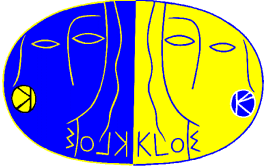


**Test of Lepton Flavor  
Universality with  $K_e2$   
decay at KLOE**

**Barbara Sciascia, *LNF INFN*  
for the *KLOE* collaboration**

**2009 Kaon International Conference  
Tsukuba, Japan – 10<sup>nd</sup> June 2009**

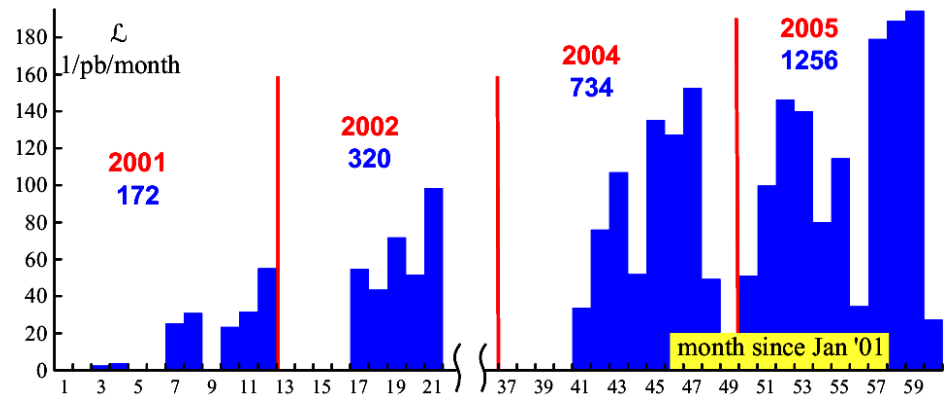


# Measurement of $R_K = \Gamma(Ke2)/\Gamma(K\mu2)$

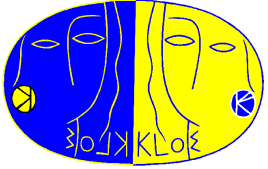
Introduction:  $R_K$  in and beyond SM.

Measurement of  $R_K = \Gamma(Ke2(\gamma))/\Gamma(K\mu2(\gamma))$  at KLOE.

- Based on  $2.2 \text{ fb}^{-1}$  of data collected at  $e^+e^-$  collider DaΦne.
- $\text{BR}(\phi \rightarrow K^+K^-) \sim 0.49$ , yielding  $3 \times 10^9$   $K^+K^-$  pairs,  $\sim 50,000$  Ke2 decays in FV



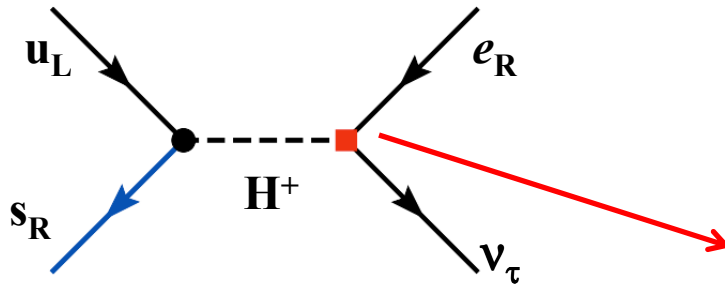
- Signal selection; analysis basic principle
- Background rejection
- Ke2 event counting; with systematics
- Reconstruction efficiencies
- Results on  $R_K$ .



# *NP potential of $R_K = \Gamma(K^\pm_{e2})/\Gamma(K^\pm_{\mu2})$*

- SM prediction with 0.04% precision, benefits of cancellation of hadronic uncertainties (no  $f_K$ ):  $R_K = 2.477(1) \times 10^{-5}$  [Cirigliano Rosell arXiv:0707:4464].

- Helicity suppression can boost NP [Masiero-Paradisi-Petronzio PRD74(2006)011701].

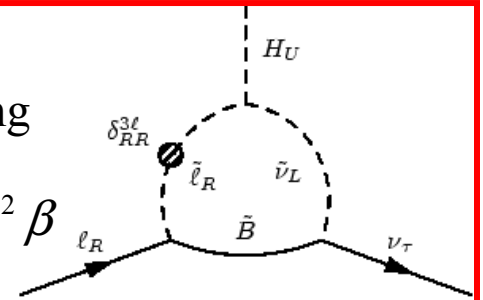


$$R_K^{LFV} = \frac{\sum_i K \rightarrow e \nu_i}{\sum_i K \rightarrow \mu \nu_i} \approx \frac{\Gamma_{SM}(K \rightarrow e \nu_e) + \Gamma(K \rightarrow e \nu_\tau)}{\Gamma_{SM}(K \rightarrow \mu \nu_\mu)}$$

$$R_K^{LFV} \approx R_K^{SM} \left( 1 + \frac{m_K^4}{m_H^4} \frac{m_\tau^2}{m_e^2} |\Delta_R^{31}|^2 \tan^6 \beta \right)$$

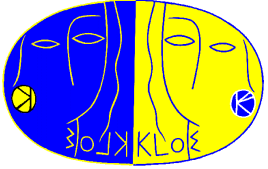
LFV from loop generates an effective  $eH^+ \nu_\tau$  coupling

$$eH^+ \nu_\tau \rightarrow \frac{g_2}{\sqrt{2}} \frac{m_\tau}{M_W} \Delta_R^{31} \tan^2 \beta$$



LFV can give **O(1%) deviation from SM** ( $\Delta_R^{31} \sim 5 \times 10^{-4}$ ,  $\tan \beta \sim 40$ ,  $m_H \sim 500$  GeV)

- Exp. accuracy on  $R_K$  (before KLOE and NA62 results) at 5% level.
- New measurements of  $R_K$  can be very interesting, **if error at 1% level or better.**



## *Entering the precision realm for $R_K$*

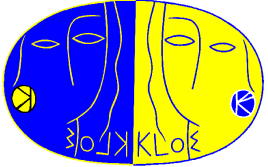
Main actors (experiments) in the challenge to push down precision on  $R_K$ :

**NA48/2**: preliminary result with 2003 data:  $R_K = 2.416(43)_{\text{stat}}(24)_{\text{syst}} 10^{-5}$ ,  
from  $\sim 4000$  Ke2 candidates (2% accuracy)

**NA48/2**: preliminary result with 2004 data:  $R_K = 2.455(45)_{\text{stat}}(41)_{\text{syst}} 10^{-5}$ ,  
from  $\sim 4000$  Ke2 candidates from special minimum bias run (3% accuracy)

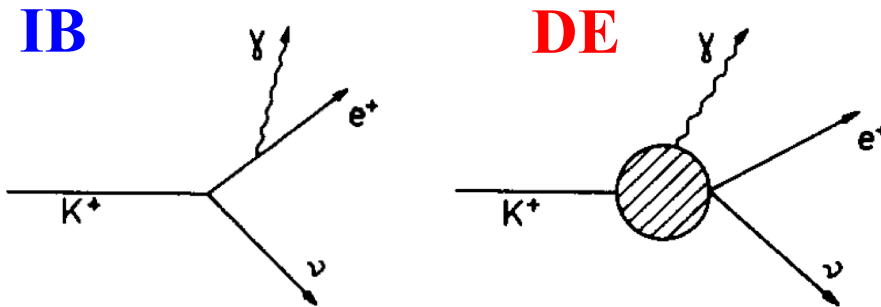
**KLOE**: preliminary result with 2001-2005 data:  $R_K = 2.55(5)_{\text{stat}}(5)_{\text{syst}} 10^{-5}$ ,  
from  $\sim 8000$  Ke2 candidates (3% accuracy), perspectives to reach 1% error  
after analysis completion.

**NA62** (ex NA48): collected  $\sim 150,000$  Ke2 events in dedicated 2007 run,  
aims to breaking the 1% precision wall, possibly reaching  $< \sim 0.5\%$

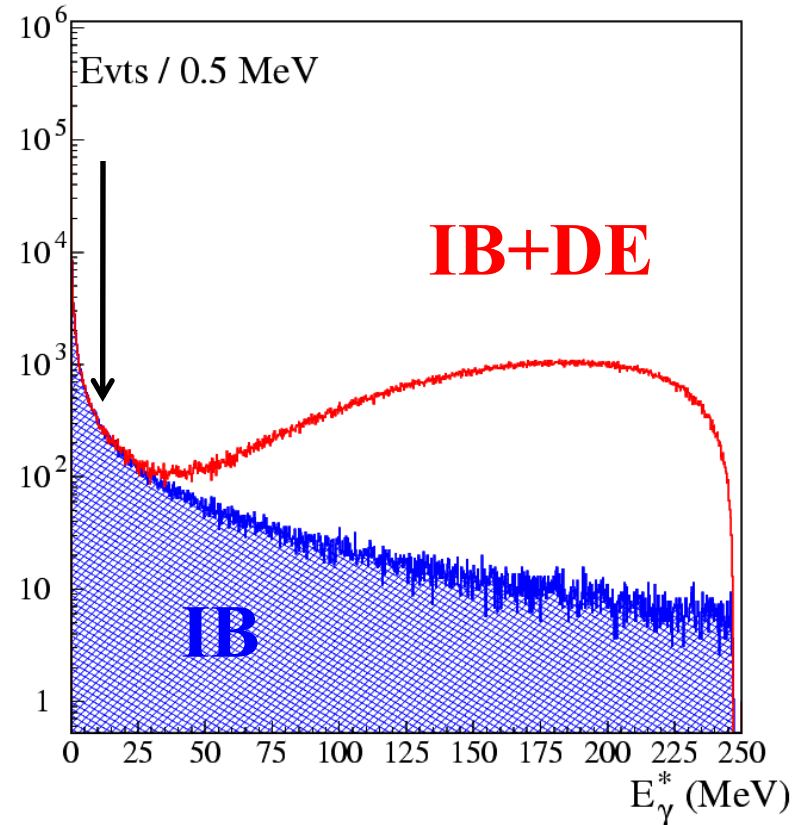


# *Ke2( $\gamma$ ): signal definition*

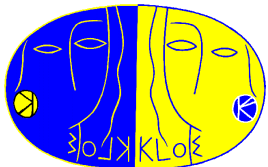
SM prediction is defined to be inclusive of **IB** (ignoring **DE** contributions).



From theory (ChPT) expect **DE**  $\sim$  **IB** for Ke2, but experimental knowledge is poor:  **$\delta\text{DE}/\text{DE} \sim 15\%$**



- Define as “signal” events with  $E_\gamma < 10$  MeV.
- Evaluating **IB** spectrum ( $O(\alpha)$ +resummation of leading logs) obtain a 0.0625(5) correction for the IB tail.
- Under 10 MeV, the **DE** contribution is expected to be negligible.



# Charged kaon at KLOE

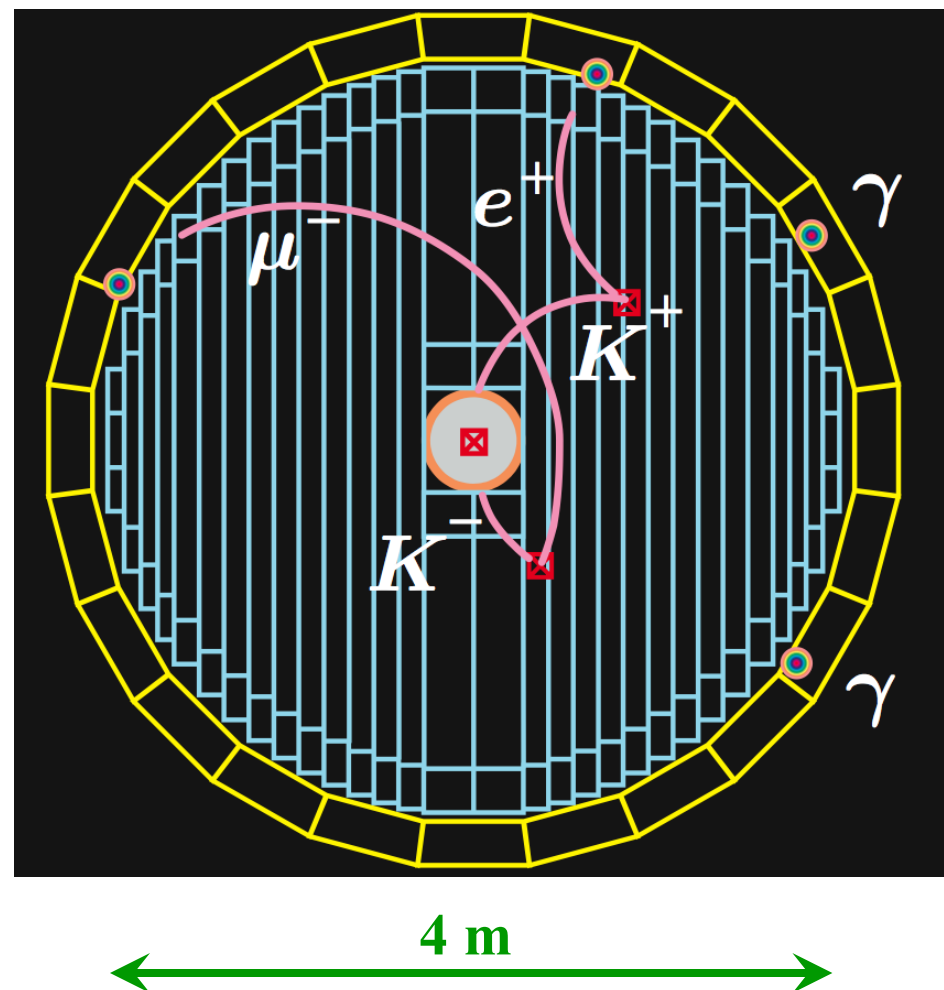
$\phi$  decay at rest provides pure kaon beams of known momentum  
 $p_K \sim 100$  MeV  
 $\lambda \sim 90$  cm (56% of  $K^\pm$  decay in DC).

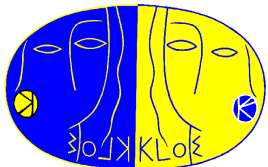
Kaon momentum measured (event by event) with 1 MeV resolution in DC.

Constraints from  $\phi$  2-body decay.

Particle ID with kinematics and ToF.

Tagging provides unbiased control samples for efficiency measurement.





