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# CPT symmetry and Quantum Mechanics tests in the neutral kaon system at KLOE



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on behalf of **KLOE collaboration**



Theoretical and experimental aspects of  
the spin-statistics connections and related symmetries,  
Trieste, Italy – October 21-25, 2008

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# CPT: introduction

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The three discrete symmetries of QM, C (charge conjugation), P (parity), and T (time reversal) are known to be violated in nature both singly and in pairs. Only CPT appears to be an exact symmetry of nature.

CPT theorem (Luders, Jost, Pauli, Bell 1955 -1957):

Exact CPT invariance holds for any quantum field theory (flat space-time) which assumes:

(1) Lorentz invariance (2) Locality (3) Unitarity (i.e. conservation of probability).

Testing the validity of the CPT symmetry probes the most fundamental assumptions of our present understanding of particles and their interactions.

Extension of CPT theorem to a theory of quantum gravity far from obvious (e.g. CPT violation appears in some models with space-time foam backgrounds).

No predictive theory incorporating CPT violation => only phenomenological models to be constrained by experiments.

The neutral kaon system offers unique possibilities to test CPT invariance e.g. :

$$\left| m_{K^0} - m_{\bar{K}^0} \right| / m_K < 10^{-18}, \quad \left| m_{B^0} - m_{\bar{B}^0} \right| / m_B < 10^{-14}, \quad \left| m_p - m_{\bar{p}} \right| / m_p < 10^{-8}$$

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# 1) “Standard” test of CPT symmetry in the neutral kaon system

# CPT test: the Bell-Steinberger relation

$$|K_{S,L}\rangle = \frac{1}{\sqrt{2(1+|\varepsilon_{S,L}|)}} \left[ (1 + \varepsilon_{S,L}) |K^0\rangle \pm (1 - \varepsilon_{S,L}) |\bar{K}^0\rangle \right]$$

**CPT violation  
in the mixing:**

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2}$$

$$\Delta m = m_L - m_S$$

$$\Delta\Gamma = \Gamma_S - \Gamma_L$$

$$\phi_{SW} = \arctan(2\Delta m/\Delta\Gamma)$$

Unitarity constraint:  $|K\rangle = a_S |K_S\rangle + a_L |K_L\rangle$

$$\left( -\frac{d}{dt} \| |K(t)\rangle \|^2 \right)_{t=0} = \sum_f |a_S \langle f|T|K_S\rangle + a_L \langle f|T|K_L\rangle|^2$$

**Bell-Steinberger relation:**

$$\left( \frac{\Re\varepsilon}{1+|\varepsilon|^2} - i\Im\varepsilon \right) = \frac{\frac{1}{\Gamma_S - \Gamma_L} \sum_f \langle f|T|K_S\rangle^* \langle f|T|K_L\rangle}{\left( \frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right)}$$

$K_S$   $K_L$  observables:  
they can be expressed in  
terms of BR's, decay  
amplitude ratios,  $\Delta m$ ,  
lifetimes, of  $K_S$  and  $K_L$

# Experimental inputs to the Bell-Steinberger relation

|   | Value   | Source               |
|---|---|----------------------|
| $\tau_{K_S}$  | $0.08958 \pm 0.00005$ ns                        | PDG [14]             |
| $\tau_{K_L}$  | $50.84 \pm 0.23$ ns                             | KLOE average         |
| $m_L - m_S$   | $(5.290 \pm 0.016) \times 10^9$ s <sup>-1</sup> | PDG [14]             |
| $\text{BR}(K_S \rightarrow \pi^+ \pi^-)$                | $0.69186 \pm 0.00051$                           | KLOE average         |
| $\text{BR}(K_S \rightarrow \pi^0 \pi^0)$                | $0.30687 \pm 0.00051$                           | KLOE average         |
| $\text{BR}(K_S \rightarrow \pi \ell \nu)$               | $(11.77 \pm 0.15) \times 10^{-4}$               | KLOE [6]             |
| $\text{BR}(K_L \rightarrow \pi^+ \pi^-)$                | $(1.933 \pm 0.021) \times 10^{-3}$              | KLOE average         |
| $\text{BR}(K_L \rightarrow \pi^0 \pi^0)$                | $(0.848 \pm 0.010) \times 10^{-3}$              | KLOE average         |
| $\phi_{+-}$   | $(43.4 \pm 0.7)^\circ$                          | PDG [14]             |
| $\phi_{00}$   | $(43.7 \pm 0.8)^\circ$                          | PDG [14]             |
| $R_{S,\gamma} (E_\gamma > 20\text{MeV})$                | $(0.710 \pm 0.016) \times 10^{-2}$              | E731 [18]            |
| $R_{S,\gamma}^{\text{th-IB}} (E_\gamma > 20\text{MeV})$ | $(0.700 \pm 0.001) \times 10^{-2}$              | KLOE MC [19]         |
| $ \eta_{+-\gamma} $                                     | $(2.359 \pm 0.074) \times 10^{-3}$              | E773 [17]            |
| $\phi_{+-\gamma}$                                       | $(43.8 \pm 4.0)^\circ$                          | E773 [17]            |
| $\text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0)$          | $0.1262 \pm 0.0011$                             | KLOE average         |
| $\eta_{+-0}$  | $((-2 \pm 7) + i(-2 \pm 9)) \times 10^{-3}$     | CPLEAR [10]          |
| $\text{BR}(K_L \rightarrow 3\pi^0)$                     | $0.1996 \pm 0.0021$                             | KLOE average         |
| $\text{BR}(K_S \rightarrow 3\pi^0)$                     | $< 1.5 \times 10^{-7}$ at 95% CL                | KLOE [5]             |
| $\phi_{000}$  | uniform from 0 to $2\pi$                        |                      |
| $\text{BR}(K_L \rightarrow \pi \ell \nu)$               | $0.6709 \pm 0.0017$                             | KLOE average         |
| $A_L + A_S$   | $(0.5 \pm 1.0) \times 10^{-2}$                  | $K_{\ell 3}$ average |
| $\text{Im}(x_+)$  | $(0.8 \pm 0.7) \times 10^{-2}$                  | $K_{\ell 3}$ average |

Main improvements done with KLOE measurements on  $K_S$  semileptonic and  $3\pi^0$  decays

# CPT test: the Bell-Steinberger relation

**KLOE result:** JHEP12(2006) 011

$$\text{Re } \varepsilon = (159.6 \pm 1.3) \times 10^{-5}$$

$$\text{Im } \delta = (0.4 \pm 2.1) \times 10^{-5}$$

CPLEAR: study of the time evolution of neutral kaons in semileptonic decays

$$\Re \delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52

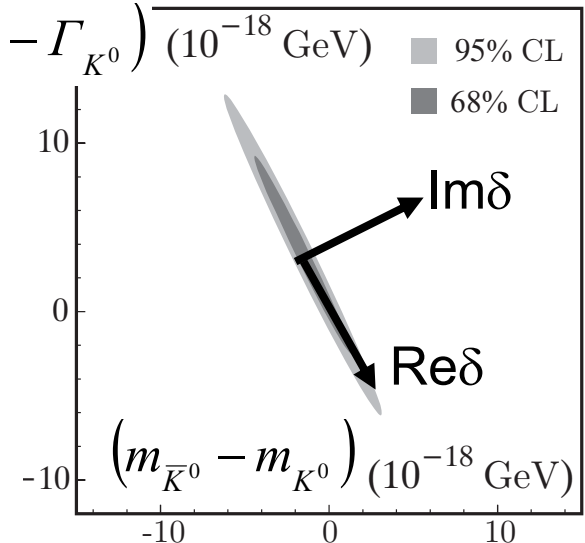
Combining  $\text{Re } \delta$  and  $\text{Im } \delta$  results:

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2} \quad (\Gamma_{\bar{K}^0} - \Gamma_{K^0}) (10^{-18} \text{ GeV})$$

Assuming  $(\Gamma_{\bar{K}^0} - \Gamma_{K^0}) = 0$ , i.e. no CPT viol. in decay:

$$-5.3 \times 10^{-19} < m_{\bar{K}^0} - m_{K^0} < 6.3 \times 10^{-19} \text{ GeV}$$

at 95% c.l.



# CPT test: the Bell-Steinberger relation

**M. Palutan**, presented at  
**FLAVIANET Kaon ws 08 (prelim.):**

$$\text{Re } \varepsilon = (161.2 \pm 0.6) \times 10^{-5}$$

$$\text{Im } \delta = (-0.1 \pm 1.4) \times 10^{-5}$$

( using new KTeV results on  $\phi_{\pi\pi}$  :  
 Moriond EW 08, HQL08)

Combining  $\text{Re}\delta$  and  $\text{Im}\delta$  results:

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2} \quad (\Gamma_{\bar{K}^0} - \Gamma_{K^0}) (10^{-18} \text{ GeV})$$

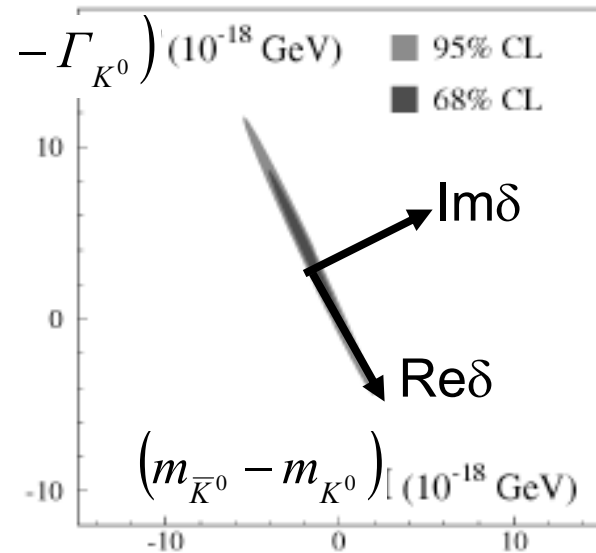
Assuming  $(\Gamma_{\bar{K}^0} - \Gamma_{K^0}) = 0$  , i.e. no CPT viol. in decay:

$$|m_{\bar{K}^0} - m_{K^0}| < 4.0 \times 10^{-19} \text{ GeV at 95\% C.L.}$$

CPLEAR: study of the time evolution of  
 neutral kaons in semileptonic decays

$$\Re\delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52



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## **2) Search for decoherence and CPT violation in the neutral kaon system**



