



# KLOE results on the pseudoscalar mixing angle and the $\eta'$ gluonium content

**Biagio Di Micco**  
(for the KLOE collaboration)

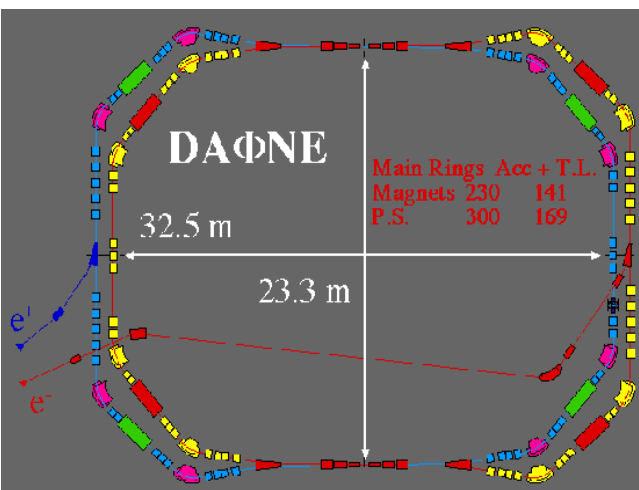
**I.N.F.N**  
sezione di  
**Roma Tre**



**Università**  
degli Studi di  
**Roma Tre**



# The DAΦNE machine and the KLOE detector



- $\sigma(e^+e^- \rightarrow \phi) \sim 3 \mu\text{b}$
- Independent  $e^+e^-$  rings to reduce beam-beam interactions
- crossing angle: 25 mrad,  $p_x(\phi) \sim 12,6 \text{ MeV}/c$
- Bunch crossing every 2.7 ns
- injection during acquisition

$$\sqrt{s} = m(\phi) = 1019.4 \text{ MeV}$$

$$\int \mathcal{L} dt = 2.5 \text{ fb}^{-1}$$

$$\mathcal{L}_{\text{peak}} = 1.5 \times 10^{32} \text{ cm}^2 \text{ s}^{-1}$$

## Electromagnetic Calorimeter (EMC)

- Fine sampling Pb / Scifi
- Hermetical coverage
- High efficiency for low energy photons