# Analysis basic principles

$$R_K = \frac{N_{Ke2}}{N_{K\mu2}} \left[ \frac{\epsilon_{K\mu2}^{\text{REC}}}{\epsilon_{Ke2}^{\text{REC}}} C^{\text{TRG}} C^{\text{REC}} \right] \frac{1}{\epsilon^{\text{IB}}}$$

1) Select kinks in DC (~ fiducial volume)

- K track from IP

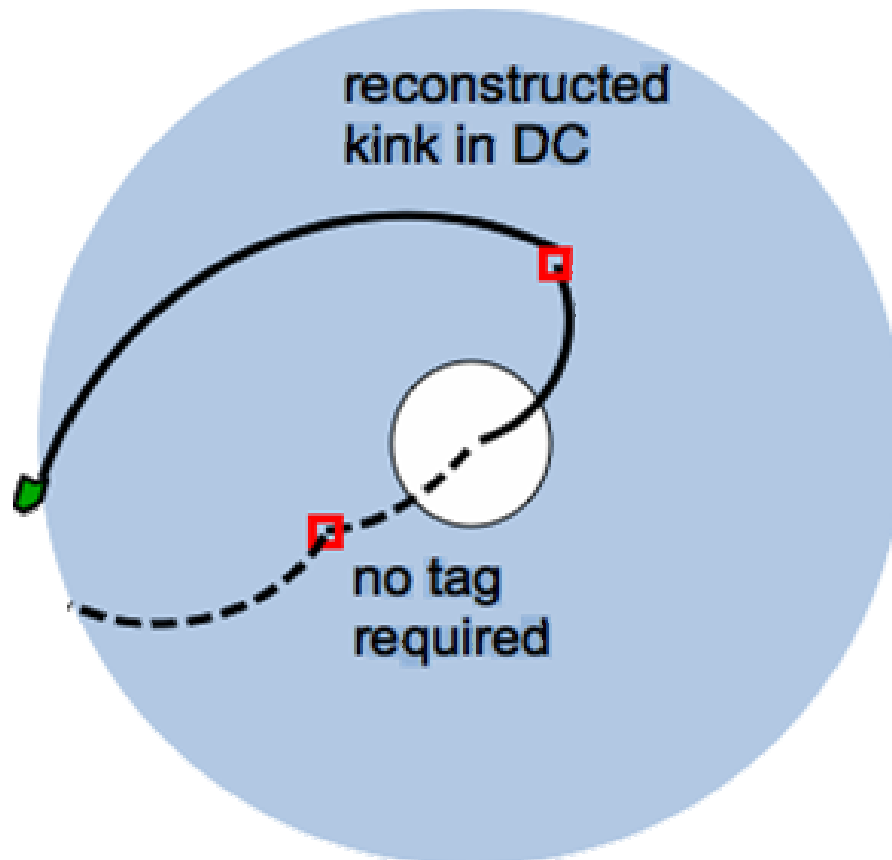
- secondary with  $p_{\text{lep}} > 180 \text{ MeV}$

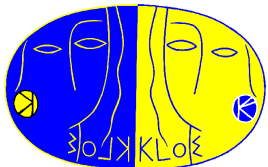
for decays occurring in the FV;

the reconstruction efficiency is ~51%.

2) No tag required on the opposite  
“hemisphere” (as we usually do!)

→ gain **×4 of statistics**



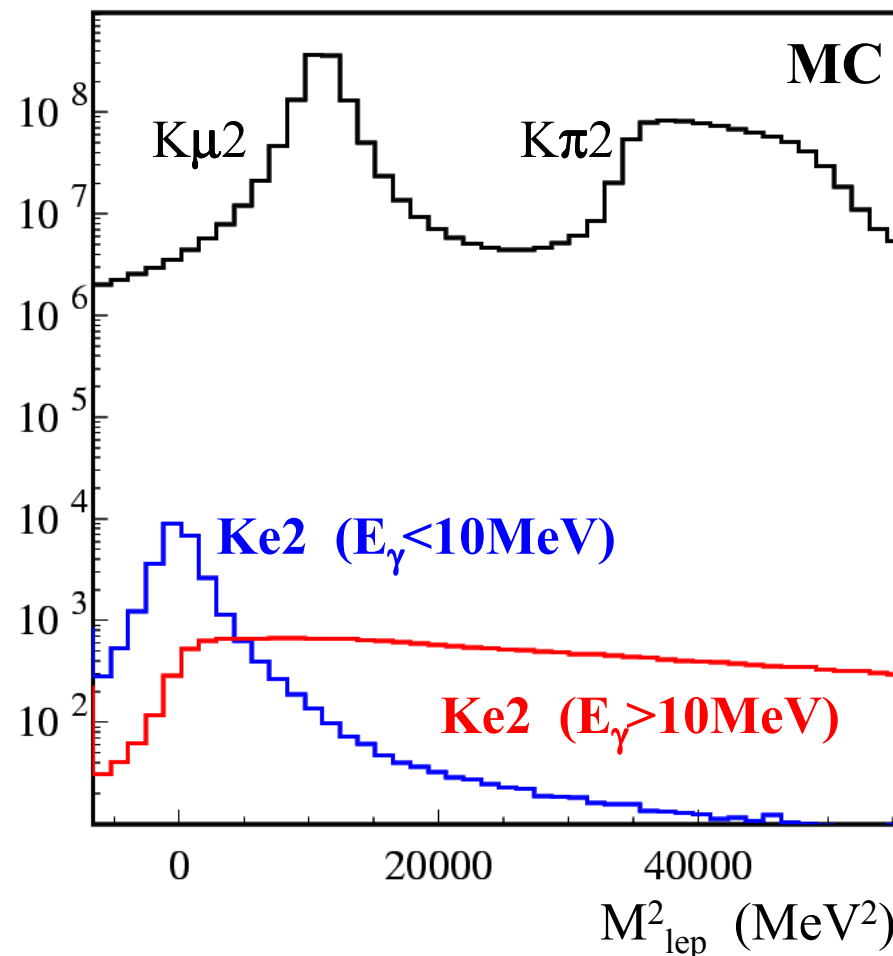


# Analysis basic principles

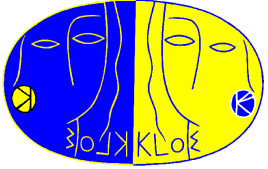
3) Exploit tracking of K and secondary: assuming  $m_\nu=0$  get  $M^2_{lep}$ :

$$M^2_{lep} = (E_K - p_{miss})^2 - p_{lep}^2.$$

Around  $M^2_{lep}=0$  we get  $S/B \sim 10^{-3}$ , mainly due to tails on the momentum resolution of  $K\mu 2$  events.

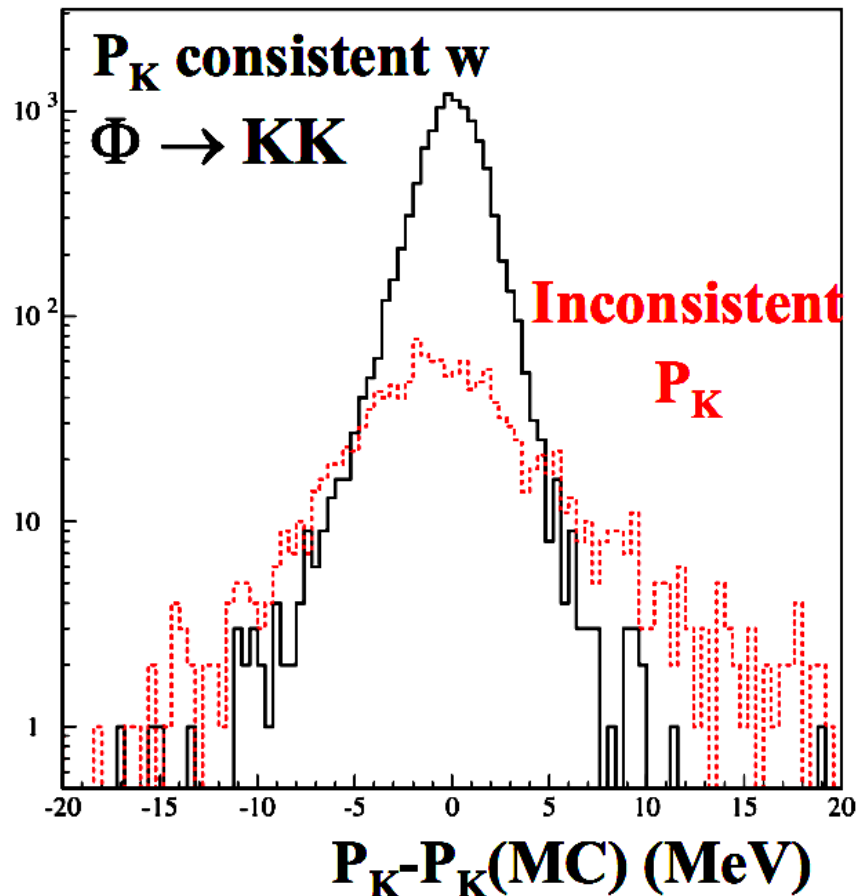




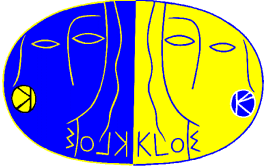


# Background rejection (track quality)

Background composition:  $K_{\mu 2}$  events with bad  $p_K$ ,  $p_{lep}$ , or decay vertex position reconstruction

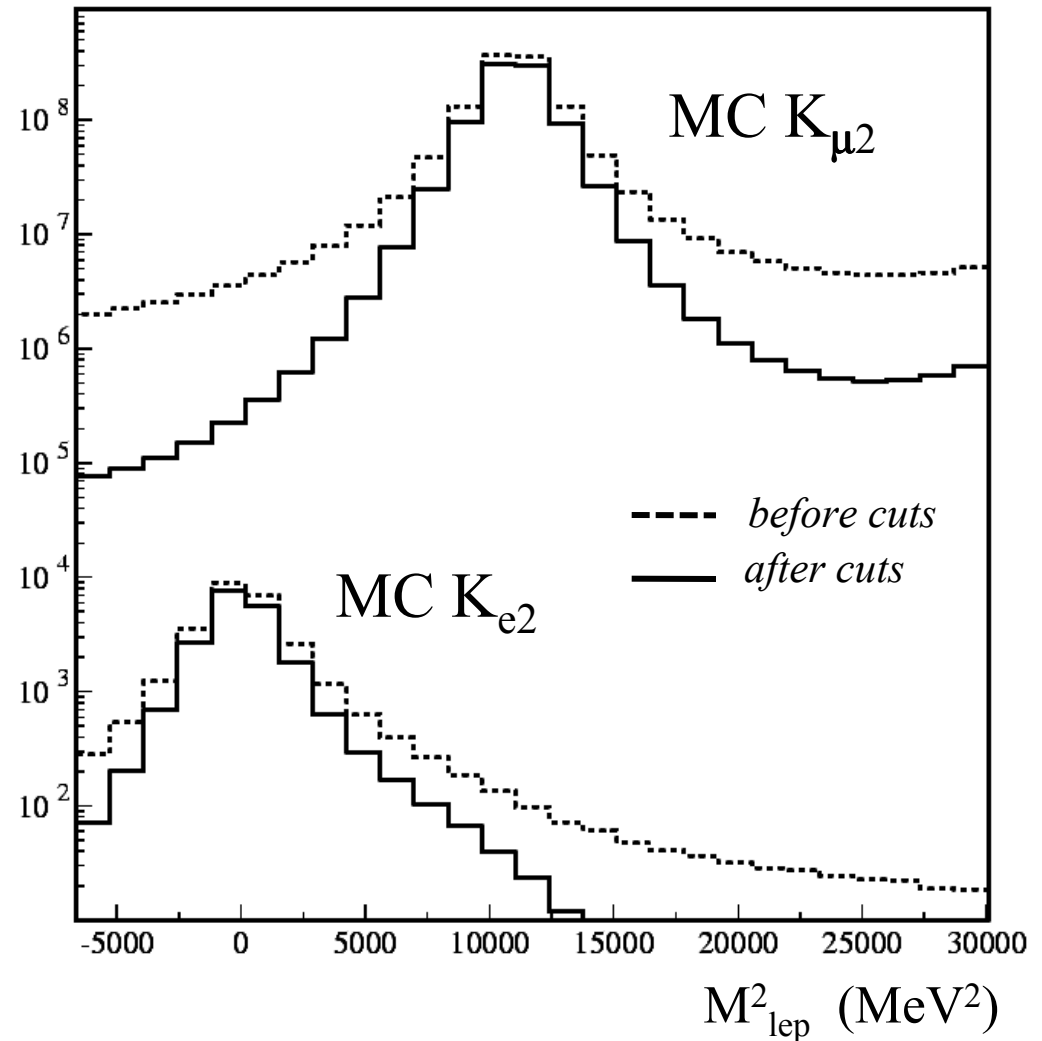


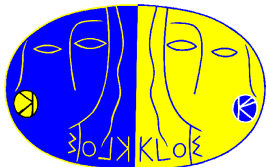
- require good quality vertex and secondary track ( $\chi^2$  cut);
- reduce  $K_{\mu 2}$  tails cutting on the error on  $M_{lep}^2$  expected from track parameters;
- quality cuts for K: the kinematic of  $\phi \rightarrow K^+K^-$  2-body decay allows redundant  $p_K$  determination.



# Background rejection (track quality)

- after cuts, we accept ~35% of decays in the FV
- most of Ke2 events lost have bad resolution
- **S/B ~ 1/20**, not enough!
- require the lepton track to be extrapolatable to the calorimeter surface and to be associated to an energy release (cluster).