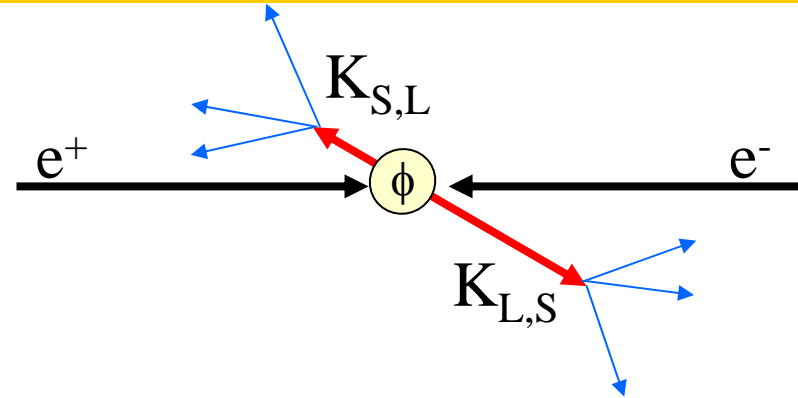
# Neutral kaons at a $\phi$ -factory

Production of the vector meson  $\phi$  in  $e^+e^-$  annihilations:

- $e^+e^- \rightarrow \phi$      $\sigma_\phi \sim 3 \mu\text{b}$   
 $W = m_\phi = 1019.4 \text{ MeV}$
- $\text{BR}(\phi \rightarrow K^0\bar{K}^0) \sim 34\%$
- $\sim 10^6$  neutral kaon pairs per  $\text{pb}^{-1}$  produced in an antisymmetric quantum state with  $J^{PC} = 1^-$  :

$$\mathbf{p}_K = 110 \text{ MeV}/c$$

$$\lambda_S = 6 \text{ mm} \quad \lambda_L = 3.5 \text{ m}$$

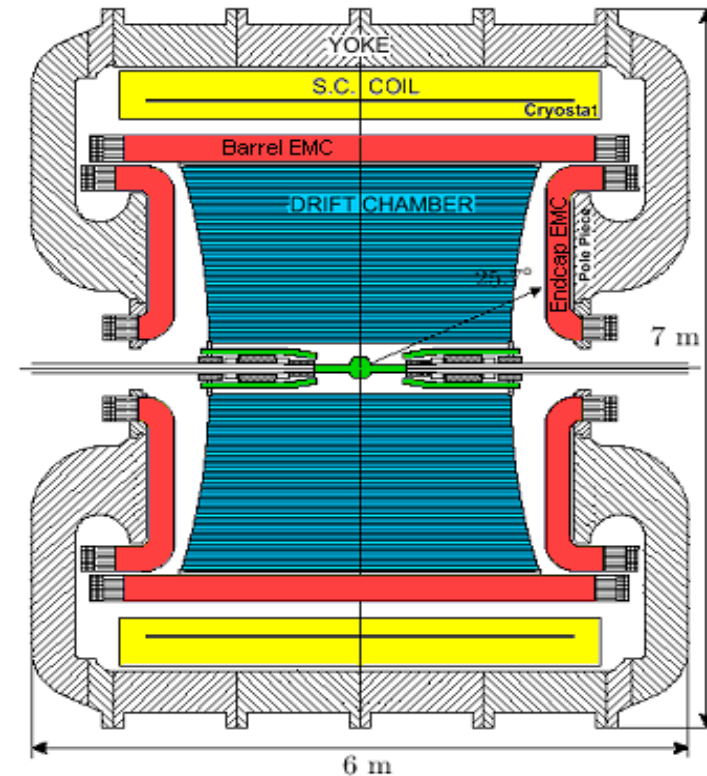


$$\begin{aligned}
 |i\rangle &= \frac{1}{\sqrt{2}} \left[ |K^0(\vec{p})\rangle |\bar{K}^0(-\vec{p})\rangle - |\bar{K}^0(\vec{p})\rangle |K^0(-\vec{p})\rangle \right] \\
 &= \frac{N}{\sqrt{2}} \left[ |K_S(\vec{p})\rangle |K_L(-\vec{p})\rangle - |K_L(\vec{p})\rangle |K_S(-\vec{p})\rangle \right]
 \end{aligned}$$

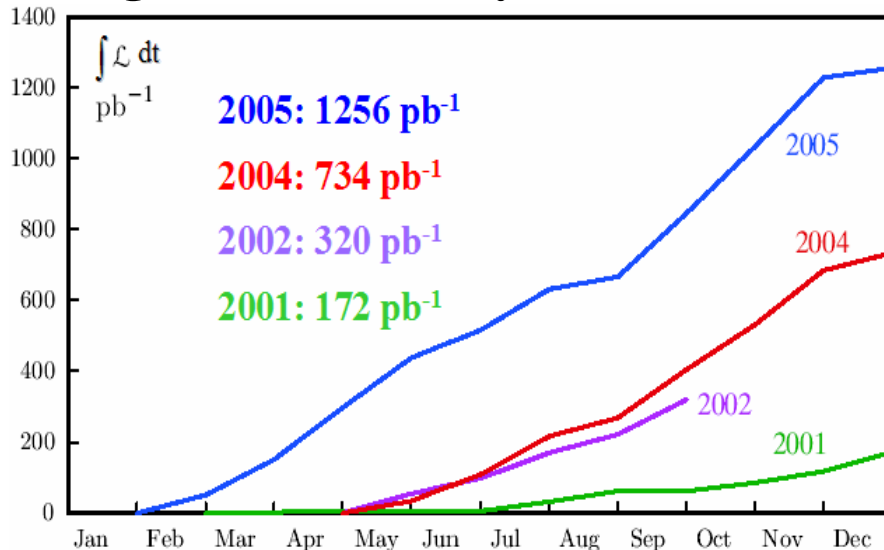
$$N = \sqrt{(1+|\varepsilon_S|^2)(1+|\varepsilon_L|^2)} / (1 - \varepsilon_S \varepsilon_L) \cong 1$$

The detection of a kaon at large (small) times tags a  $K_S$  ( $K_L$ )  
 $\Rightarrow$  possibility to select a pure  $K_S$  beam (**unique** at a  $\phi$ -factory, not possible at fixed target experiments)

# The KLOE detector at the Frascati $\phi$ -factory DAΦNE



## Integrated luminosity (KLOE)



Lead/scintillating fiber calorimeter  
 drift chamber  
 4 m diameter  $\times$  3.3 m length  
 helium based gas mixture

Total KLOE  $\int \mathcal{L} dt \sim 2.5 \text{ fb}^{-1}$   
 (2001 - 05)

$\rightarrow \sim 2.5 \times 10^9 \text{ K}_S \text{K}_L \text{ pairs}$

# Neutral kaon interferometry

$$|i\rangle = \frac{N}{\sqrt{2}} \left[ |K_S(\vec{p})\rangle |K_L(-\vec{p})\rangle - |K_L(\vec{p})\rangle |K_S(-\vec{p})\rangle \right]$$

Double differential time distribution:

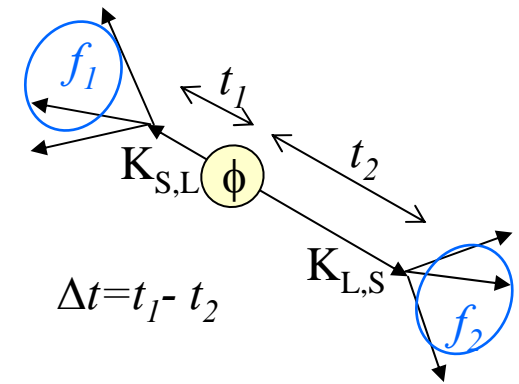
$$I(f_1, t_1; f_2, t_2) = C_{12} \left\{ |\eta_1|^2 e^{-\Gamma_L t_1 - \Gamma_S t_2} + |\eta_2|^2 e^{-\Gamma_S t_1 - \Gamma_L t_2} - 2|\eta_1||\eta_2| e^{-(\Gamma_S + \Gamma_L)(t_1 + t_2)/2} \cos[\Delta m(t_2 - t_1) + \phi_1 - \phi_2] \right\}$$

where  $t_1(t_2)$  is the proper time of one (the other) kaon decay into  $f_1$  ( $f_2$ ) final state and:

$$\eta_i = |\eta_i| e^{i\phi_i} = \langle f_i | T | K_L \rangle / \langle f_i | T | K_S \rangle$$

$$C_{12} = \frac{|N|^2}{2} \left| \langle f_1 | T | K_S \rangle \langle f_2 | T | K_S \rangle \right|^2$$

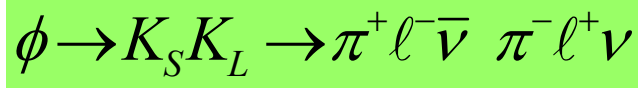
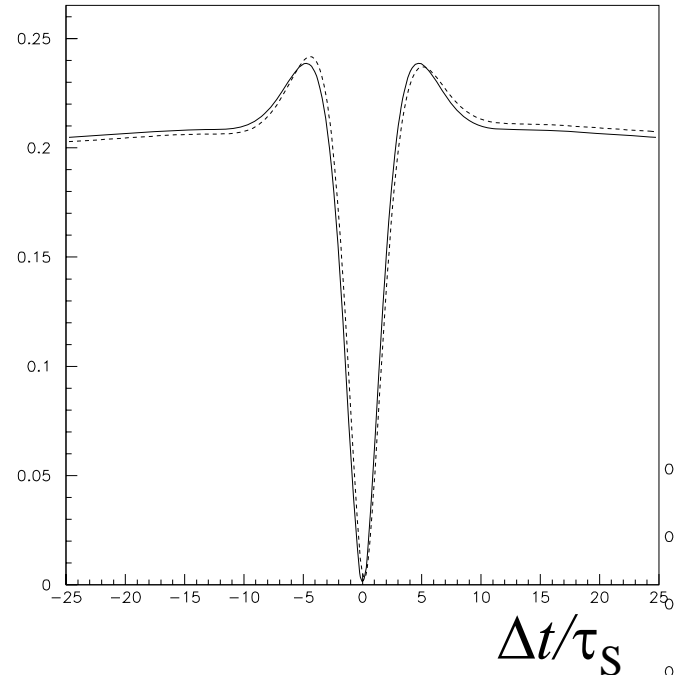
From these distributions for various final states  $f_i$  one can measure the following quantities:  $\Gamma_S$ ,  $\Gamma_L$ ,  $\Delta m$ ,  $|\eta_i|$ ,  $\phi_i \equiv \arg(\eta_i)$