$$\sigma_E/E = 5.7\%/\sqrt{E(\text{GeV})}$$

$$\sigma_t = 54 \text{ ps}/\sqrt{E(\text{GeV})} \oplus 140 \text{ ps}$$

## Central drift chamber (DCH)

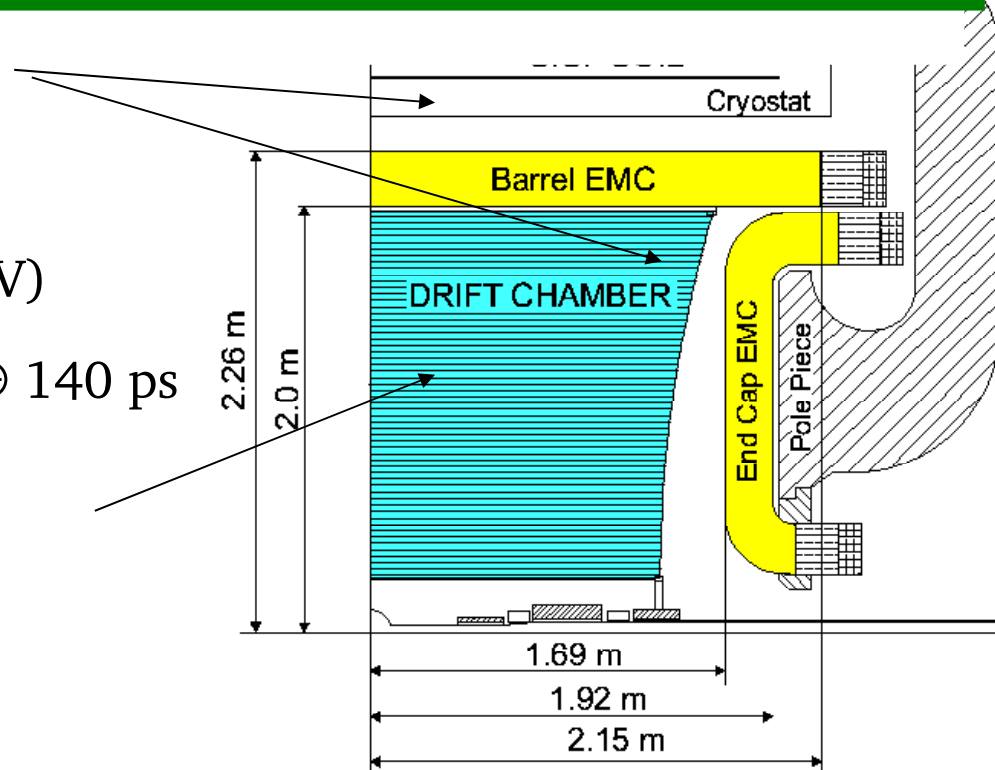
Helium based gas mixture

$$\sigma_r = 1 \text{ mm}$$

$$\sigma_{pt}/p_t = 0.5\%$$

$$\sigma_{r,\phi} = 200 \mu\text{m}$$

$$\sigma_z = 2 \text{ mm}$$

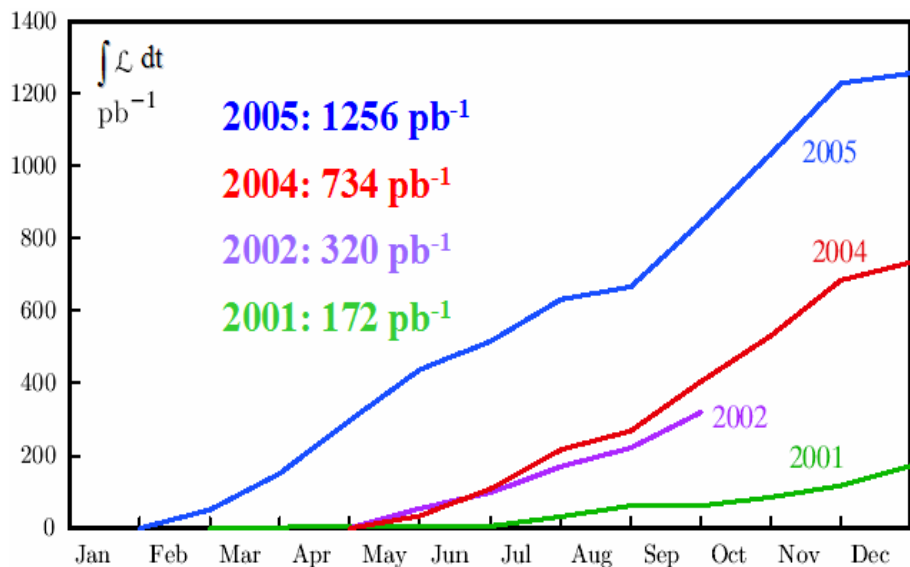




# DAΦNE: the meson factory

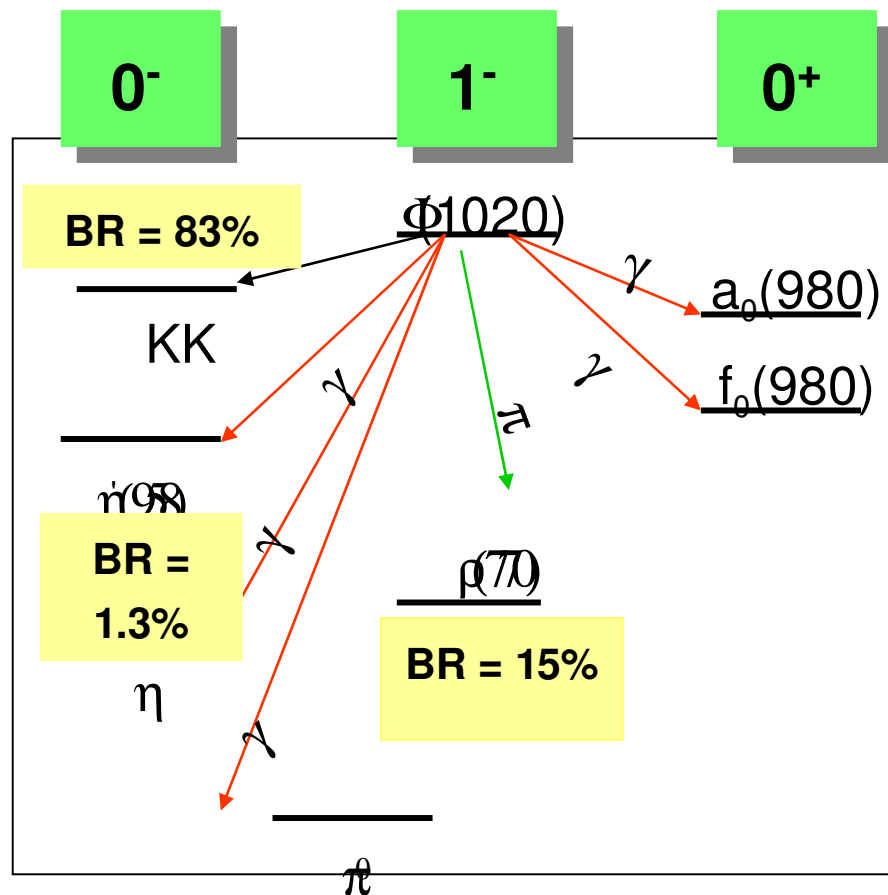
## Acquired data

### 2001-2006 data taking



**2.5 fb<sup>-1</sup> on tape @  $\sqrt{s}=M_\phi$**

**$\approx 8 \times 10^9 \phi$      $1 \times 10^8 \eta$     500.000  $\eta'$  produced**



**250 pb<sup>-1</sup> @  $\sqrt{s}=1000$  MeV + 4 scan points around the  $\phi$**



# $\text{Br}(\phi \rightarrow \eta' \gamma) / \text{Br}(\phi \rightarrow \eta \gamma)$

427 pb<sup>-1</sup> ('01-'02 data)