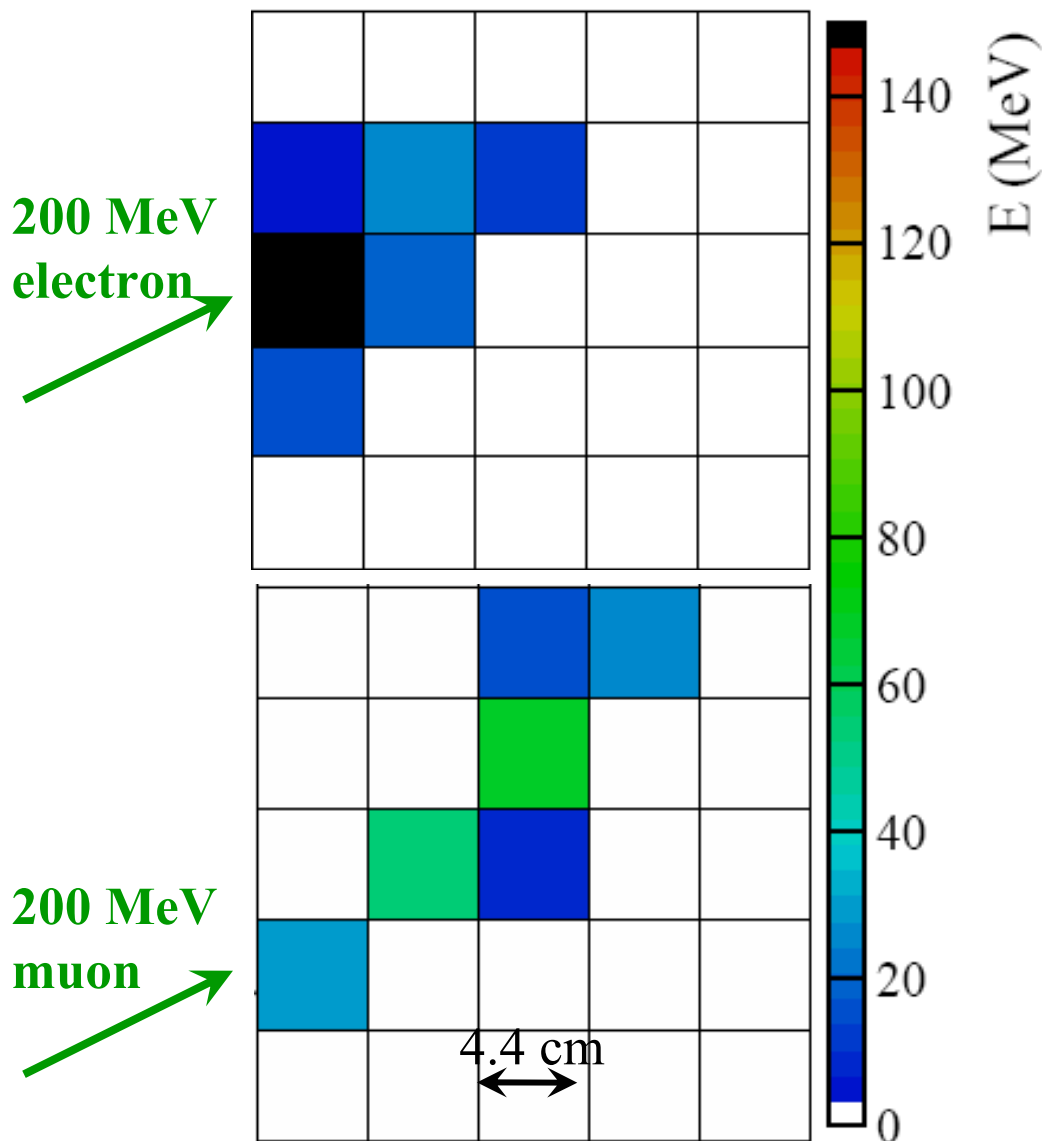
# Background rejection (PID)

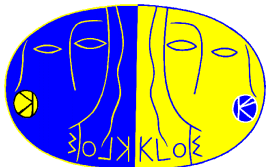
1) Particle ID exploits EMC granularity (energy deposits into 5 layers in depth):

the energy distribution and the position along the shower axis of all cells associated to the cluster allow for  $e/\mu$  PID (define 11 descriptive variables).

2) Add  $E/p$  and ToF.

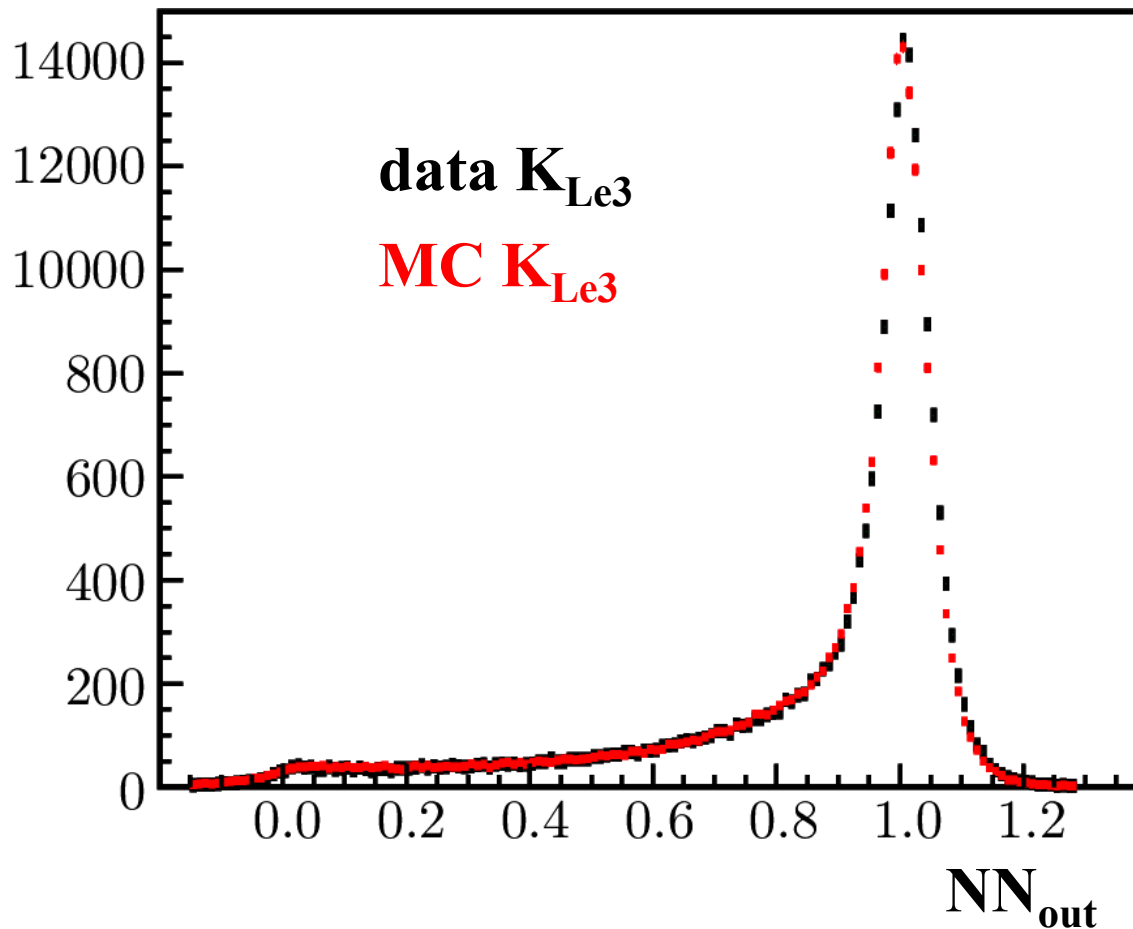
3) Combine all information in a neural network (NN).

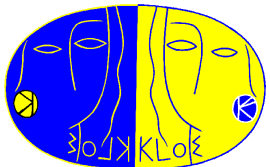




## Background rejection (PID)

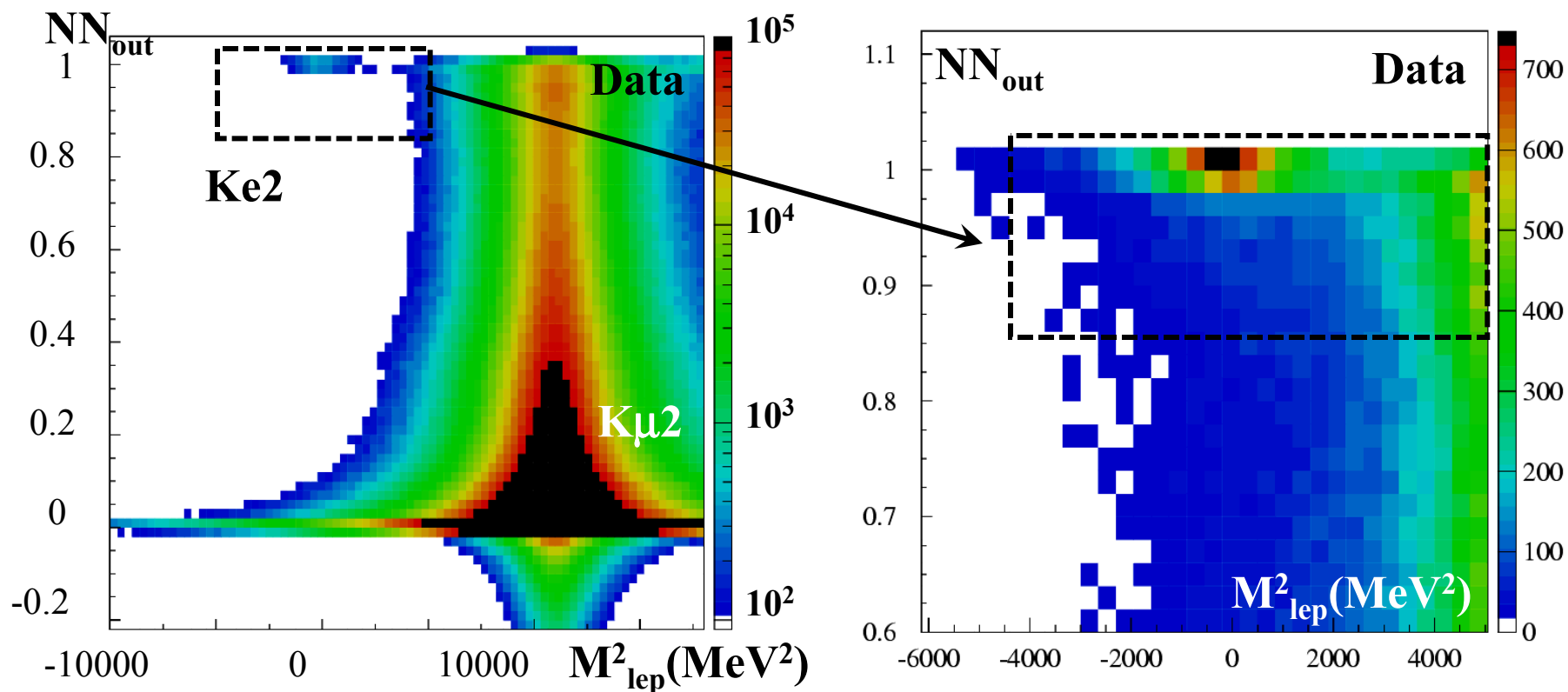
- Use a pure sample of  $K_L e3$  to correct cell response in MC.
- $K_L e3$  and  $K \mu 2$  for NN training.



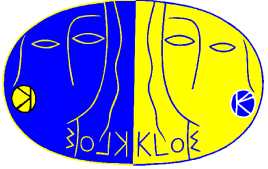


# Background rejection (PID)

Select a region with good S/B ratio in the  $M_{\text{lep}}^2 - NN_{\text{out}}$  plane



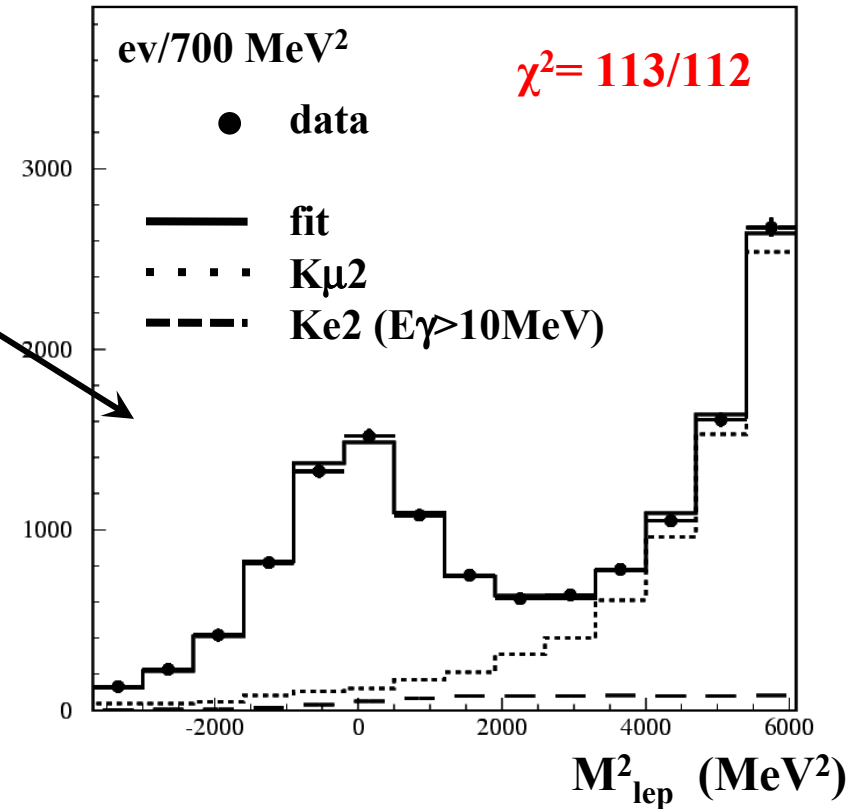
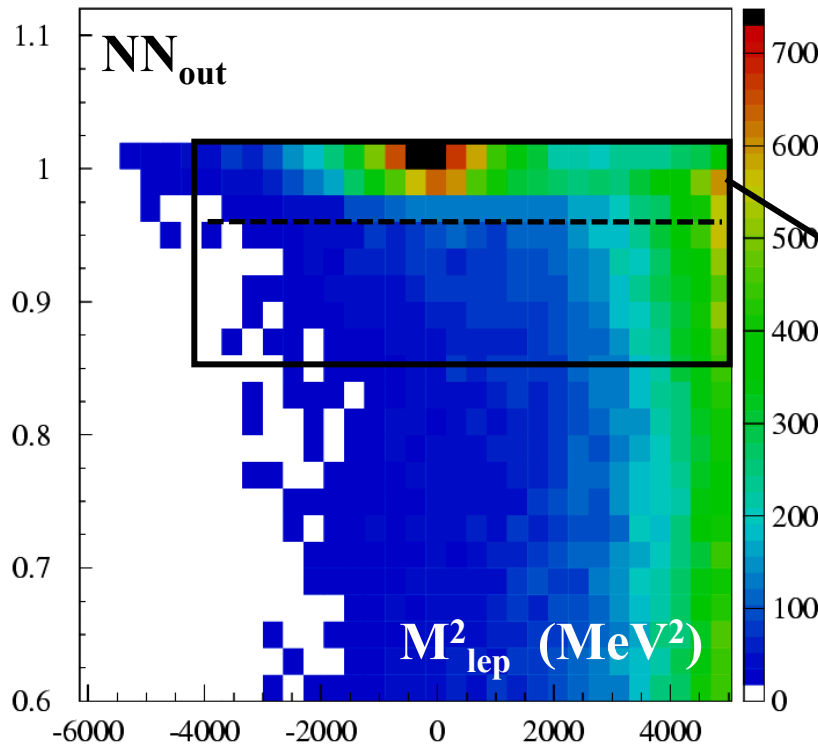
after selection:  $\epsilon \sim 30\%$  ( $\sim 15,000 K_{e2}$ )  $S/B \sim 5$