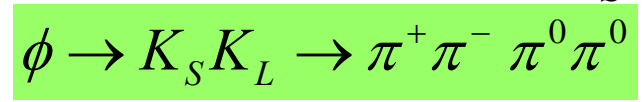
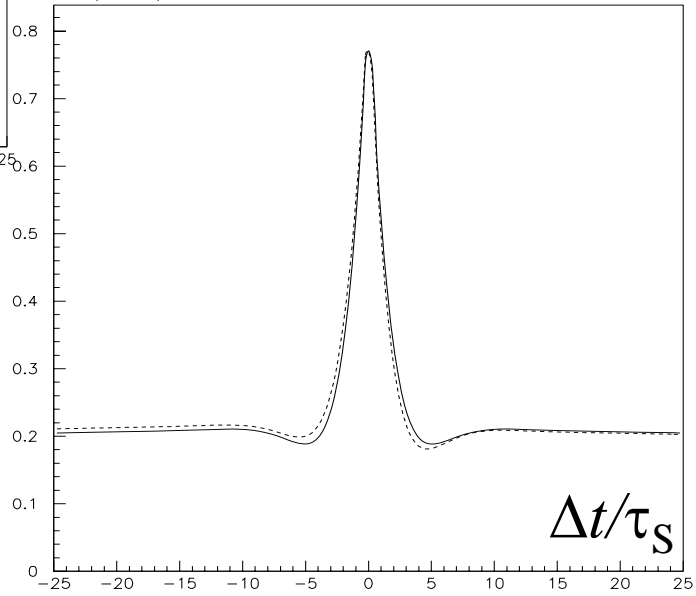
**characteristic interference term  
at a  $\phi$ -factory  $\Rightarrow$  interferometry**

# Neutral kaon interferometry: main observables

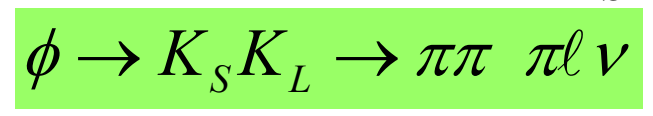
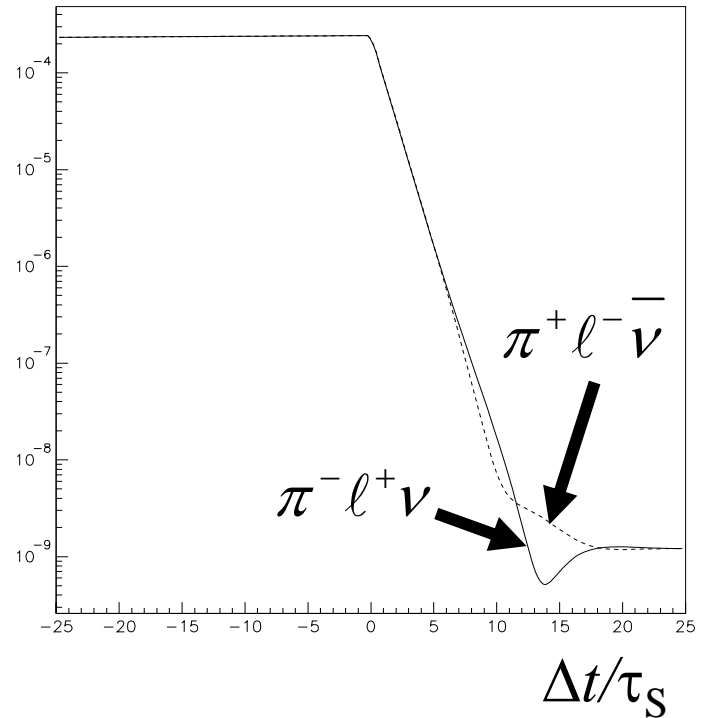
$I(\Delta t)$  (a.u)



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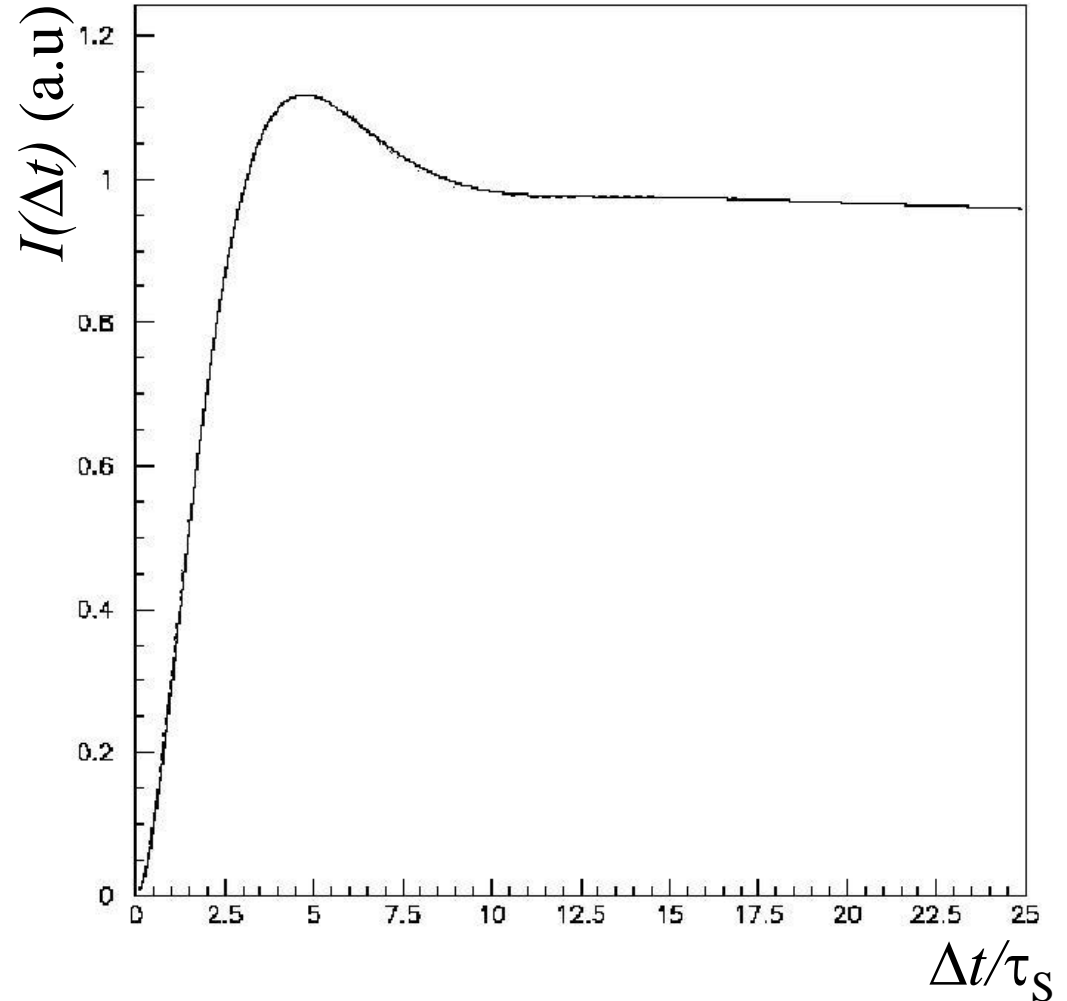
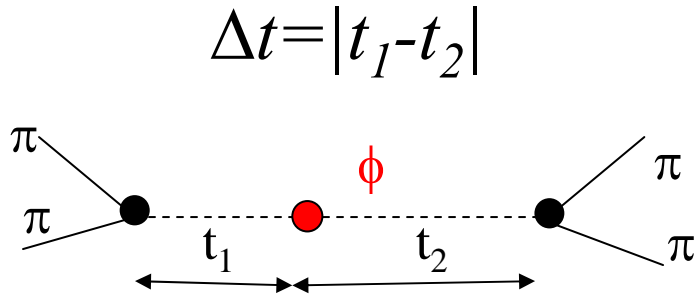
$I(\Delta t)$  (a.u)



$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

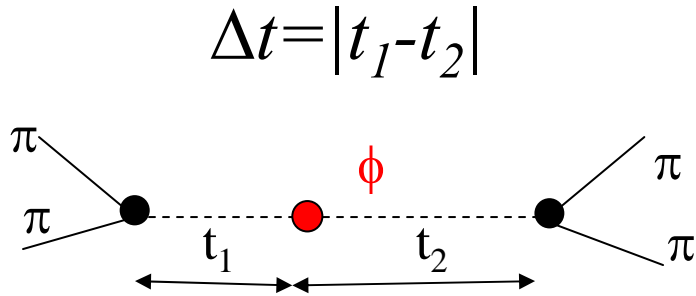
Same final state for both kaons:  $f_1 = f_2 = \pi^+ \pi^-$



$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

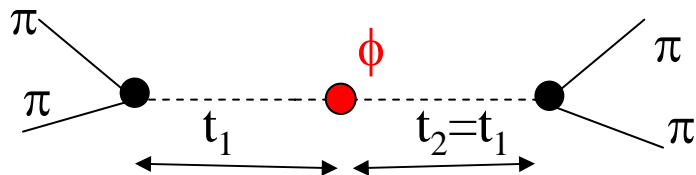
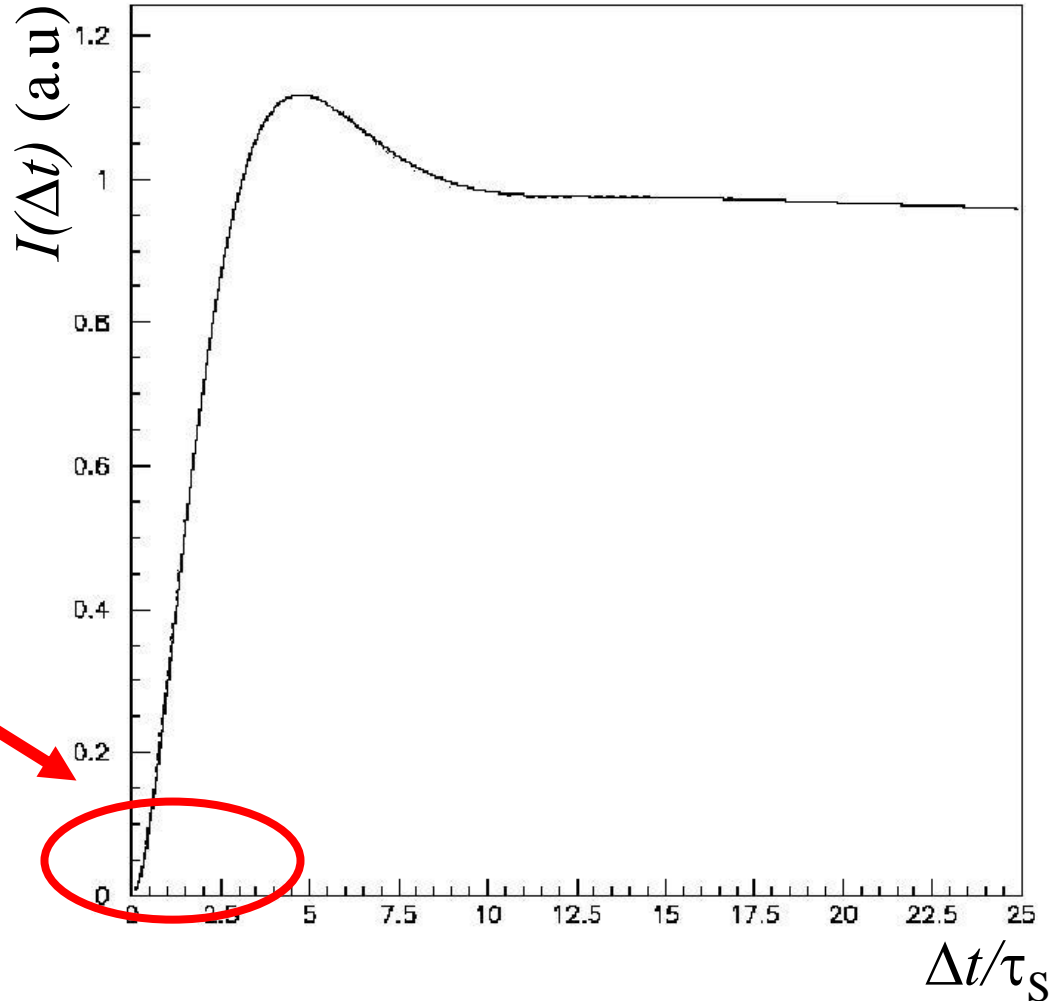
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EPR correlation:

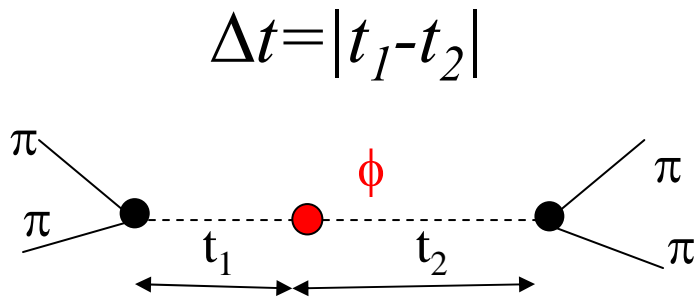
no simultaneous decays  
( $\Delta t=0$ ) in the same  
final state due to the  
destructive  
quantum interference



$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

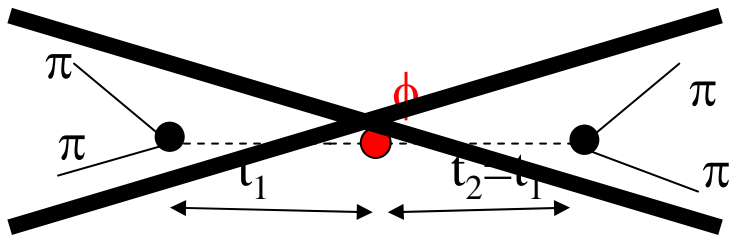
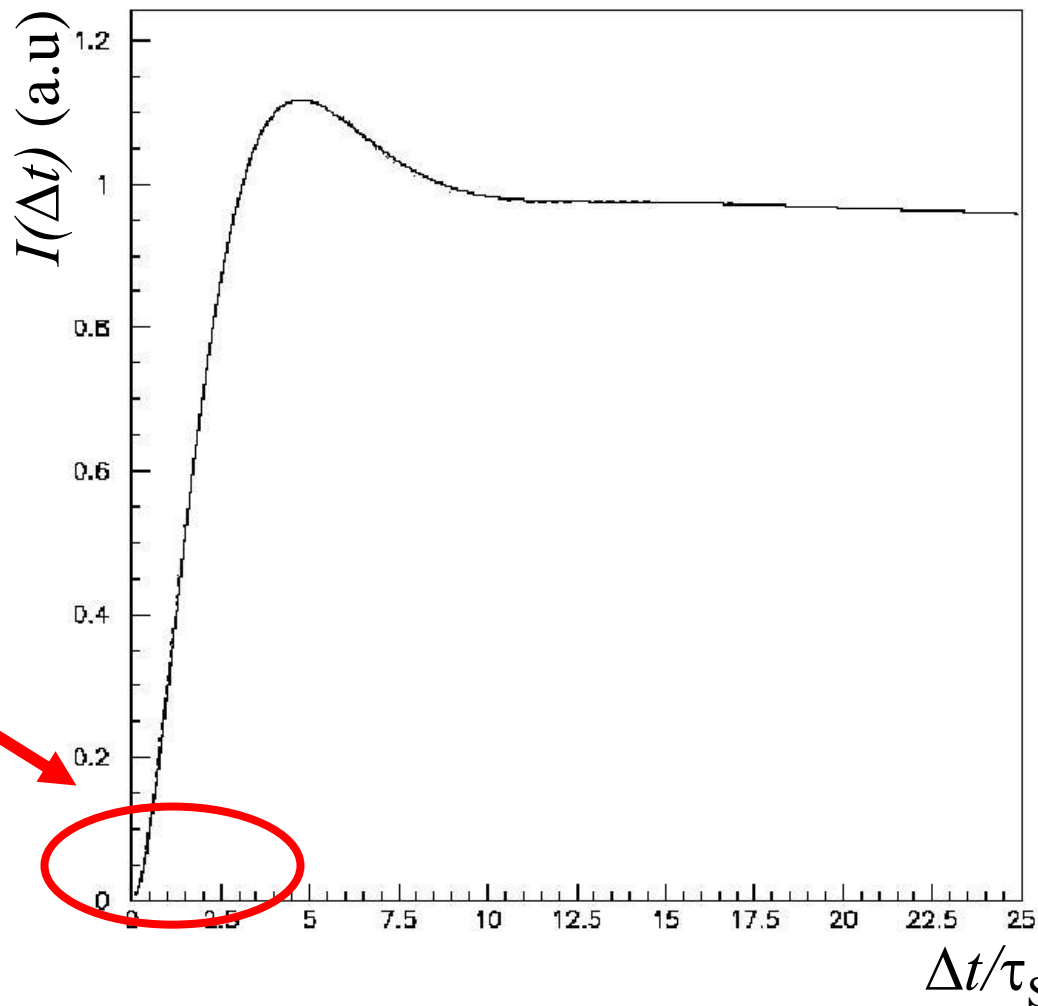
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# $\phi \rightarrow \mathbf{K}_S \mathbf{K}_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

$$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t) = \frac{N}{2} \left[ \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \right|^2 + \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle \right|^2 - 2 \Re \left( \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle^* \right) \right]$$



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Decoherence parameter:

$$\zeta_{0\bar{0}} = 0 \quad \rightarrow \quad \text{QM}$$

$$\zeta_{0\bar{0}} = 1 \quad \rightarrow \quad \text{total decoherence} \\ \text{(also known as Furry's hypothesis} \\ \text{or spontaneous factorization)} \\ \text{[W.Furry, PR 49 (1936) 393]}$$

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=380 \text{ pb}^{-1}$
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE result:** [PLB 642\(2006\) 315](#)

$$\zeta_{0\bar{0}} = (1.0 \pm 2.1_{\text{STAT}} \pm 0.4_{\text{SYST}}) \times 10^{-6}$$

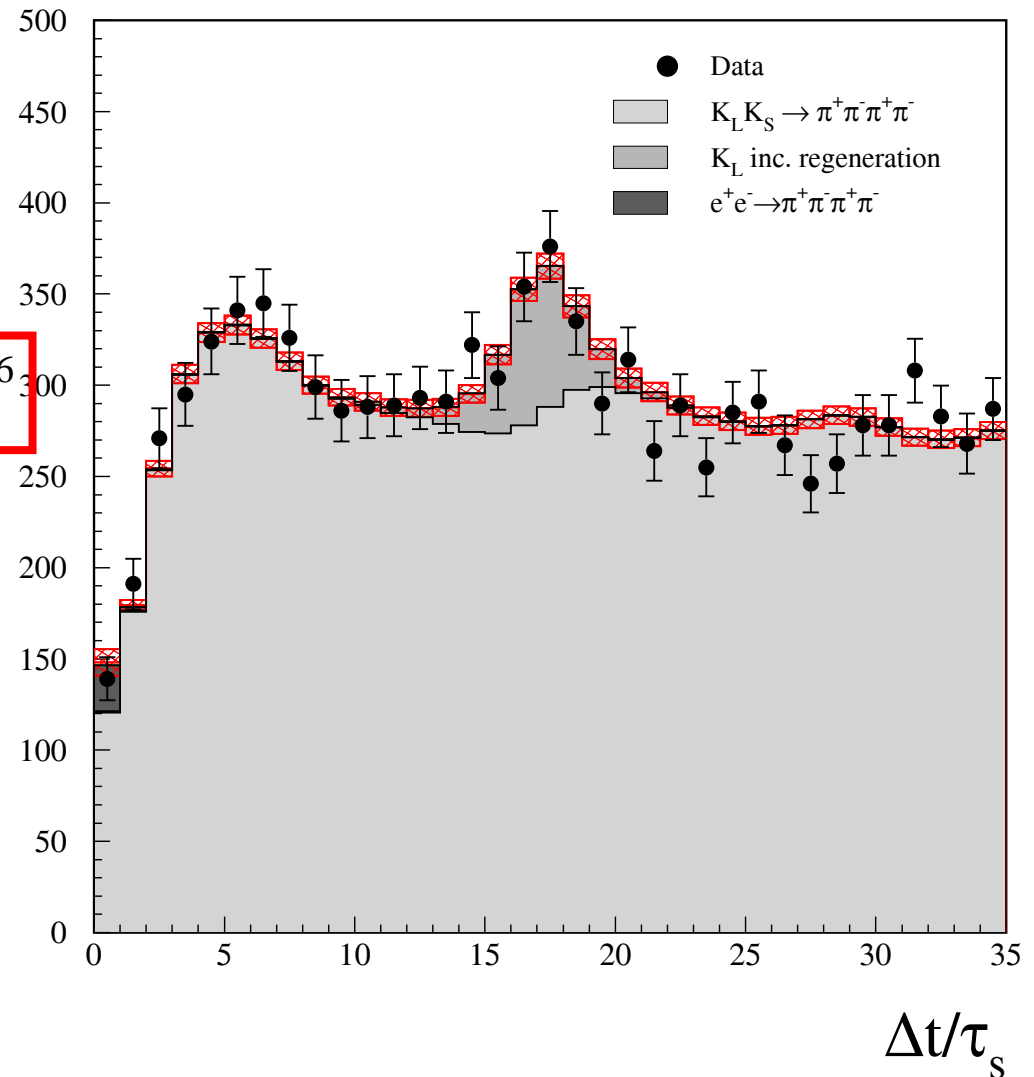
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