$N(\eta \gamma) = 1.665 \times 10^6$  (no bck)

$N(\pi^+ \pi^- \gamma \gamma) = 3750 \pm 60$  ( $N_{\text{bckg}} = 345$ )

$N(\eta' \gamma) = 3405 \pm 61_{\text{stat}} \pm 43_{\text{syst}}$

## Decay channel topology

$\eta' \rightarrow \pi^+ \pi^- \eta, \eta \rightarrow 3\pi^0$

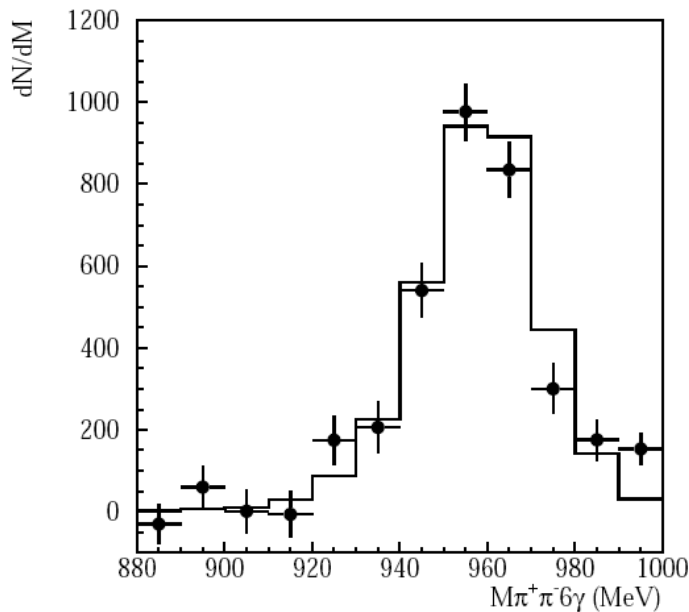
$\eta' \rightarrow \pi^0 \pi^0 \eta, \eta \rightarrow \pi^+ \pi^- \pi^0$

$$R_\phi = (4.77 \pm 0.09_{\text{stat.}} \pm 0.19_{\text{syst.}}) \times 10^{-3}$$

Dominated by the  $\eta'$  Br uncertainty

Using PDG  $\text{BR}(\phi \rightarrow \eta \gamma)$

$$\text{Br}(\phi \rightarrow \eta' \gamma) = (6.20 \pm 0.09_{\text{stat.}} \pm 0.25_{\text{syst.}}) \times 10^{-5}$$



In perfect agreement with previous KLOE result Phys. Lett. B541 (2002)

$\eta' \rightarrow \pi^+ \pi^- \eta, \eta \rightarrow \gamma \gamma$  ( $\sim 20 \text{ pb}^{-1}$ )

$$R = (4.70 \pm 0.47_{\text{stat}} \pm 0.31_{\text{syst}}) \cdot 10^{-3}$$

$$\text{BR}(\phi \rightarrow \eta' \gamma) = (6.10 \pm 0.61 \pm 0.43) \cdot 10^{-5}$$



# $\eta, \eta'$ : mixing and gluonium

The  $\eta, \eta'$  mesons wave function can be decomposed in the quark mixing base as in the following (J. L. Rosner, Phys. Rev. D 27 (1983) 1101. ).

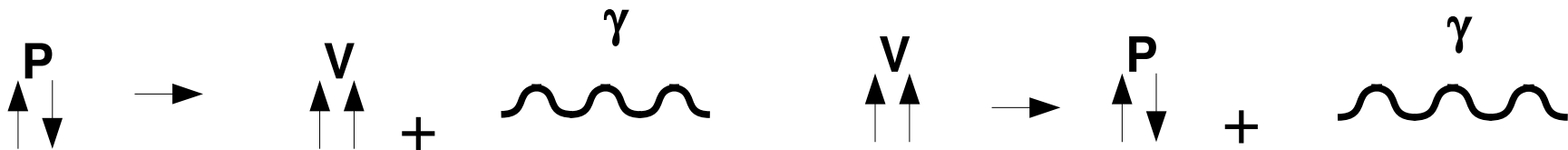
$$|\eta'\rangle = X_{\eta'} |q\bar{q}\rangle + Y_{\eta'} |s\bar{s}\rangle + Z_{\eta'} |G\rangle \quad |\eta\rangle = \cos\varphi_P |q\bar{q}\rangle - \sin\varphi_P |s\bar{s}\rangle \quad |q\bar{q}\rangle = \frac{|u\bar{u}\rangle + |d\bar{d}\rangle}{\sqrt{2}}$$

$$X_{\eta'} = \sin\varphi_P \cos\varphi_G$$

$$Y_{\eta'} = \cos\varphi_P \cos\varphi_G$$

$$Z_{\eta'} = \sin\varphi_G$$

The  $\phi \rightarrow \eta, \eta' \gamma$  transition is modelled according a spin flip transition



$$\Gamma(P \rightarrow V \gamma) = \frac{g^2}{4\pi} |p_y|^3$$

$$\Gamma(V \rightarrow P \gamma) = \frac{1}{3} \frac{g^2}{4\pi} |p_y|^3$$

Only quarks participate to the electromagnetic transition, gluonium is spectator.