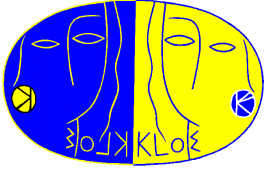
# $K_{e2}$ event counting

Two-dimensional binned likelihood fit in the  $M_{\text{lep}}^2 - NN_{\text{out}}$  plane  
 in the region  $-4000 < M_{\text{lep}}^2 < 6100$  and  $0.86 < NN_{\text{out}} < 1.02$

Ke2+ fit;  $M_{\text{lep}}^2$  proj for  $NN_{\text{out}} > 0.96$



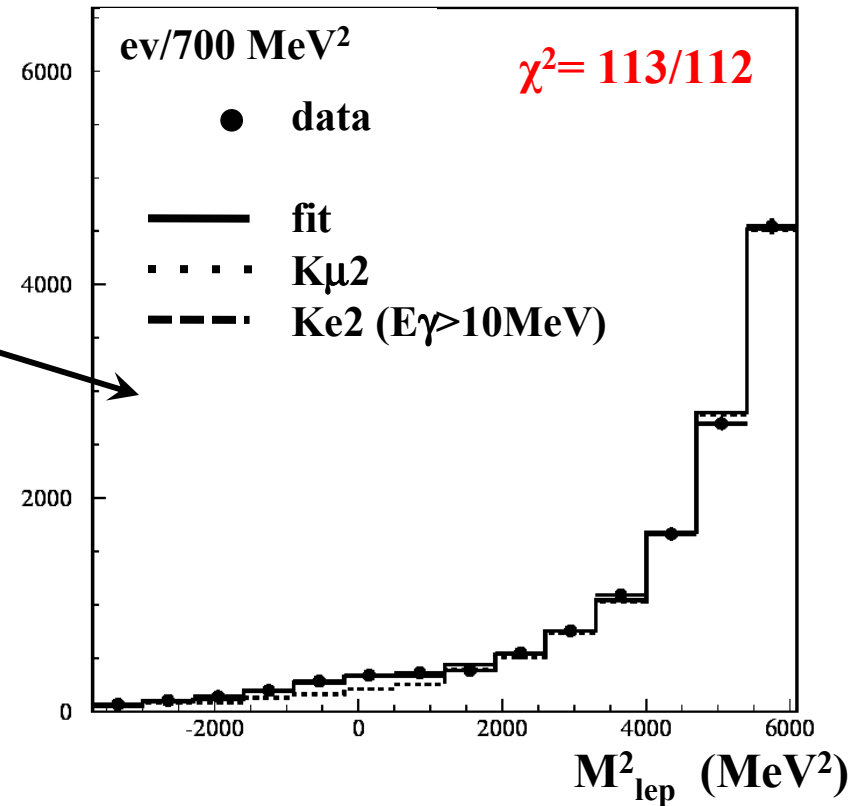
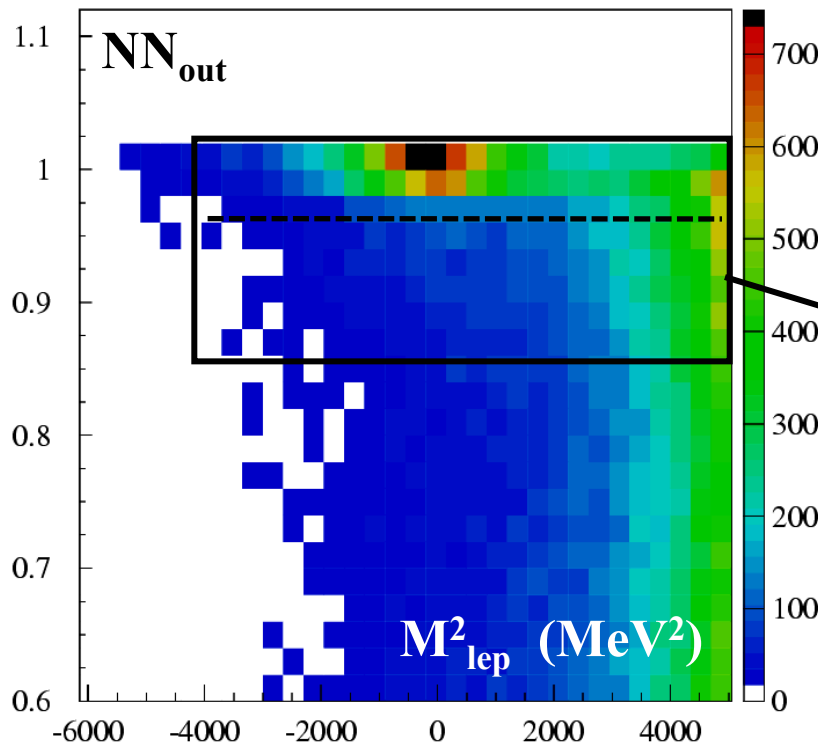
We count **7060 (102) Ke2+** **6750 (101) Ke2-** ( $\sigma_{\text{STAT}} = 1\%$ ,  $0.85\%$  from Ke2)



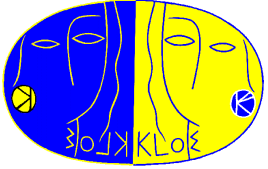
# $K_{e2}$ event counting

Two-dimensional binned likelihood fit in the  $M_{\text{lep}}^2 - NN_{\text{out}}$  plane  
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Ke2+ fit;  $M_{\text{lep}}^2$  proj for  $NN_{\text{out}} < 0.96$

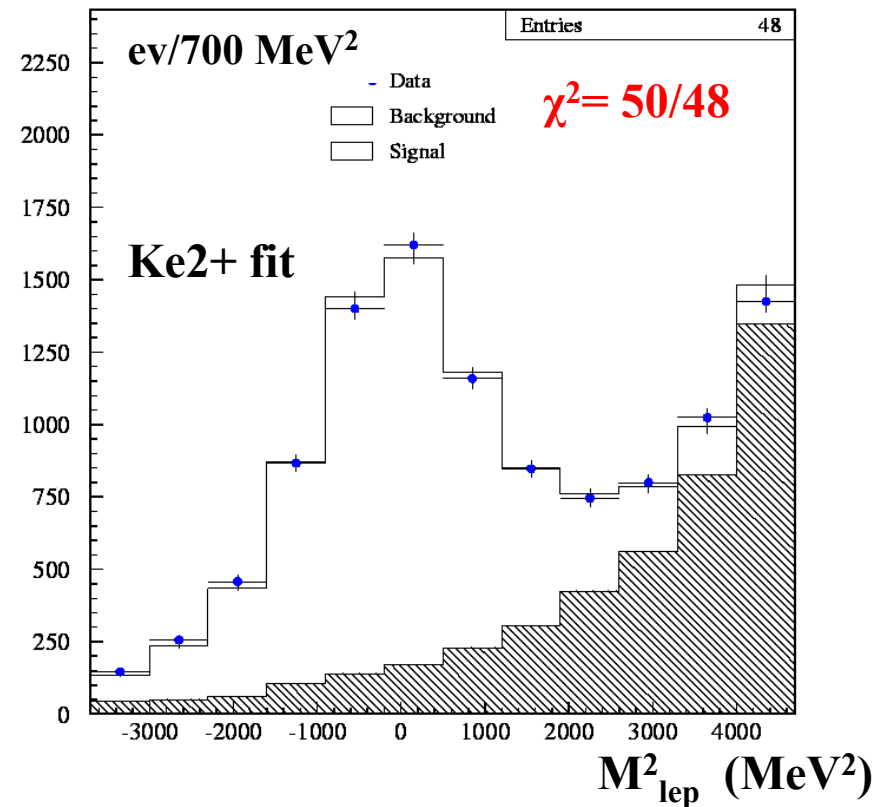
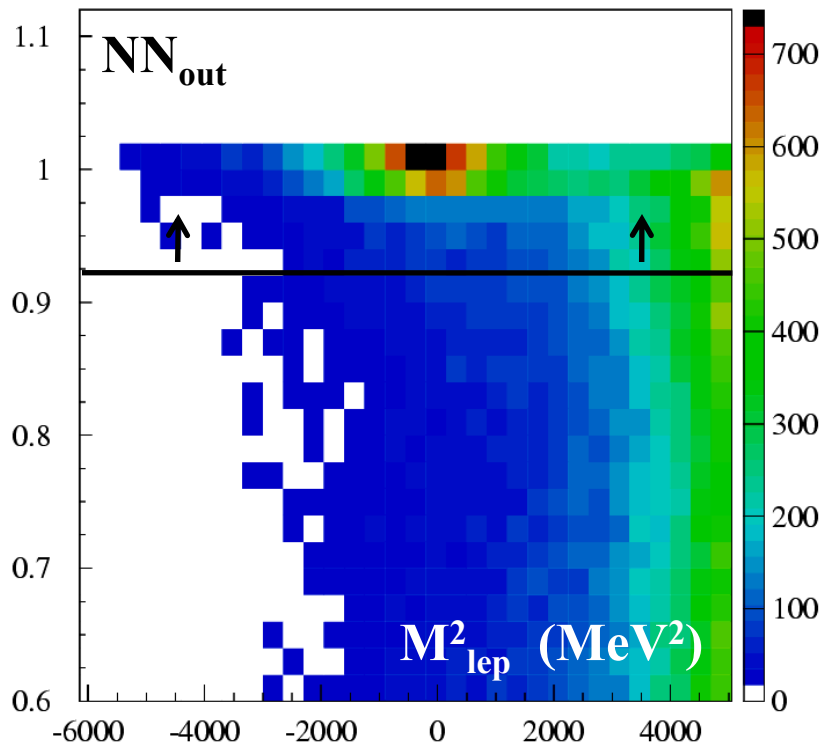


We count **7060 (102) Ke2+** **6750 (101) Ke2-** ( $\sigma_{\text{STAT}} = 1\%$ ,  $0.85\%$  from Ke2)



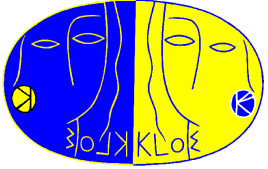
# $K_{e2}$ event counting: systematics

Repeat fit with different values of  $\max(M_{\text{lep}}^2)$  and  $\min(NN_{\text{out}})$ :  
vary significantly ( $\times 20$ ) bkg contamination + lever arm.



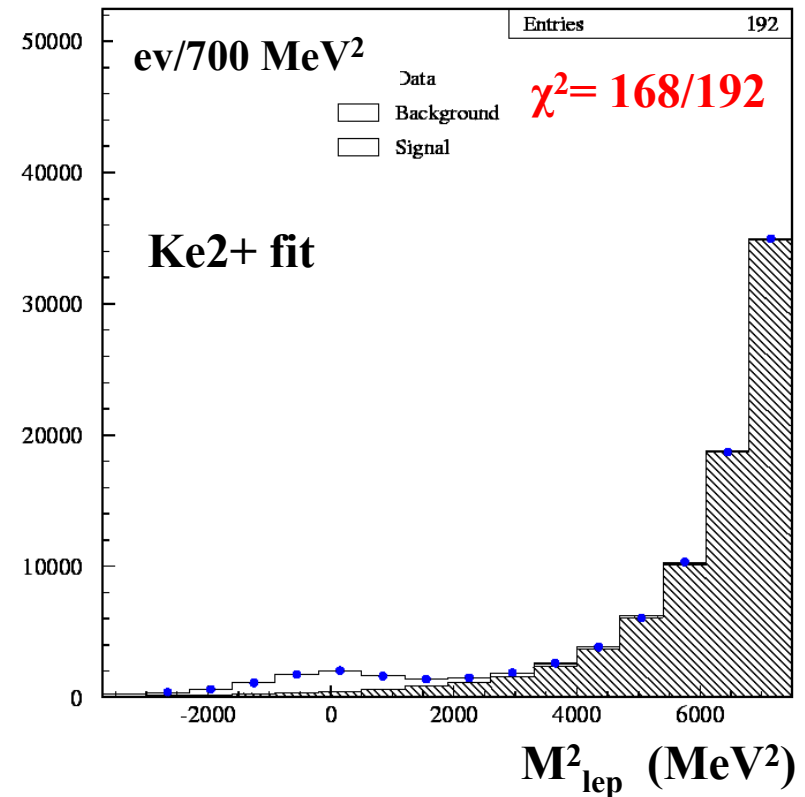
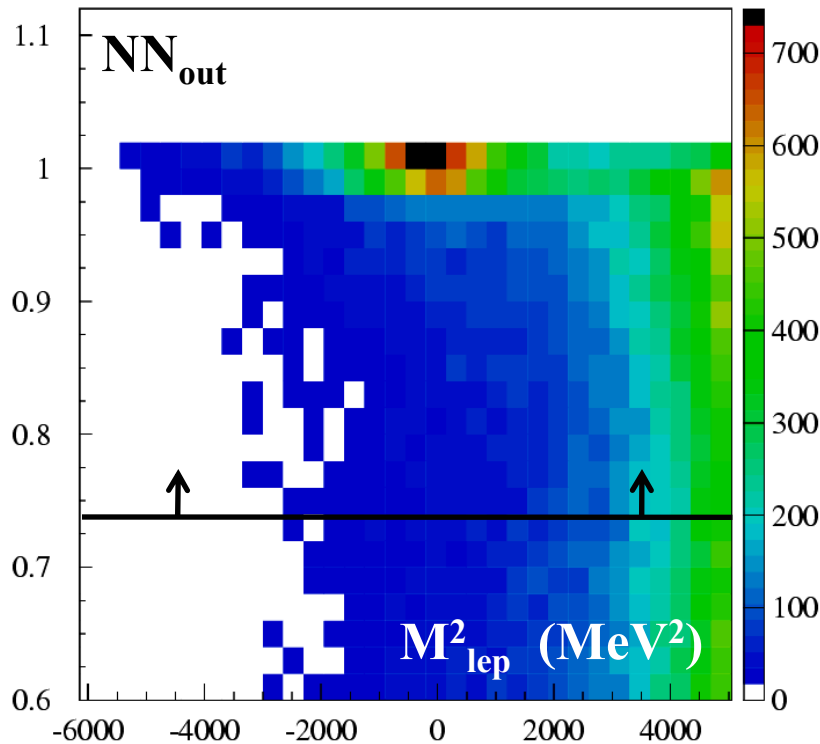
minimal bkg with:  $-4000 < M_{\text{lep}}^2 < 4650$  and  $0.94 < NN_{\text{out}} < 1.02$