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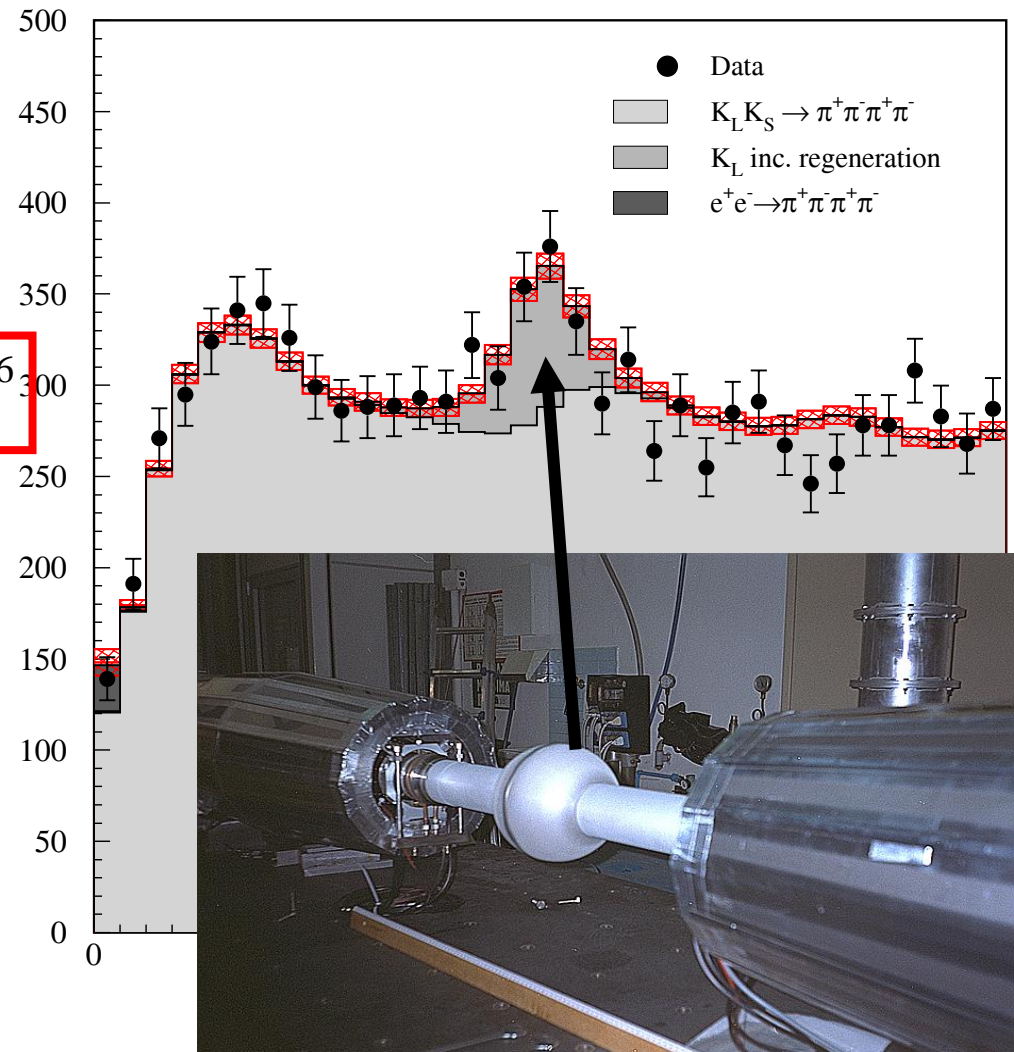
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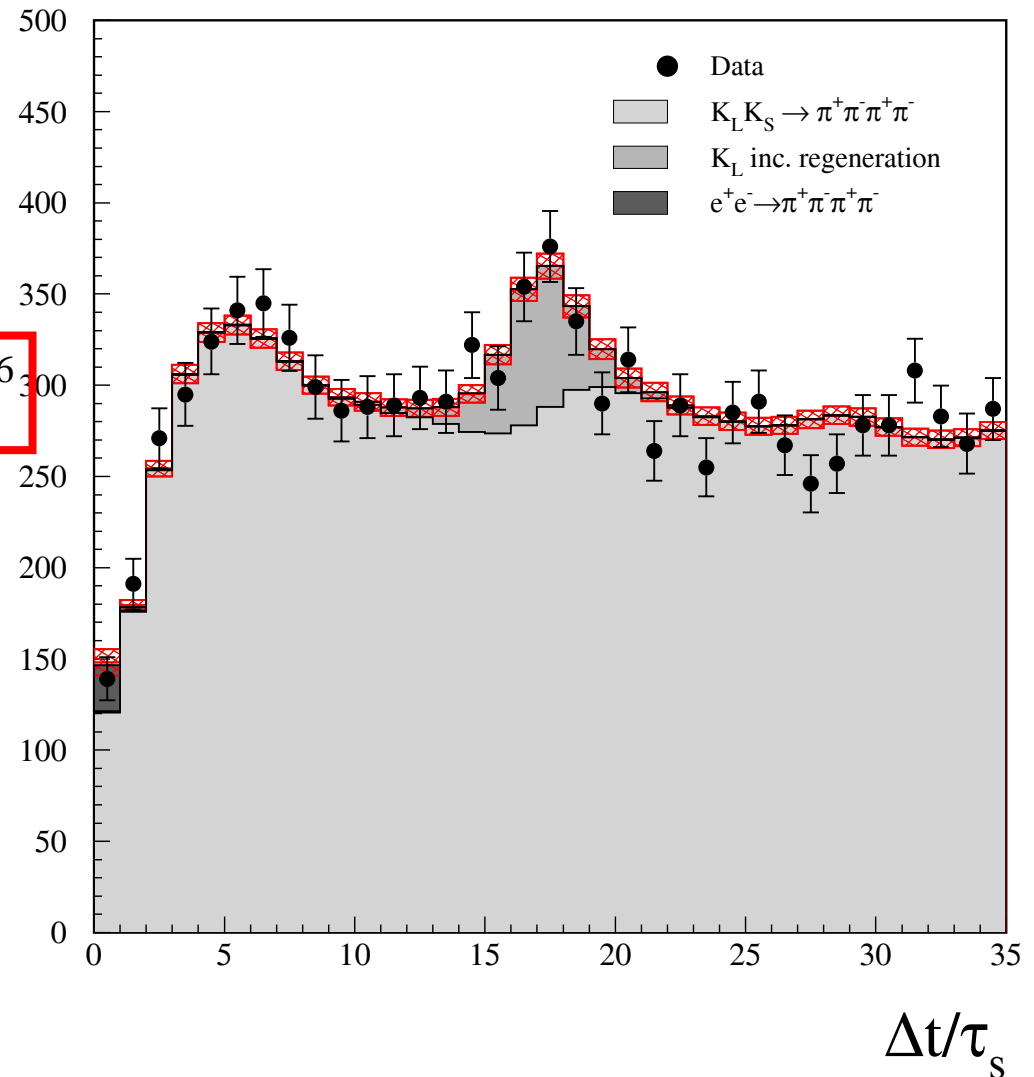
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- Analysed data:  $L=1 \text{ fb}^{-1}$  (2005 data)
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE preliminary:**

$$\zeta_{0\bar{0}} = (0.3 \pm 1.2_{\text{STAT}}) \times 10^{-6}$$

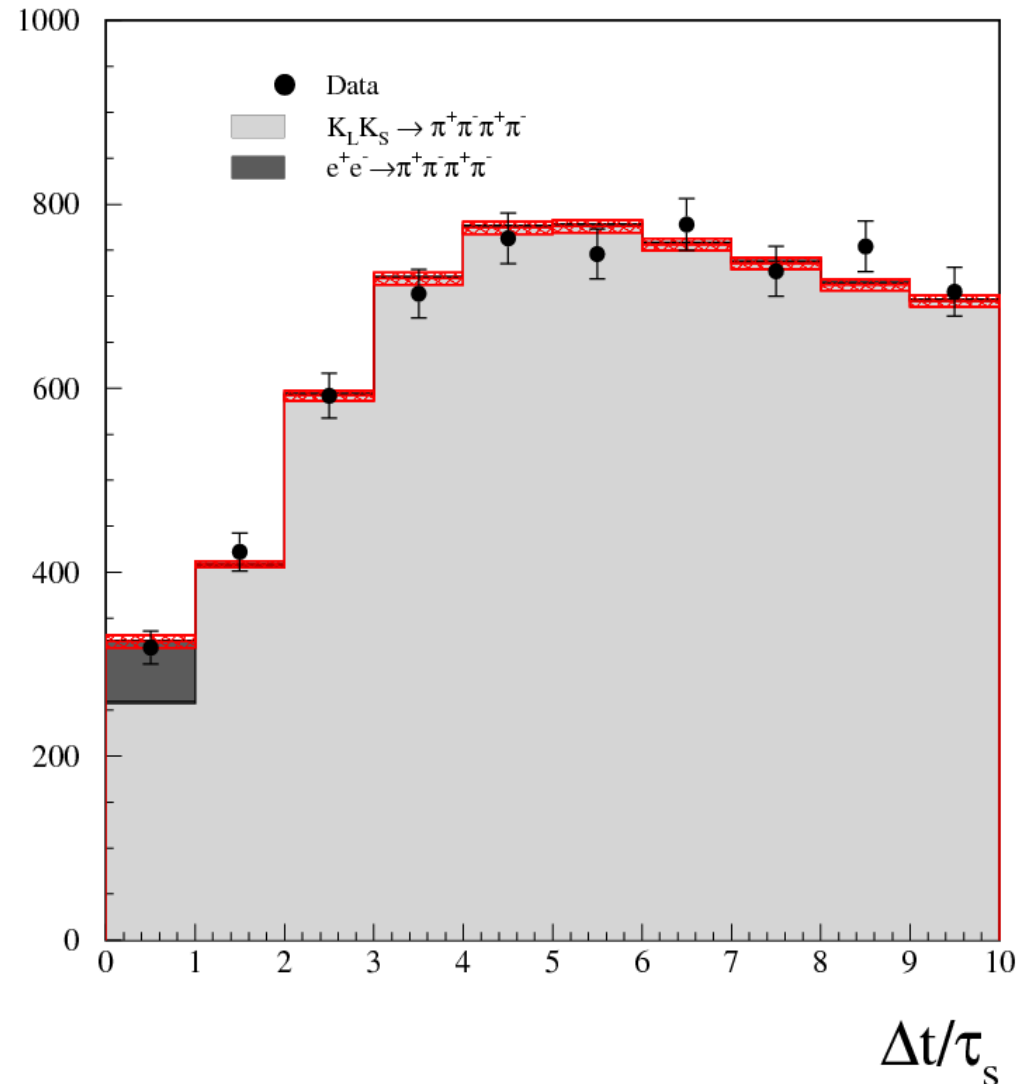
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=1 \text{ fb}^{-1}$  (2005 data)
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE preliminary:**