It appears in the  $\eta'$  decay amplitudes only through the normalisation to 1 ( $Y_{\eta'} \sim \cos\varphi_G$ )



# V P $\gamma$ and P $\gamma\gamma$ transitions

**KLOE [Phys. Lett. B648 (2007) 267] has fitted:**

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos^2 \phi_V} \cdot 3 \left( \frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}$$

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left( \frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[ z_q X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \cdot \tan \phi_V \cdot Y_{\eta'} \right]^2$$

together with the measured branching ratio:

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3} \quad \sim 4000 \quad \phi \rightarrow \eta \gamma$$

$$\sim 1.7 \times 10^6 \quad \eta \rightarrow \pi \pi, \eta \rightarrow 3\pi$$

$$\eta \rightarrow \pi \pi, \eta \rightarrow \pi \pi \pi$$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left( 1 - \frac{m_s}{\bar{m}} \frac{z_q}{z_s} \cdot \frac{\tan \phi_V}{\sin 2\phi_P} \right)^2 \cdot \left( \frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio:  $\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left( \frac{m_{\eta'}}{m_\pi} \right)^3 \left( 5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$  E. Kou, Phys. Rev. D 63 (2001) 54027



# V P $\gamma$ and P $\gamma\gamma$ transitions

**KLOE [Phys. Lett. B648 (2007) 267] has fitted:**

Were taken from a global fit without gluonium:

A. Bramon, R. Escribano,  
M.D. Scadron  
Phys. Lett. B503 (2001) 271

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos \phi_V} \cdot 3 \left( \frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}$$

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left( \frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[ z_q^2 X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \tan \phi_V X_{\eta'} \right]^2$$

together with the measured branching ratio:

$\phi \rightarrow \eta \gamma$

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3} \quad \sim 4000 \quad \eta \rightarrow \pi \pi, \eta \rightarrow 3\pi$$

$$\sim 1.7 \times 10^6 \quad \eta \rightarrow \pi \pi, \eta \rightarrow \pi \pi \pi$$

$\phi \rightarrow \eta \gamma, \eta \rightarrow 3\pi$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left( 1 - \frac{m}{\bar{m}} \frac{z_q}{z_s} \frac{\tan \phi_V}{\sin 2 \phi_P} \right)^2 \cdot \left( \frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio:  $\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left( \frac{m_{\eta'}}{m_\pi} \right)^3 \left( 5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$  E. Kou, Phys. Rev. D 63 (2001) 54027



# V P $\gamma$ and P $\gamma\gamma$ transitions

**KLOE [Phys. Lett. B648 (2007) 267] has fitted:**

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos^2 \phi_V} \cdot 3 \left( \frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}$$

T. Feldmann, Int. J. Mod. Phys. A 15 (2000) 159

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left( \frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[ z_q X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \cdot \tan \phi_V \cdot Y_{\eta'} \right]^2$$

together with the measured branching ratio:

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3} \quad \sim 4000 \quad \eta \rightarrow \pi\pi, \eta \rightarrow \pi\pi\pi$$

$$\sim 1.7 \times 10^6 \quad \eta \rightarrow \pi\pi, \eta \rightarrow \pi\pi\pi$$

$\phi \rightarrow \gamma\gamma$

$\phi \rightarrow \eta \rightarrow \pi\pi$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left( 1 - \frac{m_s}{\bar{m}} \frac{z_q}{z_s} \cdot \frac{\tan \phi_V}{\sin 2\phi_P} \right)^2 \cdot \left( \frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio:

$$\frac{\Gamma(\eta' \rightarrow \gamma\gamma)}{\Gamma(\pi^0 \rightarrow \gamma\gamma)} = \frac{1}{9} \left( \frac{m_{\eta'}}{m_\pi} \right)^3 \left( 5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$$

E. Kou, Phys. Rev. D 63 (2001) 54027





# Fit result

Fit results:

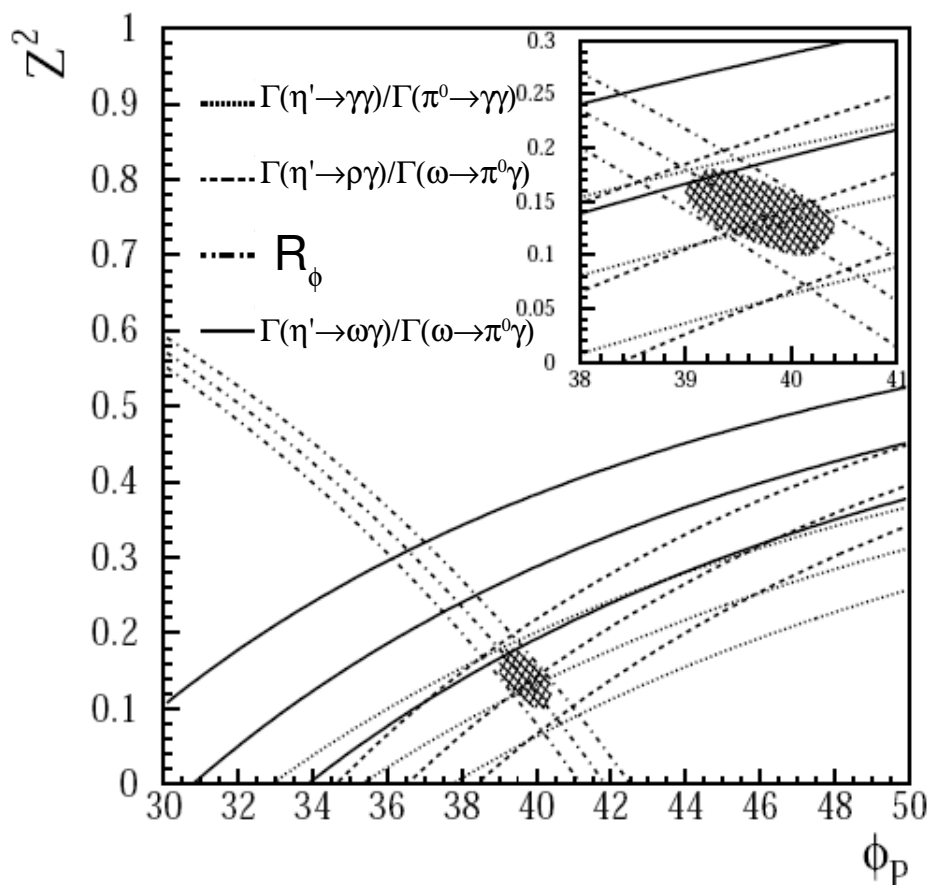
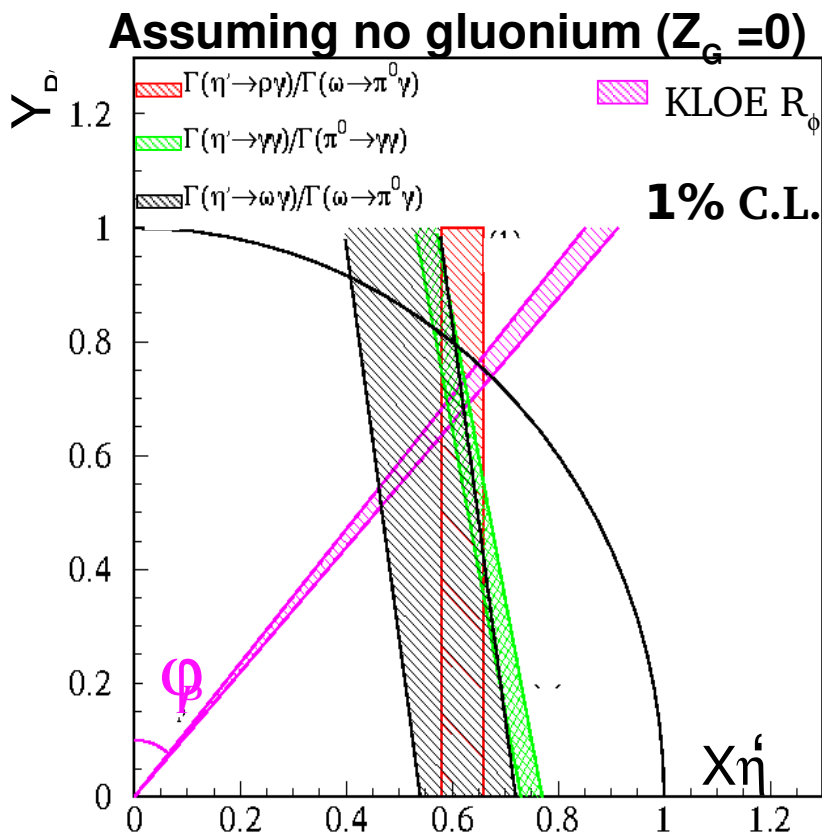
$$\phi_P = (39.7 \pm 0.7_{\text{tot}})^\circ$$

$$|\phi_G| = (22 \pm 3)^\circ$$

$$\sin^2 \phi_G = Z^2 = 0.14 \pm 0.04$$

**Glunium at  $3\sigma$**

**49% C.L.**





# Objections...

In Escribano et al. (JHEP 0705:006,2007)  
different conclusions were found:

**KLOE**  
(Phys. Lett. B648 (2007) 267)

$$\phi_P = (39.7 \pm 0.7_{\text{tot}})^\circ$$

$$|\phi_G| = (22 \pm 3)^\circ$$

$$\sin^2\phi_G = Z^2 = 0.14 \pm 0.04$$

**Escribano**  
(JHEP 0705:006,2007)

$$\phi_P = (41.4 \pm 1.3)^\circ$$

$$|\phi_G| = (12 \pm 13)^\circ$$

$$\sin^2\phi_G = Z^2 = 0.04 \pm 0.09$$

**The difference was attributed to the choice to fix the  $z_q$   
and  $z_s$  parameter from a fit without gluonium.**

**Slightly different fit:**

- 1) All theoretical parameters are left free;
- 2) Use of the couplings instead of the  $\Gamma$  ratios;
- 3)  $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$  is not used in the fit.



# To answer the objections.

- 1) Leave the z's parameter free;
- 2) Add more constraints (needed to perform the fit with larger number of parameters);
- 3) Check the contribution from  $\eta' \rightarrow \gamma\gamma$  /  $\pi^0 \rightarrow \gamma\gamma$

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[ z_q \cos(\phi_p) - 2 \frac{m_s}{\bar{m}} z_s \tan(\phi_v) \sin(\phi_p) \right]^2 (1 - z_G^2) \left( \frac{m_\omega^2 - m_\eta^2}{m_\omega^2 - m_{\pi^0}^2} \right)^3$$

$$\frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = z_q^2 \frac{\cos^2(\phi_p)}{\cos^2(\phi_v)} \left( \frac{m_\rho^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\rho} \right)^3$$

$$\frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[ z_q \tan(\phi_v) \cos(\phi_p) + 2 \frac{\bar{m}}{m_s} z_s \sin(\phi_p) \right]^2 \left( \frac{m_\phi^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\phi} \right)^3$$

$$\frac{\Gamma(\phi \rightarrow \pi^0 \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \tan^2 \phi_v \cdot \left( \frac{m_\phi^2 - m_{\pi^0}^2}{m_\omega^2 - m_{\pi^0}^2} \cdot \frac{m_\omega}{m_\phi} \right)^3, \quad \frac{\Gamma(K^{*+} \rightarrow K^+ \gamma)}{\Gamma(K^{*0} \rightarrow K^0 \gamma)} = \left( \frac{2 \frac{m_s}{\bar{m}} - 1}{1 + \frac{m_s}{\bar{m}}} \right)^2 \cdot \left( \frac{m_{K^{*+}}^2 - m_{K^0}^2}{m_{K^{*0}}^2 - m_{K^0}^2} \cdot \frac{m_{K^0}}{m_{K^{*+}}} \right)^3$$



# Fit procedure.

The  $\chi^2$  is defined as follows:

$$\chi^2 = \sum_{i,j=1,3} (y_i - y_i^{th}) \times V_{ij}^{-1} (y_j - y_j^{th})$$

$V_{ij}$  is the error matrix which is a function of theoretical uncertainties, as well as the experimental

$$V_{ij} = [B_{ij} + (A_{ik} \times C_{kl} \times A_{lj}^T)]$$

Experimental  
covariance matrix

Theoretical parameters  
covariance matrix

$B_{ij}$  Full covariance matrix  
(correlation comes  
from the constrained  
fit to  $\eta'$  Br)

$$; A_{ik} = \begin{pmatrix} \frac{\partial y_1^{th}}{\partial f_s} & \frac{\partial y_1^{th}}{\partial f_q} & \frac{\partial y_1^{th}}{\partial C_{NS}} & \frac{\partial y_1^{th}}{\partial C_S} & \frac{\partial y_1^{th}}{\partial \frac{m_s}{m}} \\ \frac{\partial y_2^{th}}{\partial f_s} & \frac{\partial y_2^{th}}{\partial f_q} & \frac{\partial y_2^{th}}{\partial C_{NS}} & \frac{\partial y_2^{th}}{\partial C_S} & \frac{\partial y_2^{th}}{\partial \frac{m_s}{m}} \\ \frac{\partial y_3^{th}}{\partial f_s} & \frac{\partial y_3^{th}}{\partial f_q} & \frac{\partial y_3^{th}}{\partial C_{NS}} & \frac{\partial y_3^{th}}{\partial C_S} & \frac{\partial y_3^{th}}{\partial \frac{m_s}{m}} \end{pmatrix}$$

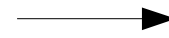
$$C_{kl} = \begin{pmatrix} \sigma_{f_q}^2 & 0 \\ 0 & \sigma_{f_s}^2 \end{pmatrix}$$

Re-evaluated at  
each  
minimization step



The experimental covariance matrix **B** contains correlation among common used quantities in the fitted relations:

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}$$



Introduces a correlation in the fitted quantities

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{Br(\eta' \rightarrow \gamma \gamma) \Gamma_{\eta'}}{\Gamma(\pi^0 \rightarrow \gamma \gamma)}$$