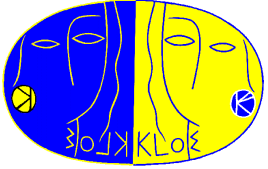


# $K_{e2}$ event counting: systematics

Repeat fit with different values of  $\max(M_{\text{lep}}^2)$  and  $\min(NN_{\text{out}})$ :  
vary significantly ( $\times 20$ ) bkg contamination + lever arm.



maximum bkg with:  $-4000 < M_{\text{lep}}^2 < 7500$  and  $0.78 < NN_{\text{out}} < 1.02$



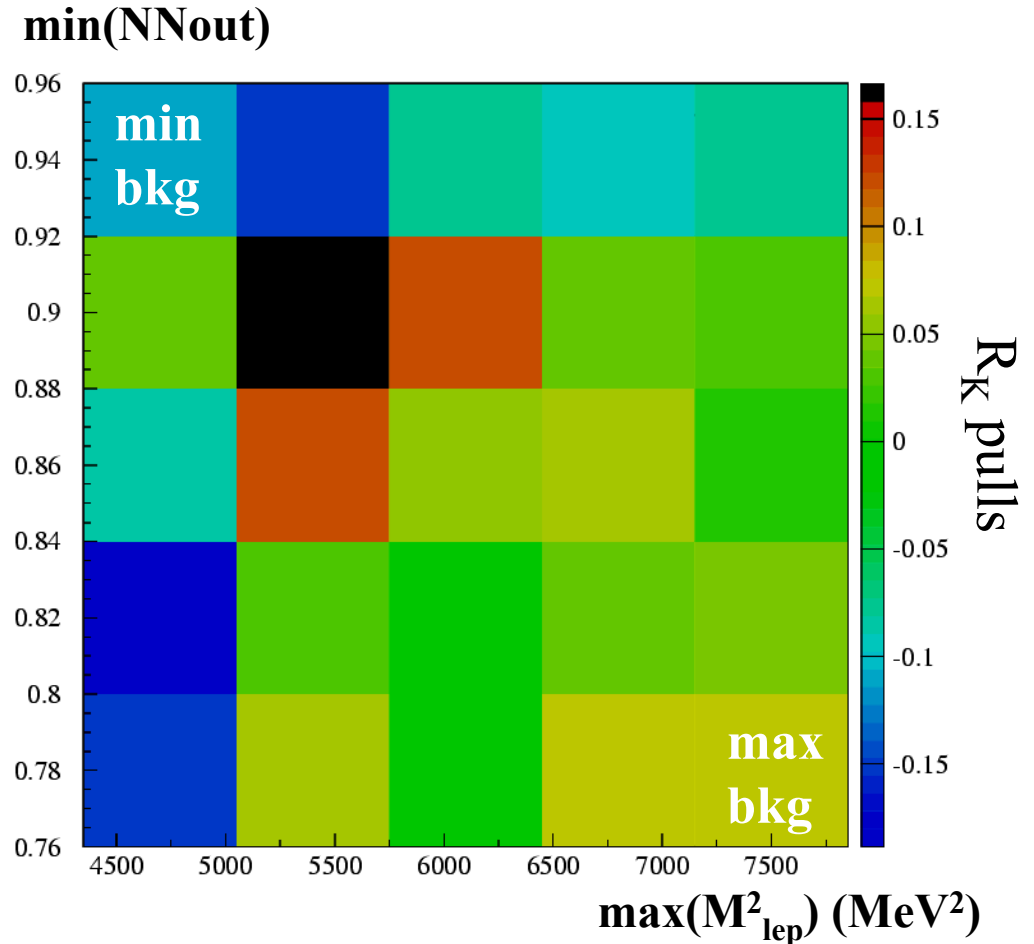
# $K_{e2}$ event counting: systematics

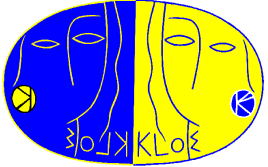
We change by a factor of 20 the amount of bkg falling in the fit region by moving

- min(NNout)
- max( $M^2_{lep}$ ).

Signal counts change by 15%.

From the pulls of the  $R_K$  measurements **we evaluated a 0.3% systematic error.**





# Ke2 fit: radiative corrections

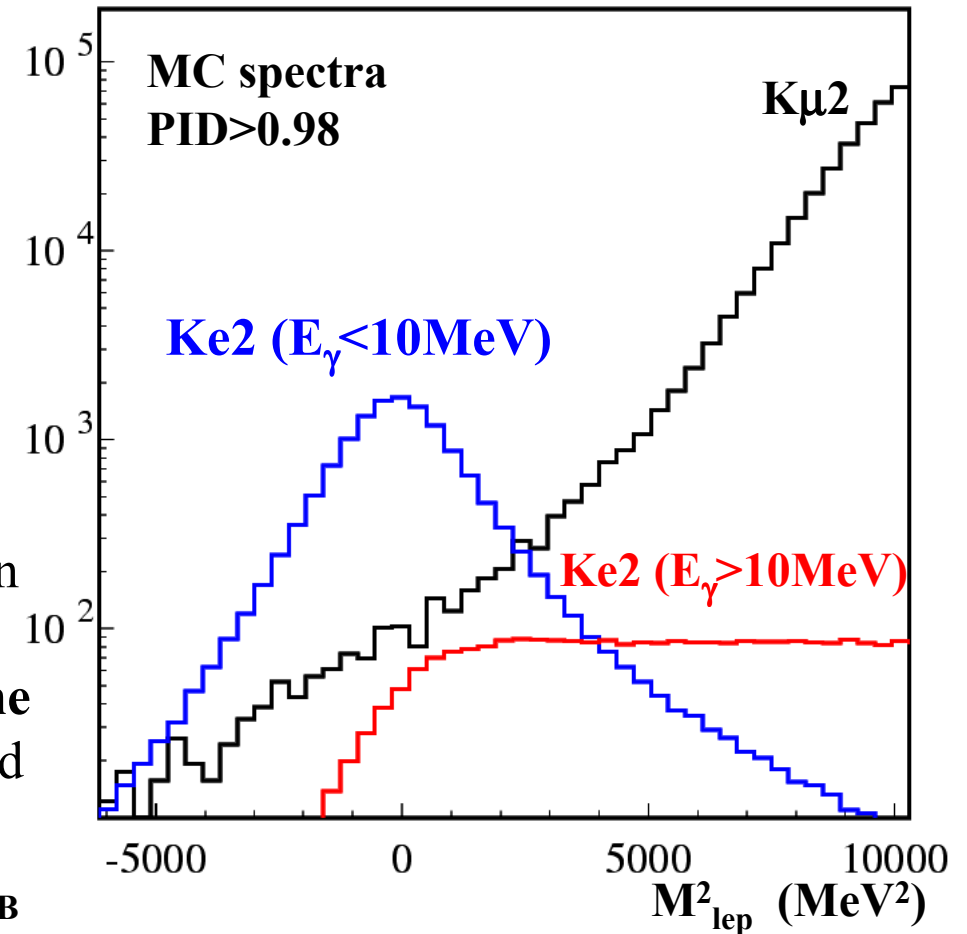
- Analysis inclusive of photons in the final state. In our fit region we expect:

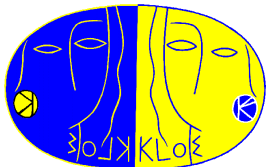
$$\frac{\text{Ke2 } (E_\gamma > 10 \text{ MeV})}{\text{Ke2 } (E_\gamma < 10 \text{ MeV})} \sim 10\%$$

- Repeat fit by varying  $\text{Ke2 } (E_\gamma > 10 \text{ MeV})$  by 15% (DE uncertainty) get 0.5% error.

We performed a **dedicated study of the Ke2 $\gamma$  differential decay rate** (see Moulson talk):

- $E_\gamma$  spectrum measured for the first time
- confirm DE content of our MC, evaluated with ChPT  $O(p^4)$ , within  $\sim 4\%$  accuracy
- obtain **0.2% systematic error on Ke2<sub>IB</sub>**



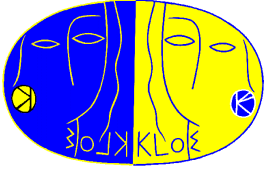


# *Reconstruction efficiencies*

The ratio of  $K_e2$  to  $K_\mu2$  efficiencies is evaluated with MC and corrected using data control samples

- 1) kink reconstruction (tracking):**  $K^+e3$  and  $K^+\mu2$  data control samples selected using the tagging and additional criteria based on EMC information only (next slide)
- 2) cluster efficiency ( $e, \mu$ ):**  $K_L$  control samples, selected with tagging and kinematic criteria based on DC information only
- 3) trigger:** exploit the OR combination of EMC and DC triggers (almost uncorrelated); downscaled samples are used to measure efficiencies for cosmic-ray and machine background vetoes

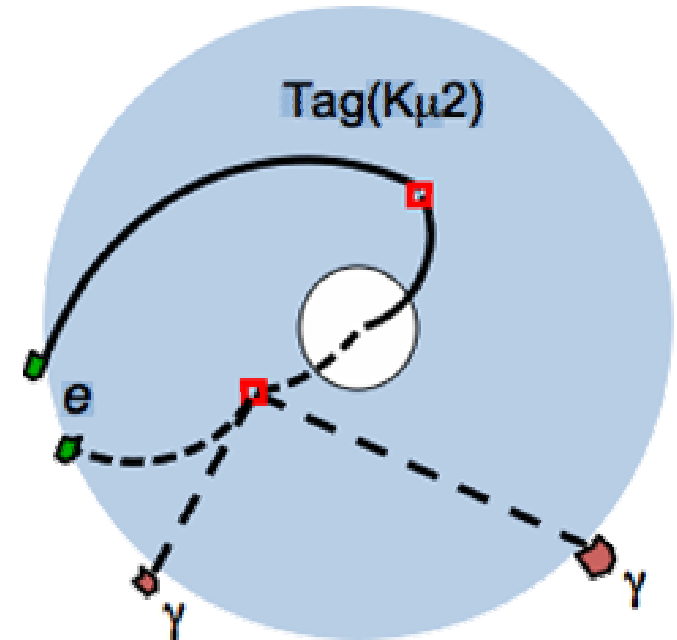
We obtain:  $\varepsilon(K_e2)/\varepsilon(K_\mu2) = 0.946 \pm 0.007$



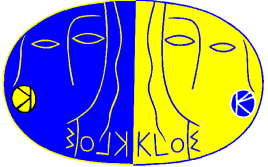
# *Control samples for tracking efficiencies*

Just an example: selection of  $K^+e3$  control sample to measure tracking efficiency for electrons

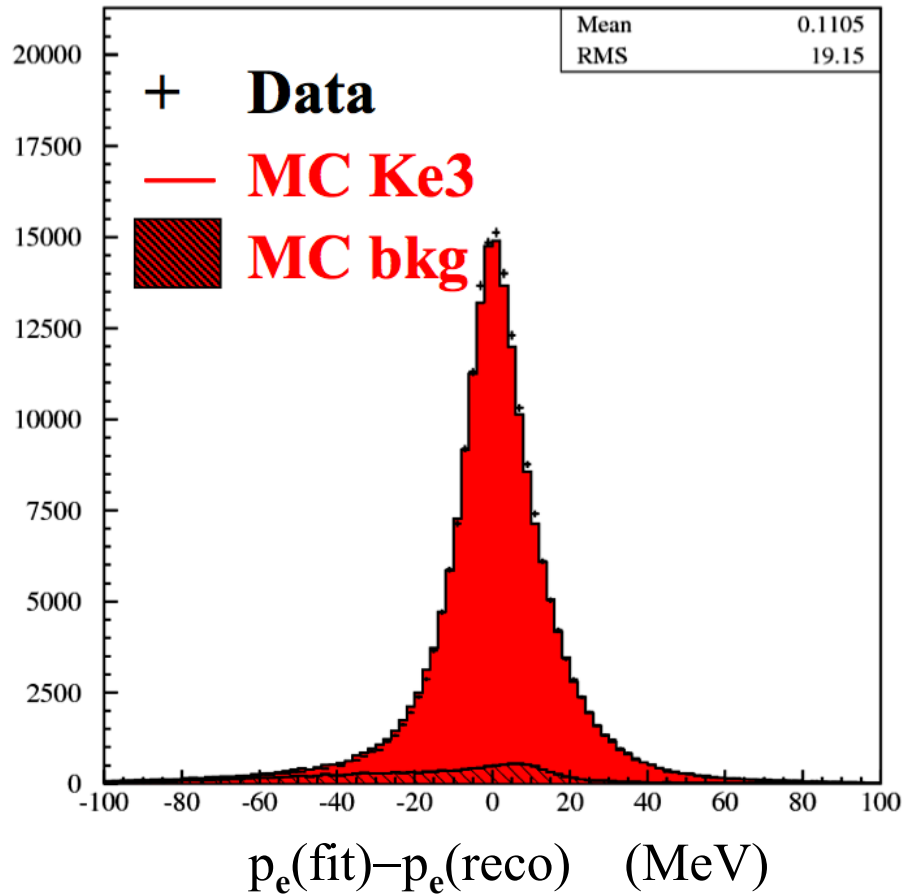
- 0) **Tagging decay** ( $K\mu2$  or  $K\pi2$ );
- 1) Tagging decay ( $K\mu2$  or  $K\pi2$ ): **reconstruction of the opposite charge kaon flight path**;
- 2) Using a ToF technique a  **$\pi^0 \rightarrow \gamma\gamma$  decay vertex** is reconstructed along the K decay path;
- 3) Require an electron cluster:  **$p_e$  estimated from a kinematic fit** with constraints on  $E/p$ , ToF, cluster position, and  $E_{\text{miss}} - P_{\text{miss}}$ .