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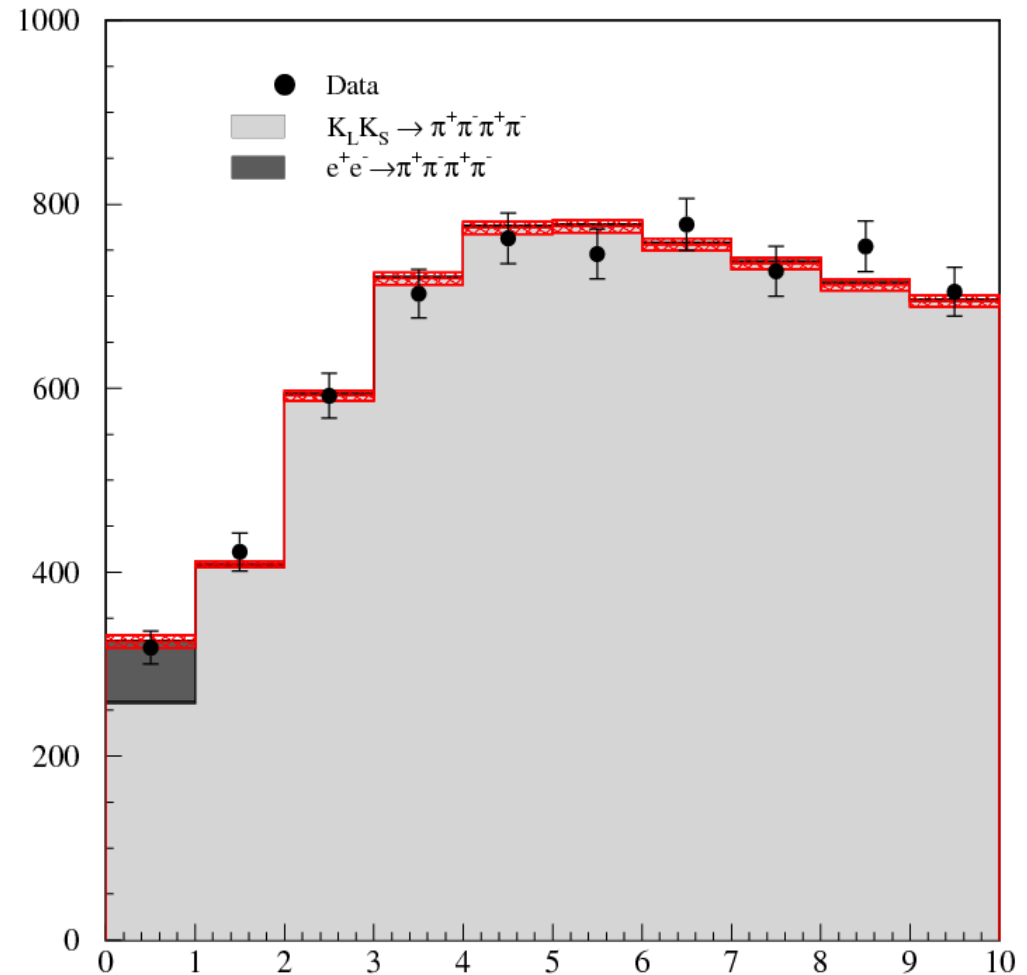
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Comparison with quantum optics test precisions

$\Delta t / \tau_S$



# Decoherence and CPT violation

Modified Liouville – von Neumann equation for the density matrix of the kaon system:

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H^\dagger}_{\text{QM}} + L(\rho)$$

← extra term inducing decoherence:  
pure state => mixed state



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← extra term inducing decoherence:  
pure state => mixed state

## Possible decoherence due quantum gravity effects:

**Black hole information loss paradox** => Possible decoherence near a black hole.

Hawking [1] suggested that at a microscopic level, in a quantum gravity picture, non-trivial space-time fluctuations (generically space-time foam) could give rise to decoherence effects, which would necessarily entail a violation of CPT [2].

J. Ellis et al.[3-6] => model of decoherence for neutral kaons => 3 new CPTV param.  $\alpha, \beta, \gamma$ :

$$L(\rho) = L(\rho; \alpha, \beta, \gamma)$$
$$\alpha, \gamma > 0, \quad \alpha\gamma > \beta^2$$

At most:  $\alpha, \beta, \gamma = O\left(\frac{M_K^2}{M_{\text{PLANCK}}}\right) \approx 2 \times 10^{-20} \text{ GeV}$

[1] Hawking, Comm.Math.Phys.87 (1982) 395; [2] Wald, PR D21 (1980) 2742; [3] Ellis et. al, NP B241 (1984) 381; PRD53 (1996)3846 [4] Huet, Peskin, NP B434 (1995) 3; [5] Benatti, Floreanini, NPB511 (1998) 550 [6] Bernabeu, Ellis, Mavromatos, Nanopoulos, Papavassiliou: Handbook on kaon interferometry [hep-ph/0607322]

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : decoherence & CPTV by QG

Study of time evolution of **single kaons**  
decaying in  $\pi^+ \pi^-$  and semileptonic final state

CPLEAR **PLB 364, 239 (1999)**

$$\alpha = (-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$$

$$\beta = (2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$$

$$\gamma = (1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$$

In the complete positivity hypothesis

$$\alpha = \gamma \quad , \quad \beta = 0$$

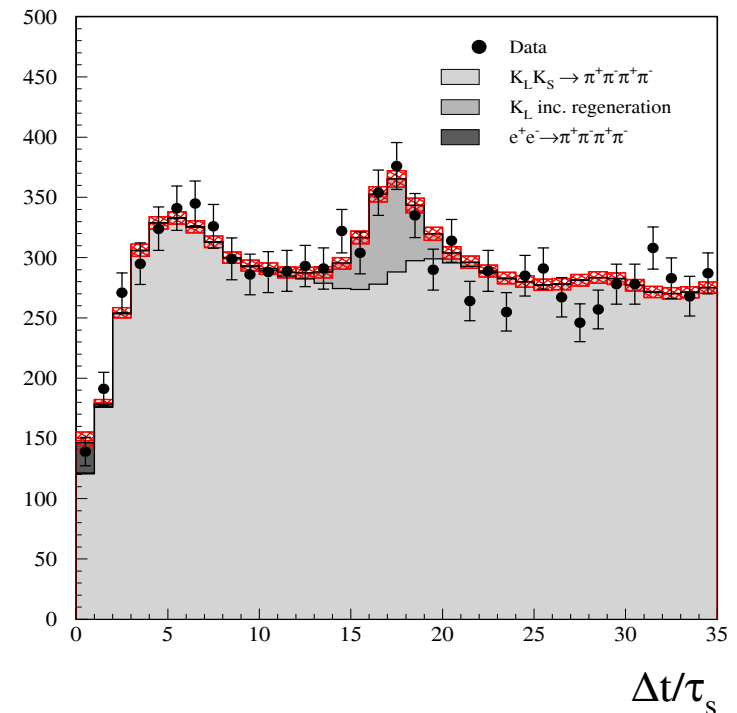
=> only one independent parameter:  $\gamma$

The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \gamma)$  gives:

**KLOE result**  $L=380 \text{ pb}^{-1}$  **PLB 642(2006) 315**

$$\gamma = \left( 1.1_{-2.4}^{+2.9} \text{STAT} \pm 0.4_{\text{SYST}} \right) \times 10^{-21} \text{ GeV}$$

Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.



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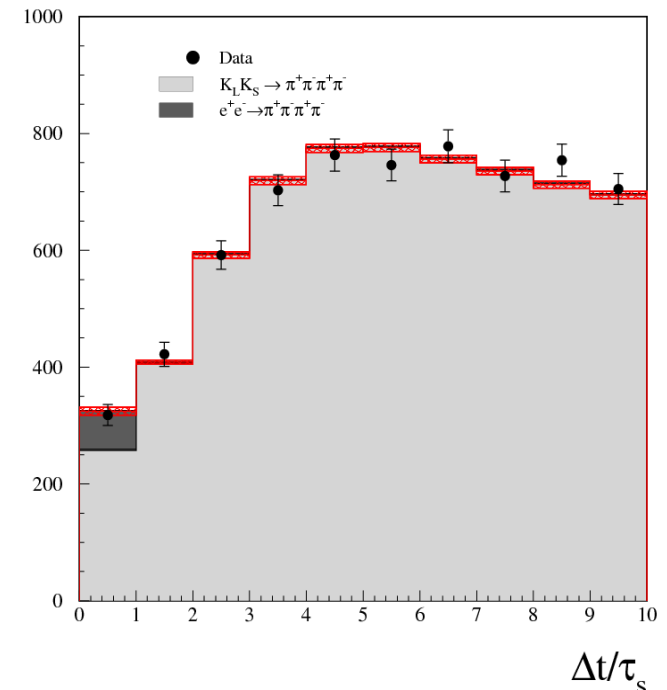
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The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \gamma)$  gives:

**KLOE preliminary**  $L = 1 \text{ fb}^{-1}$

$$\gamma = \left( 0.8^{+1.5}_{-1.3 \text{ STAT}} \right) \times 10^{-21} \text{ GeV}$$

Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^- : \text{CPT violation in correlated K states}$

In presence of decoherence and CPT violation induced by quantum gravity (CPT operator “ill-defined”) the definition of the particle-antiparticle states could be modified. This in turn could induce a breakdown of the correlations imposed by Bose statistics (EPR correlations) to the kaon state [Bernabeu, et al. PRL 92 (2004) 131601, NPB744 (2006) 180]:

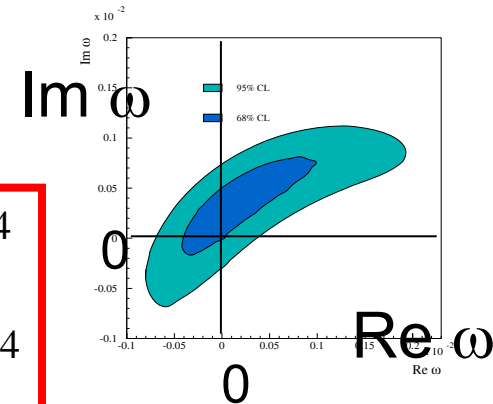
$$|i\rangle \propto (K^0 \bar{K}^0 - K^0 \bar{K}^0) + \omega (K^0 \bar{K}^0 + K^0 \bar{K}^0)$$

$|\omega|$  could be at most:  $|\omega|^2 = O\left(\frac{E^2/M_{PLANCK}}{\Delta\Gamma}\right) \approx 10^{-5} \Rightarrow |\omega| \sim 10^{-3}$

## KLOE result

Fit of  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \omega)$ :

**( $\omega$  measured for the first time)**



- Analysed data: 380 pb<sup>-1</sup>

$$\Re \omega = \left(1.1^{+8.7}_{-5.3 \text{ STAT}} \pm 0.9_{\text{SYST}}\right) \times 10^{-4}$$

$$\Im \omega = \left(3.4^{+4.8}_{-5.0 \text{ STAT}} \pm 0.6_{\text{SYST}}\right) \times 10^{-4}$$

$$|\omega| < 2.1 \times 10^{-3} \quad \text{at 95\% C.L.}$$

**KLOE result :**

**PLB 642(2006) 315**

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^- : \text{CPT violation in correlated K states}$

