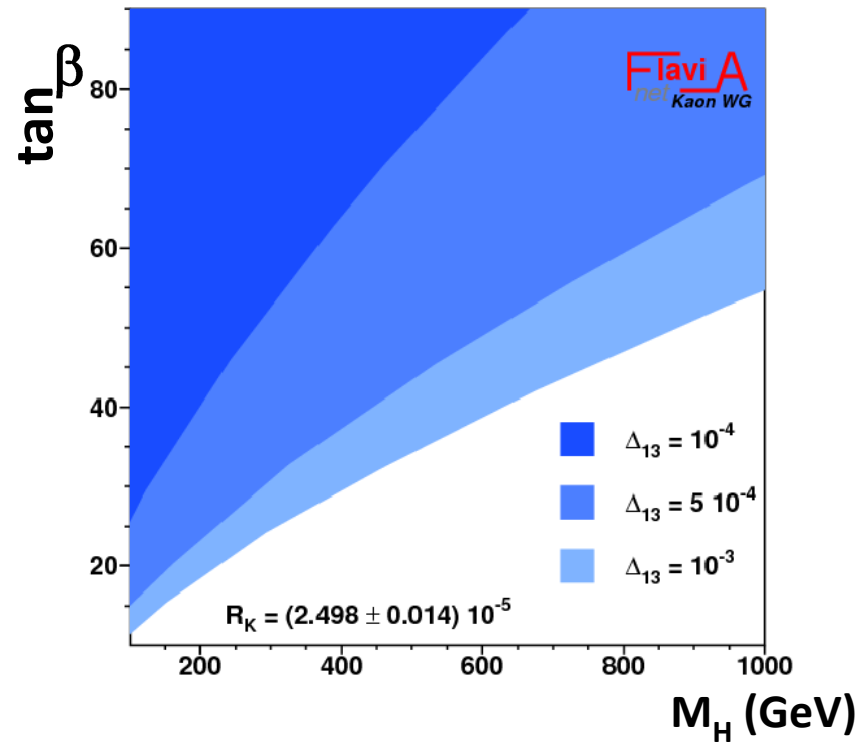
Includes NA62 preliminary (40% data set):

$R_K = 2.500(16) \times 10^{-5}$  (0.64%)



$R_K^{SM} = (2.477 \pm 0.001) \times 10^{-5}$

Sensitivity shown as 95%-CL excluded regions in the  $\tan\beta - M_H$  plane, for fixed values of the 1-3 slepton-mass matrix element,  $\Delta_{13} = 10^{-3}, 0.5 \times 10^{-3}, 10^{-4}$





# Summary & conclusions

## Precision physics with Kaon decays to test the Standard Model

- ❖ Today  $|V_{us}|f_+(0)$  @ 0.3% with KLOE (0.2% from World Average Fit)
- ❖ Lepton universality satisfied to better than 0.5%
- ❖ unitarity of CKM matrix satisfied to better than 0.1% ( $|V_{us}|$  at 0.4%)
- ❖ universality of lepton and quark weak coupling from unitarity

## and set constraints on New Physics models

- ❖ with  $Z'$  and  $H^\pm$  boson, with Lepton Flavor Violation
- ❖  $R_K$  at 1.3% from  $1.4 \times 10^4$   $Ke_2$  decays with  $2.2 \text{ fb}^{-1}$  data sample
- ❖  $\Gamma(Ke_2\gamma; 10 < E_\gamma < 250 \text{ MeV and } p_e > 200 \text{ MeV}) / \Gamma(K\mu_2)$  at 4.6%  
reduces from 0.5% to 0.2% the systematic uncertainty on  $R_K$  from DE  
which is also very important for NA62  $R_K$  measurement

SPARE SLIDES

# Outlook : universality

- ❖ Today with  $f_+(0)$  @ 0.5% the accuracy on the unitarity relation of the first row is

$$\sigma (1 - V_{ud}^2 - V_{us}^2) = 6 \times 10^{-4} \quad \left\{ \begin{array}{l} V_{us} @ 0.4\% \text{ from fit} \\ V_{ud} @ 0.026\% \end{array} \right.$$

- ❖  $f_+(0)$  @ 0.1% accuracy from lattice within few years

	$f_+(0)V_{us}$	$V_{us}$
<b>KLOE today</b> (World Average)	<b>0.28%</b> (0.23%)	<b>0.30%</b> (0.25%)
<b>KLOE + Step0 (5 fb<sup>-1</sup>) + World Average</b>	<b>0.14%</b>	<b>0.17%</b>

- ❖  $f_K / f_\pi$  @ 0.1% within few years and  $|V_{us} / V_{ud}|$  @ 0.28% from  $\Gamma(K_{\mu 2}) / \Gamma(\pi_{\mu 2})$
- ❖ With  $|V_{ud}|$  @ 0.02% and  $|V_{us}|$  @ 0.17% the accuracy on the unitarity relation of the first row would improve by a factor of  $\sim 2$

$$\sigma (1 - V_{ud}^2 - V_{us}^2) = (3 \div 4) \times 10^{-4}$$

*Improve constraints on New Physics and interplay with other sectors*