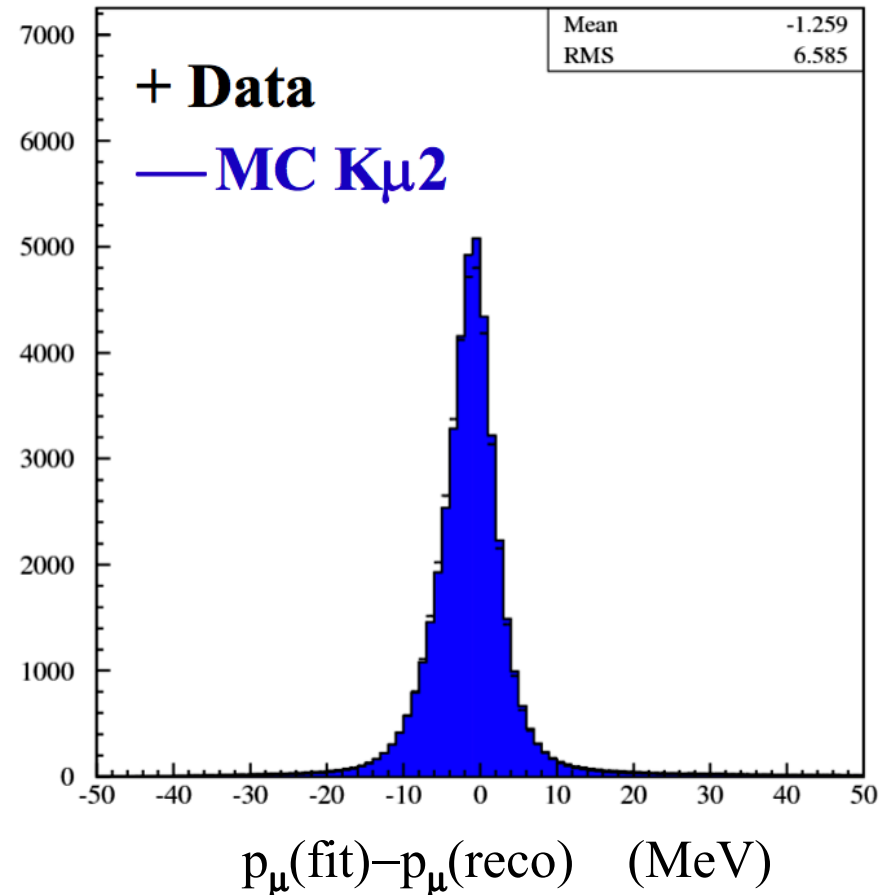
Evaluate the K + electron kink reconstruction efficiency



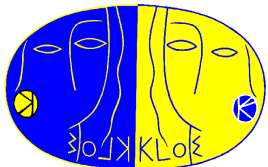
# Control samples for tracking efficiencies



- For electron tracks obtain a resolution  $\sigma \sim 19$  MeV



- With a similar method, get  $\sigma \sim 7$  MeV for muon tracks



# Systematics and checks

**Cross-check on efficiencies:** use same algorithms to measure  $R_{13} = \Gamma(\text{Ke}3)/\Gamma(\text{K}\mu3)$

$$R_{13} = 1.507 \pm 0.005 \text{ for } \text{K}^+$$

$$R_{13} = 1.510 \pm 0.006 \text{ for } \text{K}^-$$

SM expectation (FlaviaNet)

$$R_{13} = 1.506 \pm 0.003$$

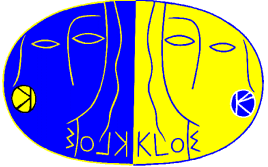
## Summary of systematics:

<b>Tracking</b>	<b>0.6%</b>	$\text{K}^+$ control samples
<b>Trigger</b>	<b>0.4%</b>	downscaled events
<b>syst on Ke2 counts</b>	<b>0.3%</b>	fit stability
<b>Ke2<math>\gamma</math> DE component</b>	<b>0.2%</b>	measurement on data
<b>Clustering for e, <math>\mu</math></b>	<b>0.2%</b>	$\text{K}_L$ control samples

**Total Syst**

**0.8%**

(0.6% from statistics of control samples)



# $R_K$ : KLOE result

$$R_K = (2.493 \pm 0.025 \pm 0.019) \times 10^{-5}$$

Total error:

$$1.3\% = 1.0\%_{\text{stat}} + 0.8\%_{\text{syst}}$$

0.9% from 14k Ke2 dominated  
+ bkg subtraction by statistics

PDG 2008:

$$R_K = (2.45 \pm 0.11) \times 10^{-5}$$

4.5% accuracy

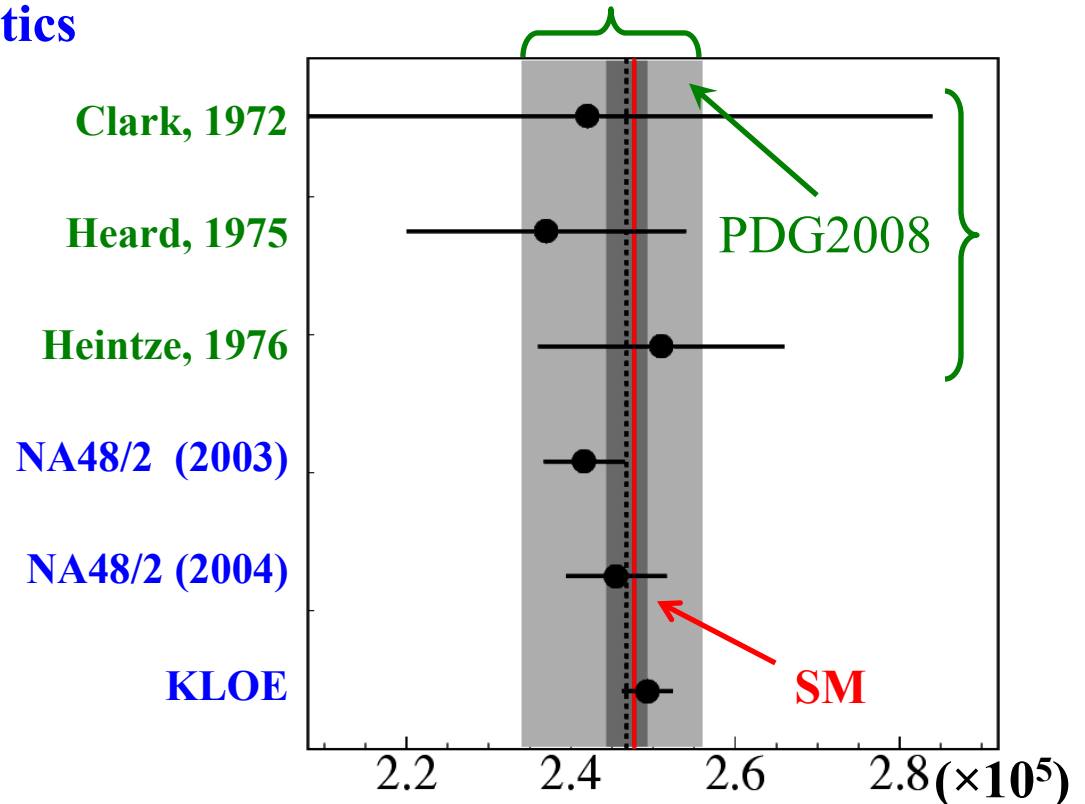
New world average:

$$R_K = (2.468 \pm 0.025) \times 10^{-5}$$

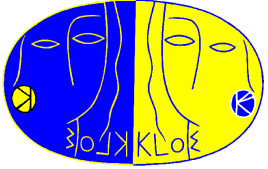
1% accuracy

$$R_K^{\text{SM}} = 2.477(1) \times 10^{-5}$$

- The result does not depend upon the kaon charge:  
 $K^+$ : 2.496(37) vs  $K^-$ : 2.490(38)  
(uncorrelated errors only)
- Agrees with SM prediction

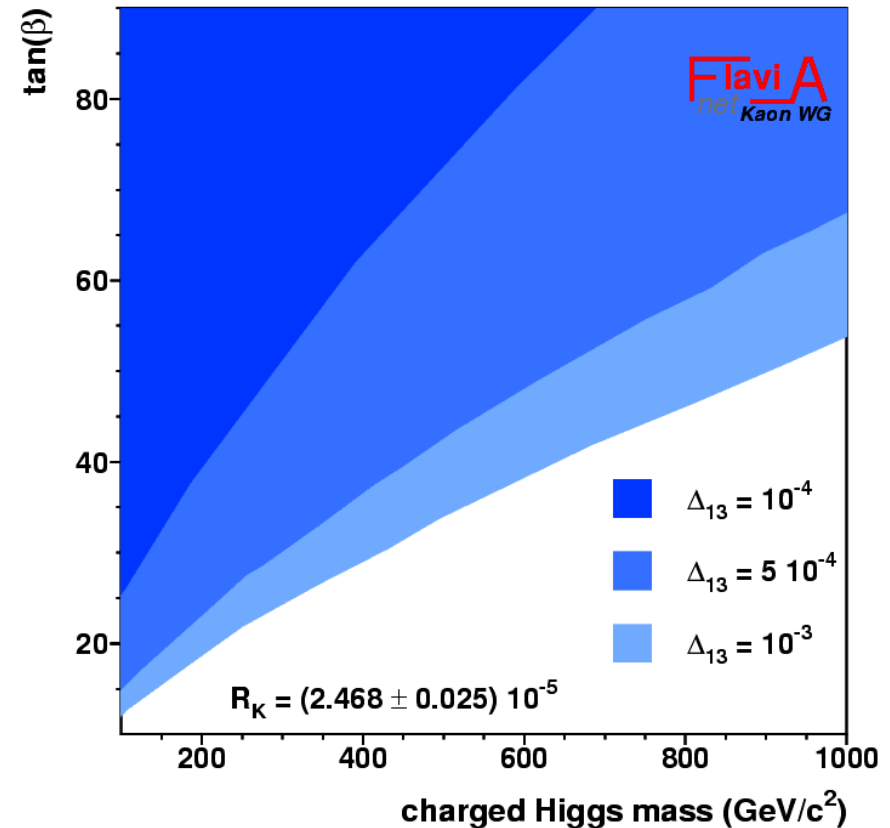
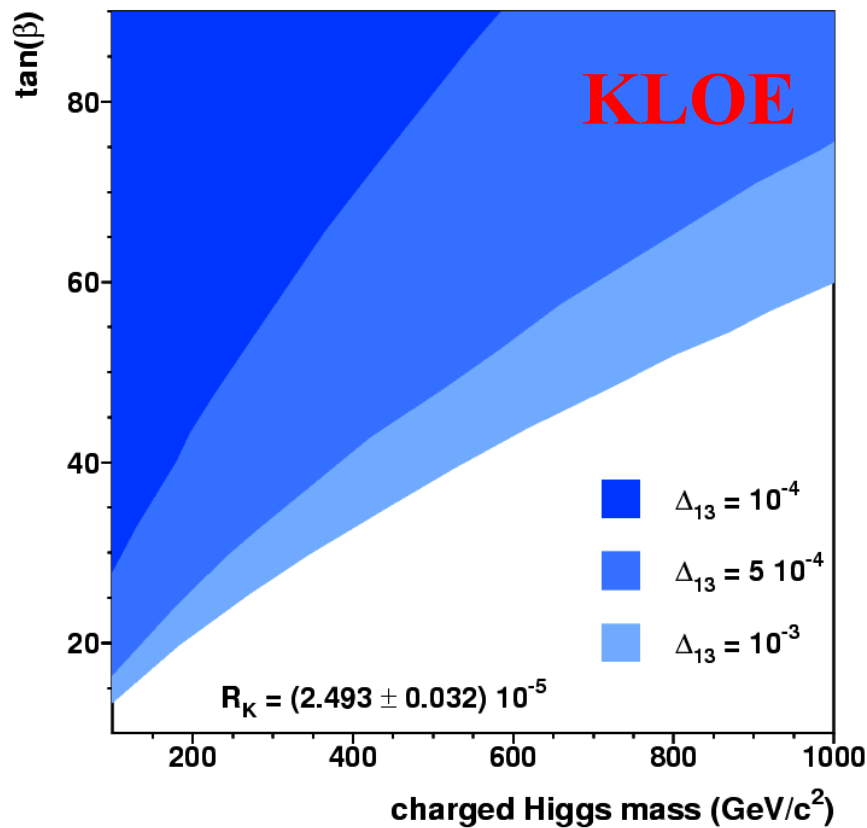






# $R_K$ : sensitivity to new physics

Sensitivity shown as 95% CL excluded regions in the  $\tan\beta$ – $M_H$  plane, for different values of the LFV effective coupling,  $\Delta_{13} = 10^{-3}, 5 \times 10^{-4}, 10^{-4}$





# Conclusions

- Using  $2.2 \text{ fb}^{-1}$  of data acquired at the  $\phi$  peak, KLOE measured:  
 $R_K = (2.493 \pm 0.025_{\text{stat}} \pm 0.019_{\text{syst}}) \times 10^{-5}$
- This results confirms the SM prediction within the 1.3% accuracy
- The error is dominated by the **counting** and the **control samples statistics**.
- Can contribute to set constraints on the parameter space of MSSM with LFV.



東海道  
五拾三次之内

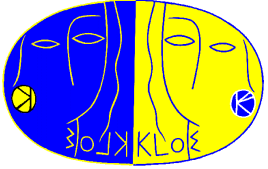
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Additional  
information



# $K_{\mu 2}$ : sensitivity to new physics

Scalar currents, e.g. due to Higgs exchange, affect  $K \rightarrow \mu\nu$  width

$$R_{l23} = \left| \frac{V_{us}(K_{\mu 2})}{V_{us}(K_{l3})} \times \frac{V_{ud}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\mu 2})} \right|$$

$$= \left| 1 - \frac{m_{K^+}^2}{m_{H^+}^2} \left( 1 - \frac{m_{\pi^+}^2}{m_{K^+}^2} \right) \frac{\tan^2 \beta}{1 - \varepsilon_0 \tan \beta} \right|$$

[Hou, Isidori-Paradisi]