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## KLOE result

Fit of  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \omega)$ :

**( $\omega$  measured for the first time)**

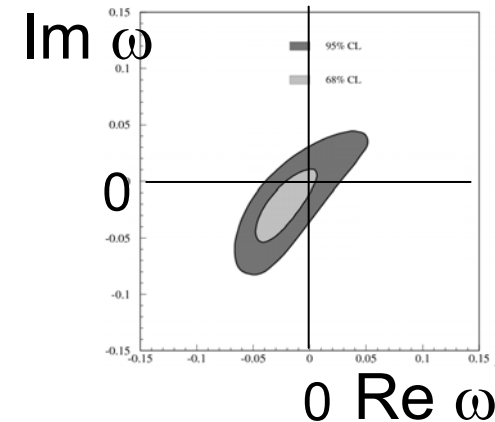
- Analysed data:  
1 fb<sup>-1</sup> (2005 data)

$$\Re \omega = \left( -2.5^{+3.1}_{-2.3 STAT} \right) \times 10^{-4}$$

$$\Im \omega = \left( -2.2^{+3.4}_{-3.1 STAT} \right) \times 10^{-4}$$

**KLOE preliminary :**

$$|\omega| < 0.98 \times 10^{-3} \text{ at 95\% C.L.}$$



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### **3) Tests of Lorentz invariance and CPT symmetry in the neutral kaon system**

# CPT and Lorentz invariance violation (SME)

Kostelecky et al. developed a phenomenological effective model providing a framework for CPT and Lorentz violations, based on spontaneous breaking of CPT and Lorentz symmetry, which might happen in quantum gravity (e.g. in some models of string theory)

**Standard Model Extension (SME)** [Kostelecky PRD61, 016002, PRD64, 076001]

## CPT violation in neutral kaons according to SME:

- CPTV only in mixing, not in decay (at first order)
- $\delta$  cannot be a constant (momentum dependence)

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K \left( \Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a} \right) / \Delta m$$

where  $\Delta a_\mu$  are four parameters associated to SME lagrangian terms and related to CPT and Lorentz violation.

# CPT and Lorentz invariance violation (SME)

$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K (\Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a}) / \Delta m$$

$\delta$  depends on sidereal time  $t$  since laboratory frame rotates with Earth.

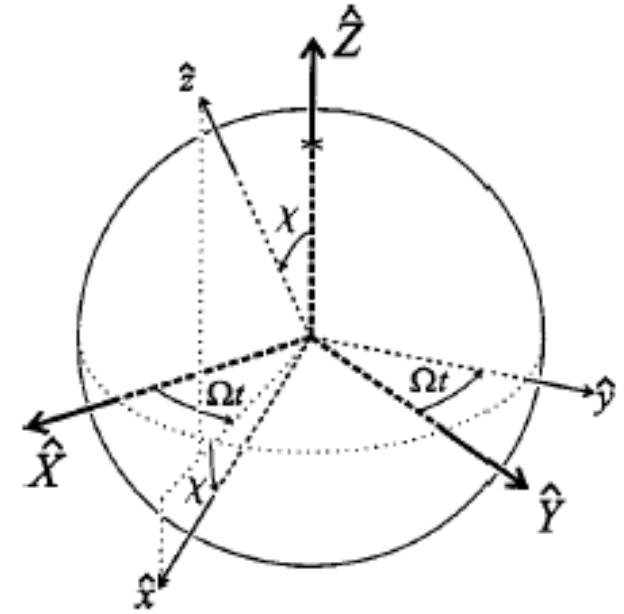
For a  $\phi$ -factory there is an additional dependence on the polar and azimuthal angle  $\theta, \phi$  of the kaon momentum in the laboratory frame:

$$\bar{\delta}(|\vec{p}|, \theta, t) = \frac{1}{2\pi} \int_0^{2\pi} \delta(\vec{p}, t) d\phi$$

$$= \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right.$$

$$+ \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t$$

$$\left. + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right]$$



(in general  $z$  lab. axis is non-normal to Earth's surface)

$\Omega$ : Earth's sidereal frequency  
 $\chi$ : angle between the  $z$  lab. axis and the Earth's rotation axis



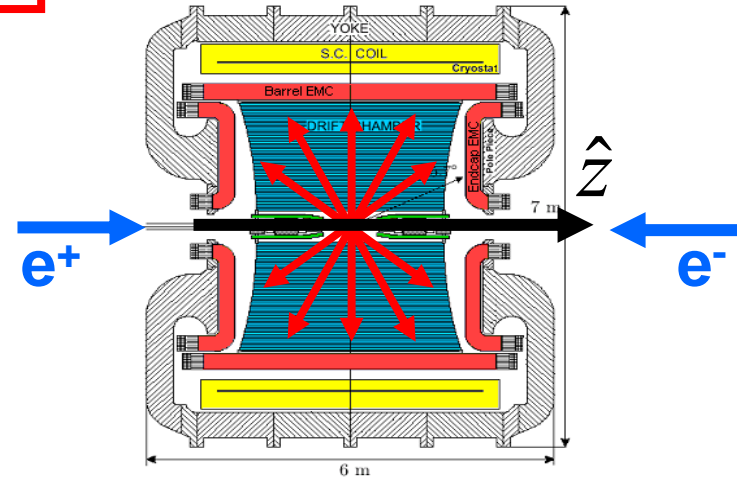
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For a  $\phi$ -factory there is an additional dependence on the polar and azimuthal angle  $\theta, \phi$  of the kaon momentum in the laboratory frame:

$$\begin{aligned} \bar{\delta}(|\vec{p}|, \theta, t) &= \frac{1}{2\pi} \int_0^{2\pi} \delta(\vec{p}, t) d\phi \\ &= \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right. \\ &\quad \left. + \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t \right. \\ &\quad \left. + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right] \end{aligned}$$



$\Omega$ : Earth's sidereal frequency  
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# Measurement of $\Delta a_\mu$ at KLOE

$\Delta a_0$  from  $K_{S,L}$  semileptonic asymmetries

$A_{S,L}$  (with symmetric polar angle  $\theta$  and sidereal time  $t$  integration)

$$A_S - A_L \cong \frac{4\Re(i \sin\phi_{SW} e^{i\phi_{SW}}) \gamma_K}{\Delta m} \Delta a_0$$

with  $L=400 \text{ pb}^{-1}$  (preliminary):

$$\Delta a_0 = (0.4 \pm 1.8) \times 10^{-17} \text{ GeV}$$

with  $L=2.5 \text{ fb}^{-1}$  :  $\sigma(\Delta a_0) \sim 7 \times 10^{-18} \text{ GeV}$  ( $\Delta a_0$  evaluated for the first time)

$\Delta a_{x,y,z}$  from  $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$   
(analysis vs polar angle  $\theta$  and sidereal time  $t$ )

Fit to:  $I[\pi^+ \pi^- (\cos\theta > 0), \pi^+ \pi^- (\cos\theta < 0); \Delta t]$

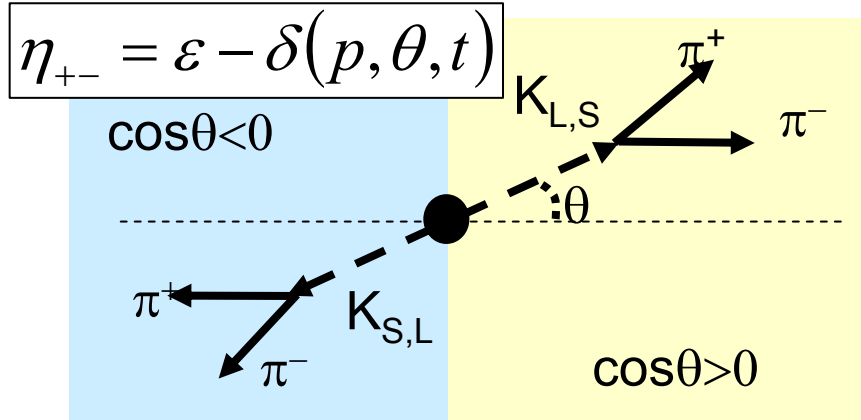
• at  $\Delta t \sim \tau_s$  sensitive to  $\text{Im}(\delta/\epsilon)$

With  $L=1 \text{ fb}^{-1}$  (preliminary):

$$\Delta a_X = (-6.3 \pm 6.0) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Y = (2.8 \pm 5.9) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Z = (2.4 \pm 9.7) \times 10^{-18} \text{ GeV}$$



KTeV :  $\Delta a_X, \Delta a_Y < 9.2 \times 10^{-22} \text{ GeV}$  @ 90% CL

BABAR  $\Delta a_{x,y}^B, (\Delta a_0^B - 0.30 \Delta a_Z^B) \sim \mathcal{O}(10^{-13} \text{ GeV})$   
[PRL 100 (2008) 131802]

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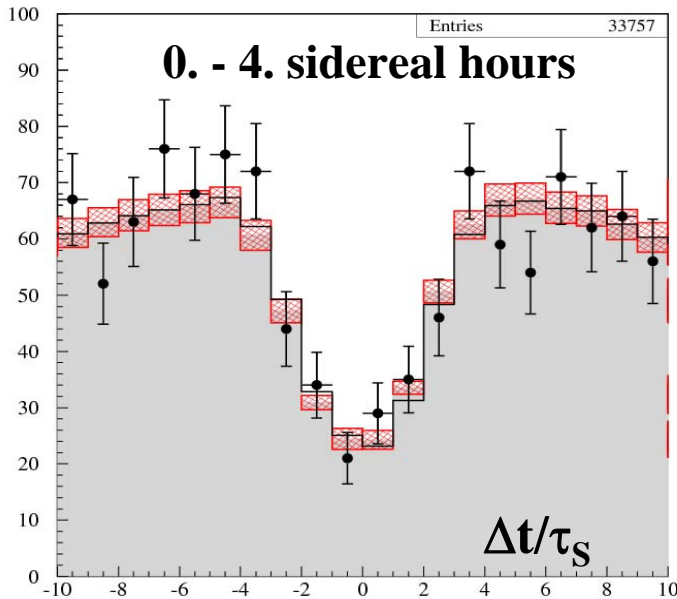
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[PRL 100 (2008) 131802]

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## 4) Future plans

### Proposals to upgrade DAΦNE in luminosity (and energy):

Crabbed waist scheme at DAΦNE (proposal by P. Raimondi)

- increase L by a factor  $O(5)$
- requires minor modifications
- relatively low cost
- Experimental test at DAΦNE in progress

### KLOE-2 Proposal:

- phase 0: KLOE should restart taking data mid 2009 with a minimal upgrade
- phase 1: full KLOE upgrade (KLOE-2) 2011 (?)