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{Br(\eta' \rightarrow \rho \gamma) \Gamma_{\eta'}}{\Gamma(\omega \rightarrow \pi^0 \gamma)}$$

$x_2$	-34					
$x_3$	-78	-29				
$x_4$	-35	-24	32			
$x_5$	-26	-12	26	8		
$x_6$	-28	-11	35	11	9	
$\Gamma$	32	-2	-24	-5	-88	-8
	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$

**Br and  $\Gamma$  strongly correlated (above all  $\Gamma(\eta' \rightarrow \gamma \gamma)$ )**

**the  $\Gamma$  is measured using:**

$$e^+e^- \rightarrow \eta' e^+e^-$$

**An independent measurement of the  $\eta'$  total width is welcome.**

Mode	Rate (MeV)	Scale factor
$\Gamma_1$ $\pi^+ \pi^- \eta$	0.090 ± 0.008	1.2
$\Gamma_2$ $\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$ )	0.060 ± 0.005	1.2
$\Gamma_3$ $\pi^0 \pi^0 \eta$	0.042 ± 0.004	1.6
$\Gamma_4$ $\omega \gamma$	0.0062 ± 0.0008	1.2
$\Gamma_5$ $\gamma \gamma$	0.00430 ± 0.00015	1.1
$\Gamma_6$ $3\pi^0$	(3.2 ± 0.6) × 10 <sup>-4</sup>	1.1



# Fit results without $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$

**This fit**

$$\chi^2/\text{ndf} = 1.8/2$$

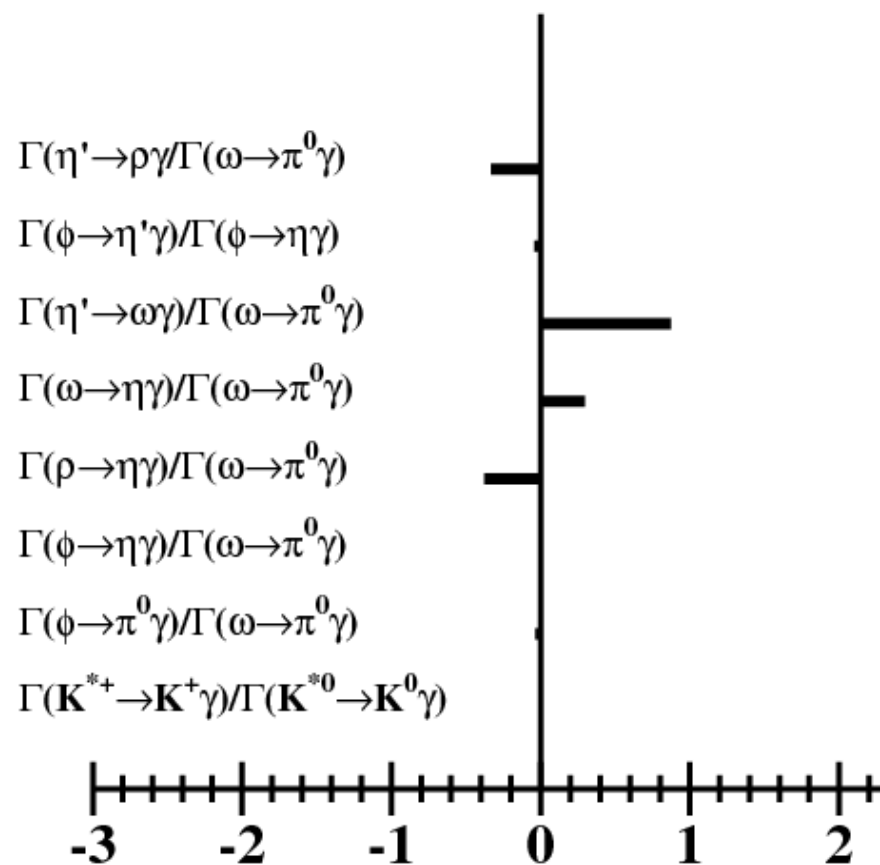
**Escribano et al.**

(JHEP 0705:006,2007)

$$\chi^2/\text{ndf} = 4.0/4$$

$Z^2$	$0.03 \pm 0.06$	$0.04 \pm 0.09$
$\phi_p$	$(41.6 \pm 0.8)^\circ$	$(41.4 \pm 1.3)^\circ$
$Z_q$	$0.85 \pm 0.03$	$0.86 \pm 0.03$
$Z_s$	$0.78 \pm 0.05$	$0.79 \pm 0.05$
$\phi_V$	$(3.16 \pm 0.10)^\circ$	$(3.2 \pm 0.1)^\circ$
$\frac{m_s}{\bar{m}}$	$1.24 \pm 0.07$	$1.24 \pm 0.07$