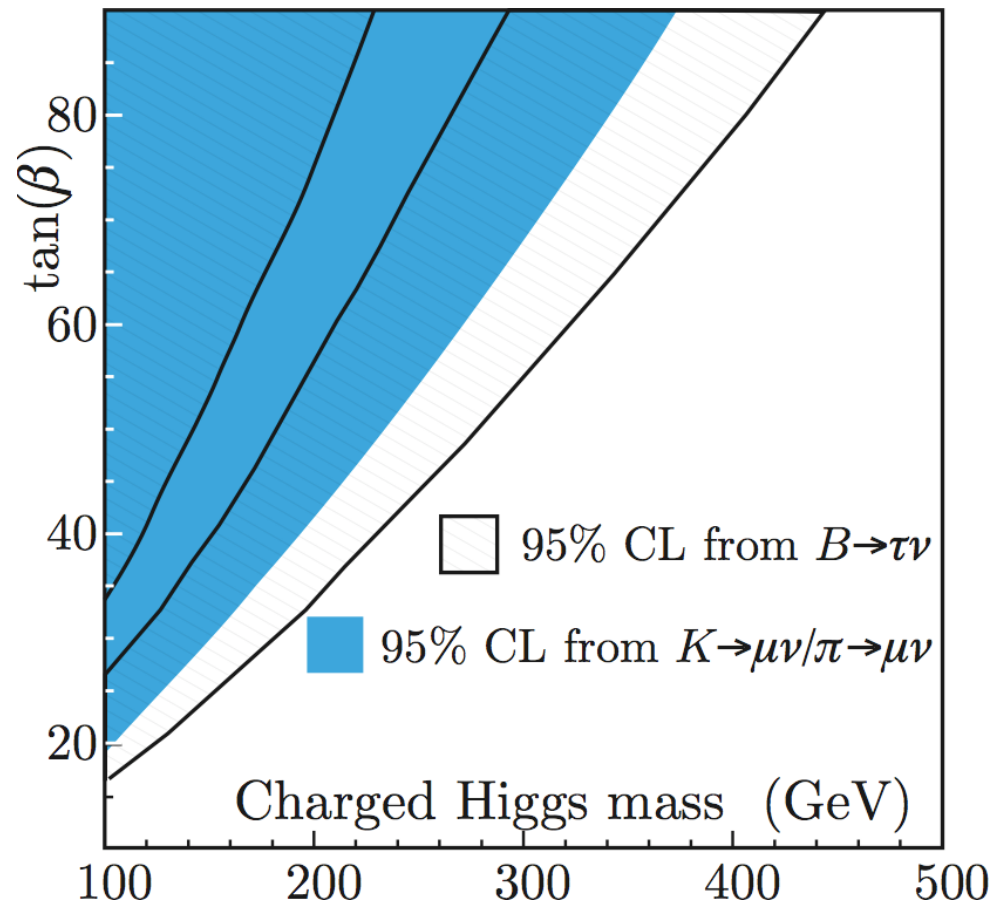
$R_{l23} = 1$  in SM

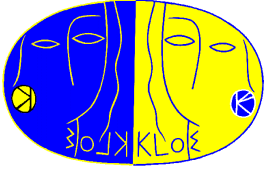
we find

$$R_{l23} = 1.008 \pm 0.008$$

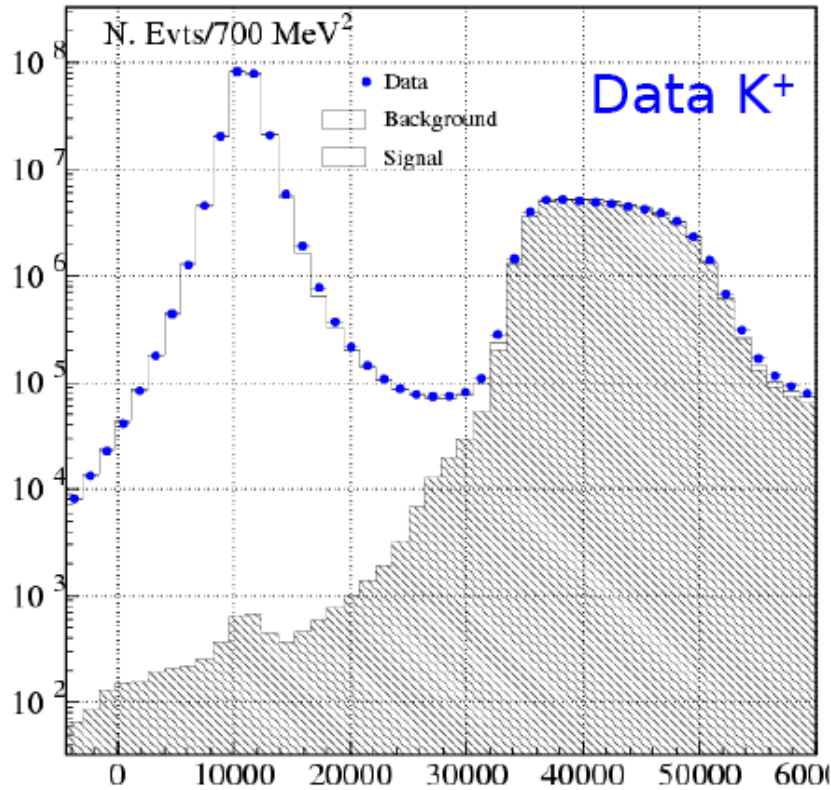
limited by lattice uncertainty on  $f_+(0)$  and  $f_K/f_\pi$

From direct searches (LEP),  $M_{H^+} > 80$  GeV,  $\tan\beta > 2$

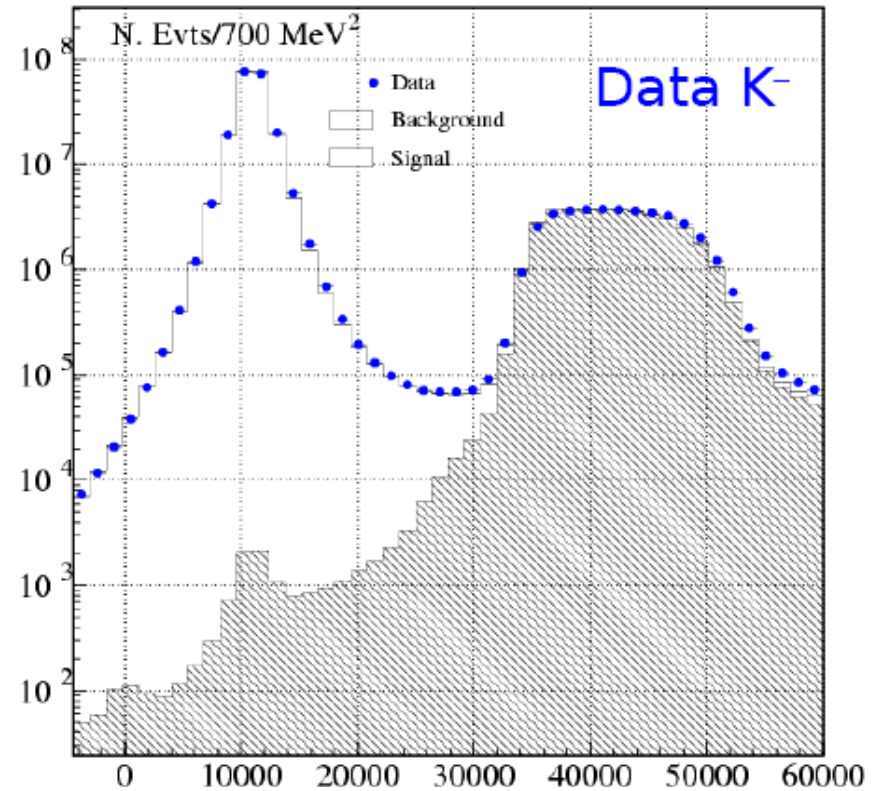




# $K\mu 2$ event counting

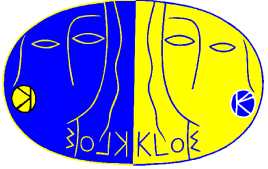


$M^2_{lep} \text{ (MeV}^2\text{)}$

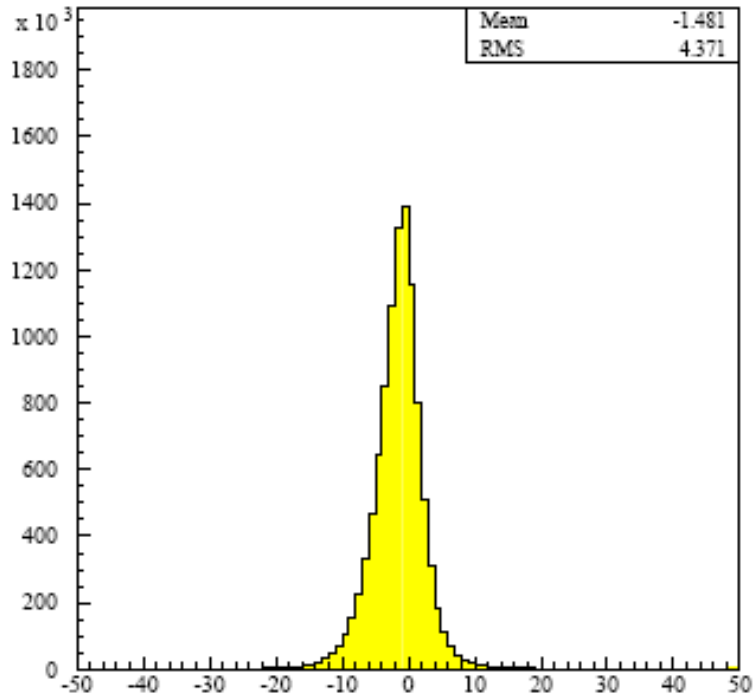


$M^2_{lep} \text{ (MeV}^2\text{)}$

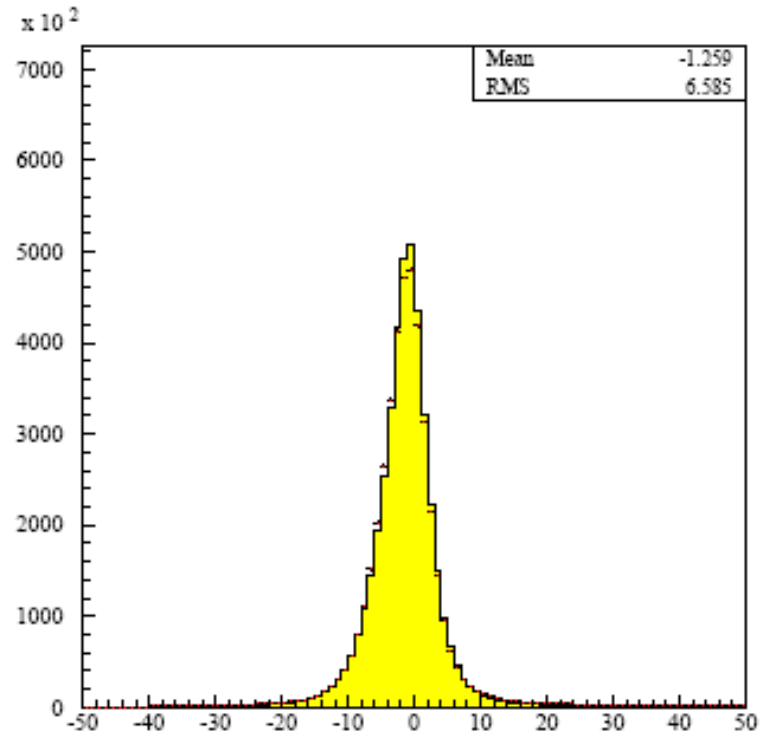
Fit to  $M^2_{lept}$  distribution: 300 million  $K\mu 2$  events per charge  
Background under the peak  $< 0.1\%$ , from MC



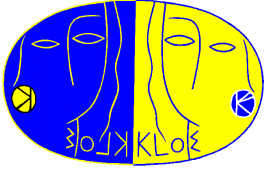
# Tracking efficiency



$p_{\mu}(\text{fit}) - p_{\mu}(\text{MC})$  (MeV)

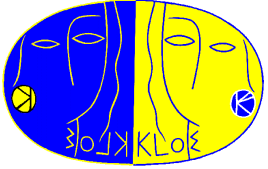


$p_{\mu}(\text{fit}) - p_{\mu}(\text{reco})$  (MeV)



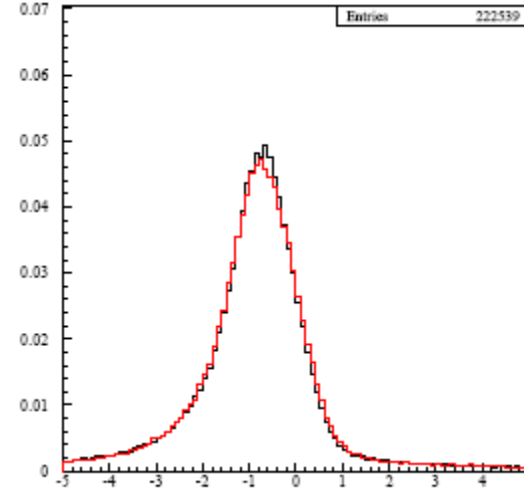
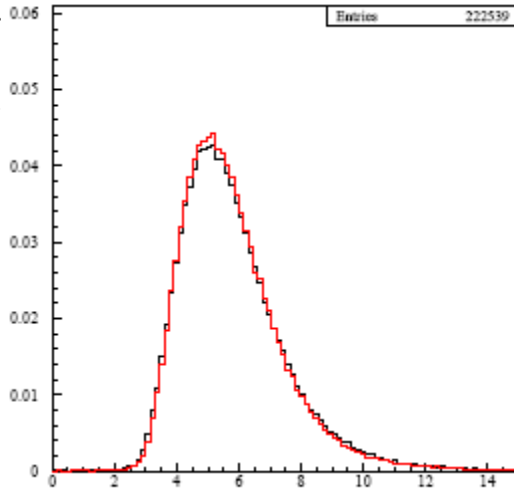
- 1) E/P;
- 2) 1st momentum of the distribution of the longitudinal energy path deposition (cluster centroid depth) evaluated at cell level;
- 3) the 3rd momentum of the longitudinal energy path deposition (skewness);
- 4,5) asymmetry of energy lost in first two innermost (outermost) planes;
- 6) RMS of energy plane distribution;
- 7) energy lost in the 1st plane;
- 8) number of the plane with largest energy deposition;
- 9) largest energy deposition in a single plane;
- 10) slope of the  $E_{int}(x)$  energy distribution;
- 11) curvature of the  $E_{int}(x)$  energy distribution;
- 12)  $de/dx$  i.e. value of  $E_{int}(x)/x|_{x < 15 \text{ cm}}$

Additional separation using ToF information: difference  $\delta T$  of the time measured in the EMC with that expected from the DC measurements in electron mass hypothesis has been included in the final version of the NN: 12-25-20-1 becomes 13-25-20-1



# *NN input distributions: some example*

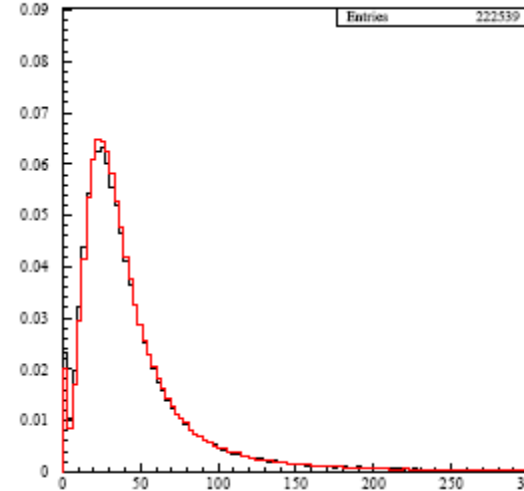
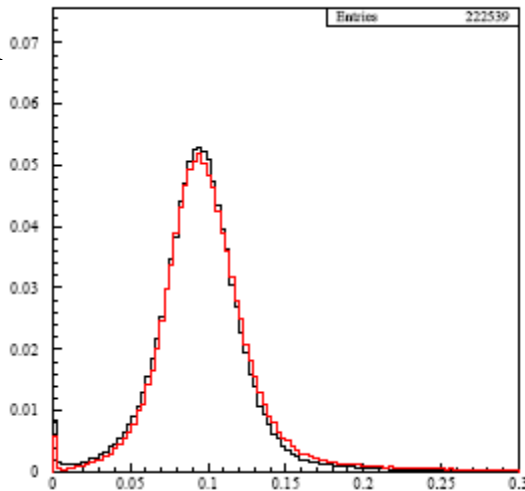
Cluster  
centroid  
depth