### Physics issues:

- Neutral kaon interferometry, CPT symmetry & QM tests
- Kaon physics, CKM, LFV, rare  $K_S$  decays
- $\eta, \eta'$  physics
- Light scalars,  $\gamma\gamma$  physics
- Hadron cross section at low energy, muon anomaly
- (baryon electromagnetic form factors,  $e^+e^- \rightarrow pp, nn, \Lambda\Lambda$ )

### Detector upgrade issues:

- Inner tracker R&D
- $\gamma\gamma$  tagging system
- Calorimeter, increase of granularity
- FEE maintenance and upgrade
- Computing and networking update
- etc.. (Trigger, software, ...)

# Perspectives with KLOE-2 at upgraded DAΦNE

| Mode                        | Test of | Param.                                | Present best published measurement   | KLOE-2<br>L=50 fb <sup>-1</sup>       |
|-----------------------------|---------|---------------------------------------|--|---------------------------------------|
| $K_S \rightarrow \pi e \nu$ | CP, CPT | $A_S$                                 | $(1.5 \pm 11) \times 10^{-3}$  | $\pm 1 \times 10^{-3}$                |
| $\pi^+ \pi^- \pi e \nu$     | CP, CPT | $A_L$                                 | $(3322 \pm 58 \pm 47) \times 10^{-6}$  | $\pm 25 \times 10^{-6}$               |
| $\pi^+ \pi^- \pi^0 \pi^0$   | CP      | $\text{Re}(\varepsilon'/\varepsilon)$ | $(1.65 \pm 0.26) \times 10^{-3}$ (*)   | $\pm 0.2 \times 10^{-3}$              |
| $\pi^+ \pi^- \pi^0 \pi^0$   | CP, CPT | $\text{Im}(\varepsilon'/\varepsilon)$ | $(-1.2 \pm 2.3) \times 10^{-3}$ (*)  | $\pm 3 \times 10^{-3}$                |
| $\pi e \nu \pi e \nu$       | CPT     | $\text{Re}(\delta) + \text{Re}(x_-)$  | $\text{Re}(\delta) = (0.25 \pm 0.23) \times 10^{-3}$ (*)<br>$\text{Re}(x_-) = (-4.2 \pm 1.7) \times 10^{-3}$ (*) | $\pm 0.2 \times 10^{-3}$              |
| $\pi e \nu \pi e \nu$       | CPT     | $\text{Im}(\delta) + \text{Im}(x_+)$  | $\text{Im}(\delta) = (-0.6 \pm 1.9) \times 10^{-5}$ (*)<br>$\text{Im}(x_+) = (0.2 \pm 2.2) \times 10^{-3}$ (*)   | $\pm 3 \times 10^{-3}$                |
| $\pi^+ \pi^- \pi^+ \pi^-$   |         | $\Delta m$                            | $(5.288 \pm 0.043) \times 10^9 \text{ s}^{-1}$   | $\pm 0.03 \times 10^9 \text{ s}^{-1}$ |

(\*) = PDG 2008 fit

# Perspectives with KLOE-2 at upgraded DAΦNE

| Mode                            | Test of         | Param.           | Present best published measurement            | KLOE-2<br>L=50 fb <sup>-1</sup>  |
|---------------------------------|-----------------|------------------|---|--|
| $\pi^+\pi^- \quad \pi^+\pi^-$   | QM              | $\zeta_{00}$     | $(1.0 \pm 2.1) \times 10^{-6}$                | $\pm 0.1 \times 10^{-6}$   |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | QM              | $\zeta_{SL}$     | $(1.8 \pm 4.1) \times 10^{-2}$                | $\pm 0.2 \times 10^{-2}$   |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | CPT & QM        | $\alpha$         | $(-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$  | $\pm 2 \times 10^{-17} \text{ GeV}$  |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | CPT & QM        | $\beta$          | $(2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$   | $\pm 0.1 \times 10^{-19} \text{ GeV}$  |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | CPT & QM        | $\gamma$         | $(1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$   | $\pm 0.2 \times 10^{-21} \text{ GeV}$<br>compl. pos. hyp.<br>$\pm 0.1 \times 10^{-21} \text{ GeV}$ |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | CPT & EPR corr. | Re( $\omega$ )   | $(1.1 \pm 7.0) \times 10^{-4}$                | $\pm 2 \times 10^{-5}$   |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | CPT & EPR corr. | Im( $\omega$ )   | $(3.4 \pm 4.9) \times 10^{-4}$                | $\pm 2 \times 10^{-5}$   |
| $K_{S,L} \rightarrow \pi e \nu$ | CPT & Lorentz   | $\Delta a_0$     | $[(0.4 \pm 1.8) \times 10^{-17} \text{ GeV}]$ | $\pm 2 \times 10^{-18} \text{ GeV}$  |
| $\pi^+\pi^- \quad \pi^+\pi^-$   | CPT & Lorentz   | $\Delta a_Z$     | $[(2.4 \pm 9.7) \times 10^{-18} \text{ GeV}]$ | $\pm 7 \times 10^{-19} \text{ GeV}$  |
| $\pi^+\pi^- \quad \pi e \nu$    | CPT & Lorentz   | $\Delta a_{X,Y}$ | $[<10^{-21} \text{ GeV}]$                     | $\pm 4 \times 10^{-19} \text{ GeV}$  |

[...] = preliminary

# Conclusions

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- The neutral kaon system is an excellent laboratory for the study of CPT symmetry and the basic principles of Quantum Mechanics;
- Several parameters related to possible
  - CPT violation (within QM)
  - CPT violation and decoherence
  - CPT violation and Lorentz symmetry breakinghave been measured at KLOE, in some cases with a precision reaching the interesting Planck's scale region;
- All results are consistent with no CPT violation
  
- The analysis of the full KLOE data sample ( $2.5 \text{ fb}^{-1}$ ) is in being completed;
- KLOE and DAΦNE are going to be upgraded;
- Neutral kaon interferometry, CPT symmetry and QM tests are one of the main issues of the KLOE-2 physics program



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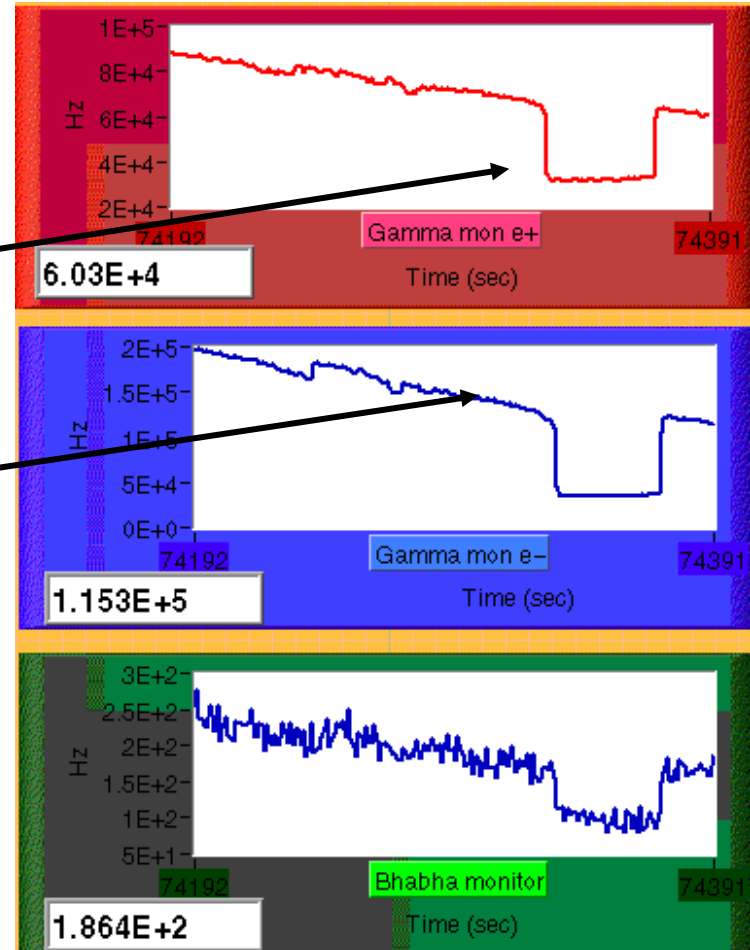
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**Spare**

# EFFECTS OF CRAB SEXTUPOLES ON LUMINOSITY

A huge work on machine optimization has been done and is still in progress in term of feedbacks systems tuning, background minimization and tuning of the machine luminosity...

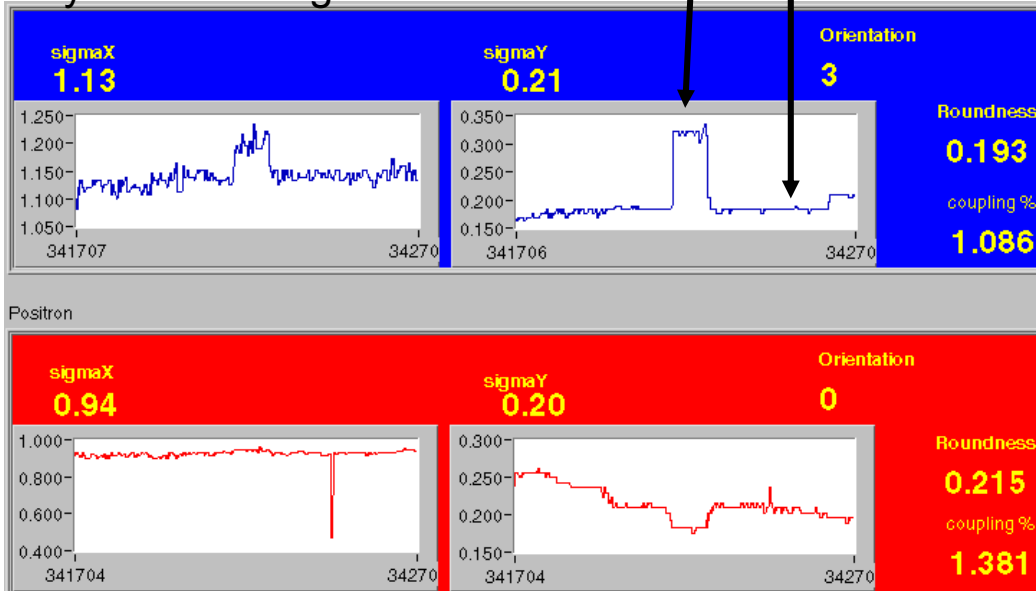
## LUMINOMETERS



Crab off

Crab on

Transverse beam dimensions at the Synchrotron Light Monitor



*P. Raimondi May 6, 2008*