Asymmetry  
of energy lost  
in first two  
innermost  
planes

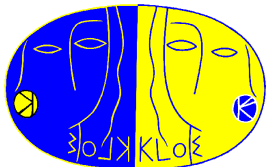
**Data and MC**

dE/dx

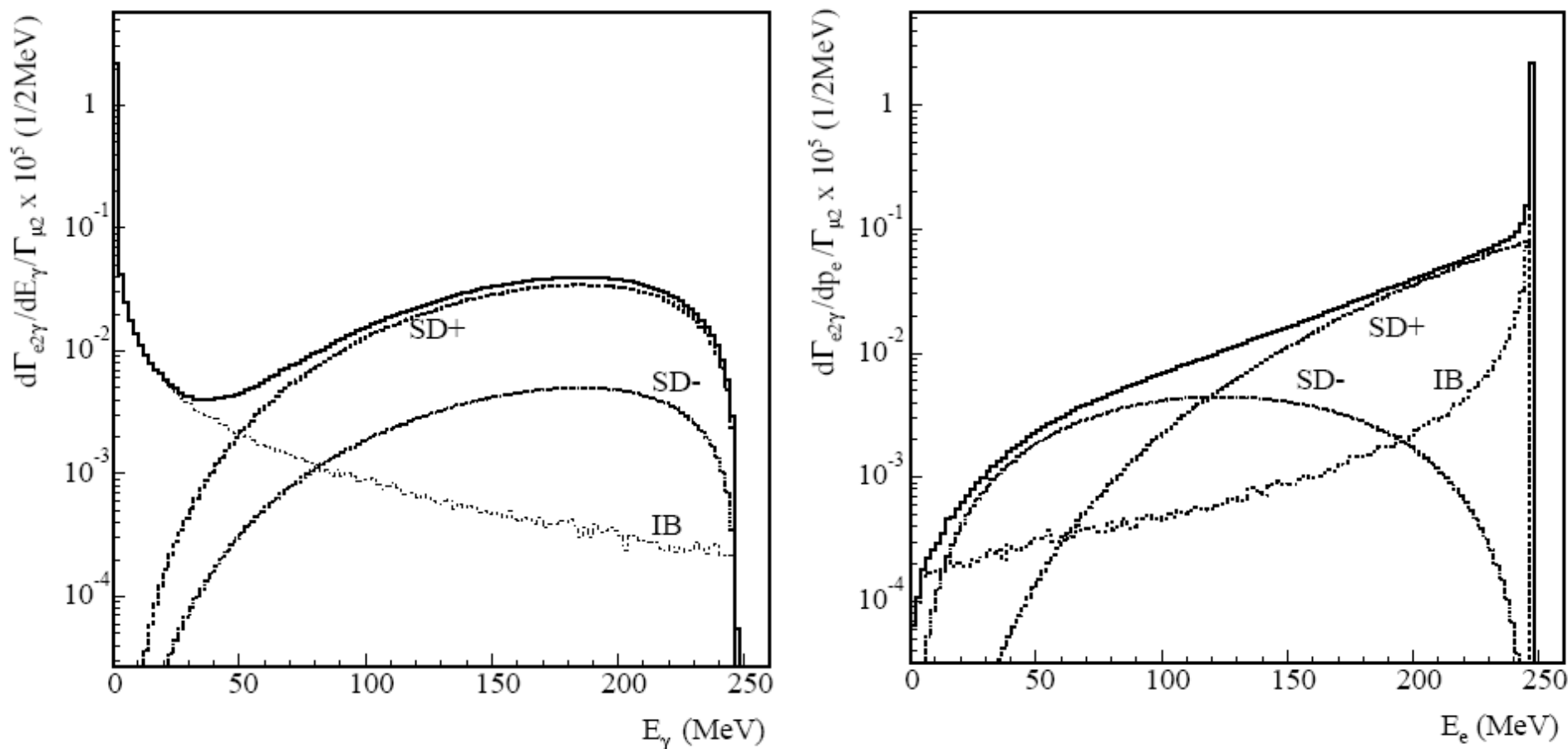


$E_{INT}(x)$  slope

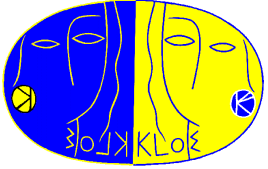




# Distributions for $Ke2\gamma$ decay



For  $Ke2\gamma$  generator, the IB component is described with  $\chi_{PT}$  at  $O(e^2p^2)$  including resummation of leading logarithms, while DE component is described with  $\chi_{PT}$  at  $O(e^2p^4)$ .



# Ke2 $\gamma$ process

Dalitz density

$$\frac{d\Gamma(K \rightarrow e\nu\gamma)}{dxdy} = \rho_{IB}(x,y) + \rho_{SD}(x,y) + \rho_{INT}(x,y)$$

*helicity suppressed*
*negligible*

$$x = 2E_\gamma/M_K \quad y = 2E_e/M_K$$

$E_\gamma, E_e$  in the K rest frame

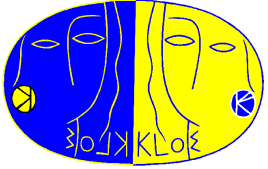
## Structure Dependent

$$\rho_{SD}(x,y) = \frac{G_F^2 |V_{us}|^2 \alpha}{64\pi^2} M_K^5 \left( (f_V + f_A)^2 f_{SD+}(x,y) + (f_V - f_A)^2 f_{SD-}(x,y) \right)$$

$f_V, f_A$  : effective vector  
and axial couplings

SD+ = V+A :  $\gamma$  polarization +

SD- = V-A :  $\gamma$  polarization -



# *Ke2 $\gamma$ theory predictions*

## 1) ChPT at O(p<sup>4</sup>):

$$f_V \approx 0.0945$$

$$f_A \approx 0.0425$$

no dependence on photon energy

Bijnens, Ecker, Gasser 93

## 2) ChPT at O(p<sup>6</sup>):

$$f_V \approx 0.082(1 + \lambda(1-x))$$

$$f_A \approx 0.034$$

V linear x dependence ( $\lambda \approx 0.4$ )

Ametller, Bijnens, Bramon, Cornet 93

Geng, Ho, Wu 04

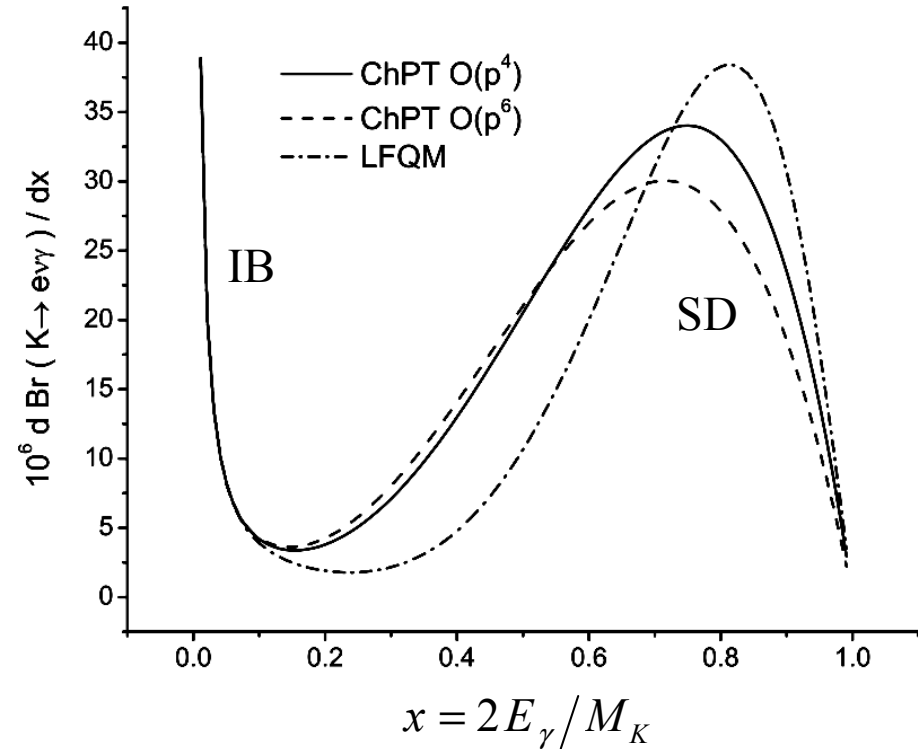
Chen, Geng, Lih 08

## 3) LFQM:

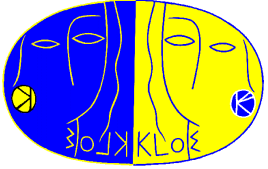
non trivial x dependence

$$f_V = f_A = 0 \quad \text{at } x=0$$

Chen, Geng, Lih 08

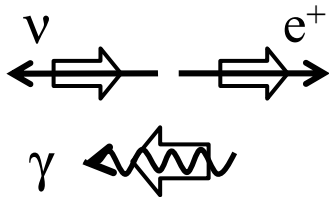
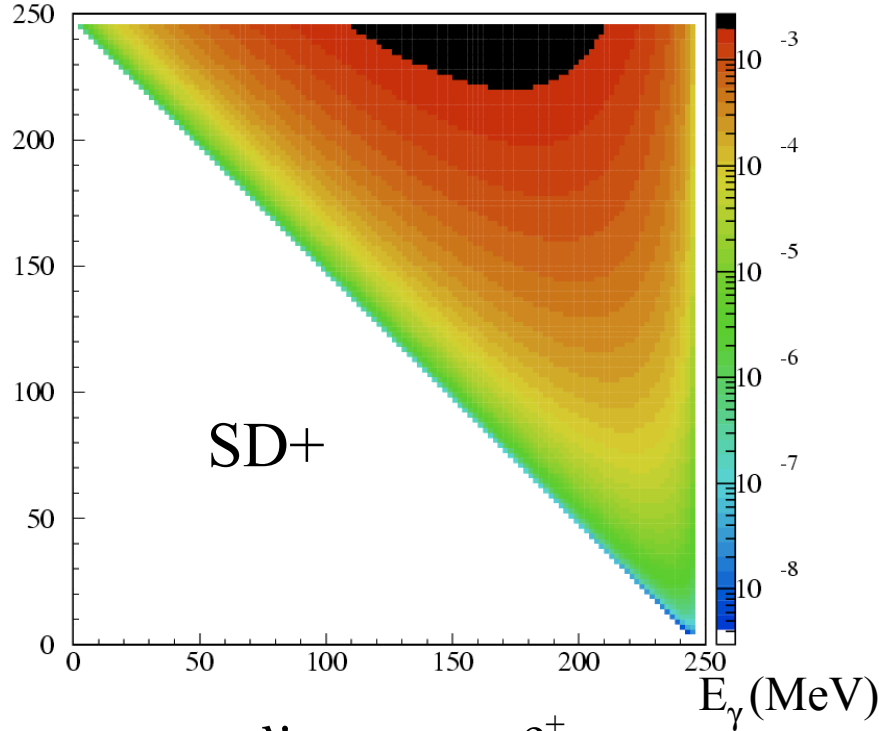


from Phys. Rev. D77 (2008) 014004



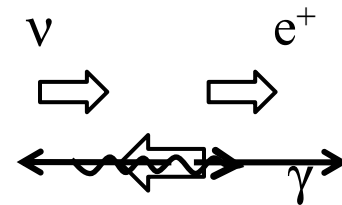
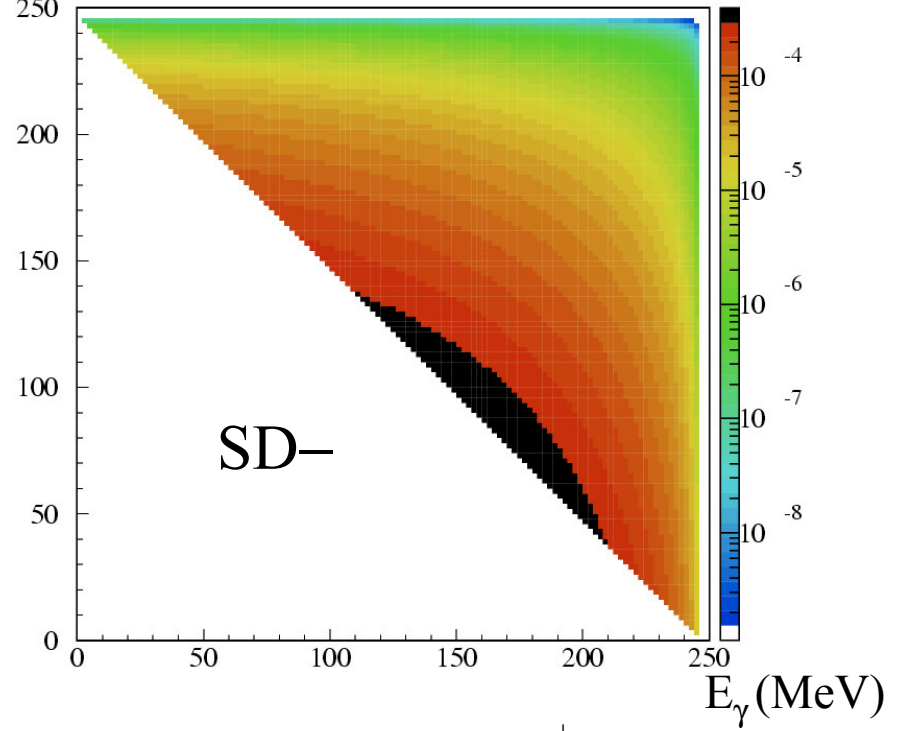
# Dalitz plots for $SD+$ and $SD-$

$p_e$  (MeV)



electron peaks at 250 MeV,  
e- $\gamma$  antiparallel

$p_e$  (MeV)



electron peaks at 100 MeV: **very bad**,  
since  $Ke3$  endpoint is 230 MeV