$$\text{Pulls} = \frac{\text{Measure} - \text{Fit}}{\sigma_{\text{Measure}}}$$

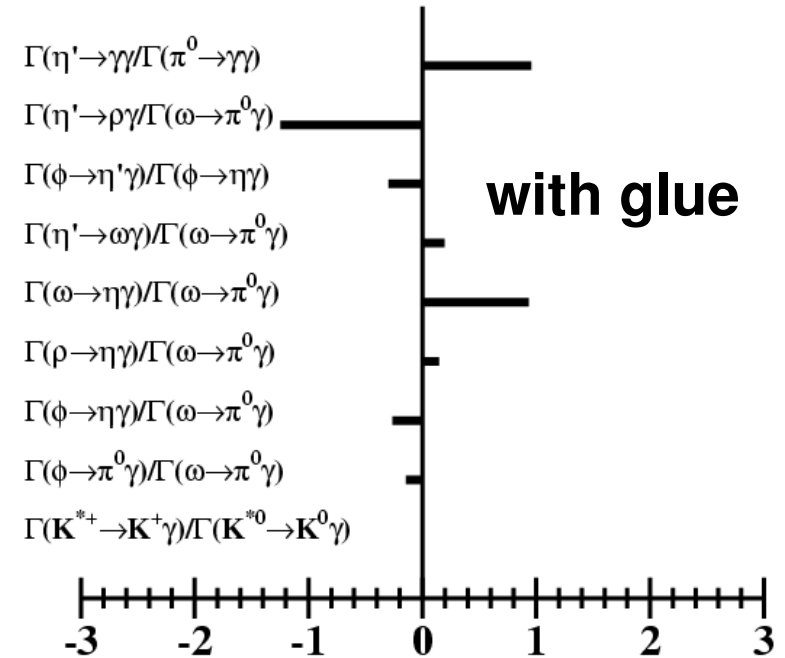
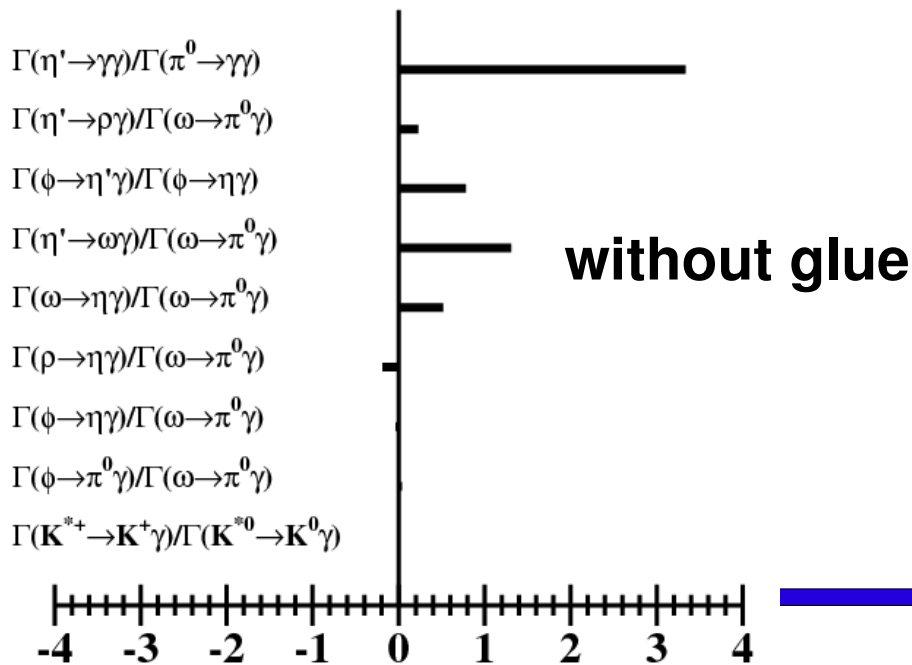


If we include the  $P \rightarrow \gamma\gamma$  constraint

$$\frac{\Gamma(\eta' \rightarrow \gamma\gamma)}{\Gamma(\pi^0 \rightarrow \gamma\gamma)} = \frac{1}{9} \left( \frac{m_{\eta'}}{m_{\pi}} \right)^3 \left( 5 \sin(\phi_P) \cos(\phi_G) + \sqrt{2} \frac{f_q}{f_s} \cos(\phi_P) \cos(\phi_G) \right)^2$$

$$Pulls = \frac{Measure - Fit}{\sigma_{Measure}}$$

	without glue $\chi^2/ndf = 13/4$ ( 1.1%)	with glue $\chi^2/ndf = 5/3$
$z^2$	fixed 0	$0.105 \pm 0.037$
$\phi_P$	$(41.6 \pm 0.5)^\circ$	$(40.7 \pm 0.7)^\circ$
$z_q$	$0.863 \pm 0.024$	$0.866 \pm 0.025$
$z_s$	$0.78 \pm 0.05$	$0.79 \pm 0.05$
$\phi_V$	$(3.17 \pm 0.10)^\circ$	$(3.15 \pm 0.10)^\circ$
$\frac{m_s}{\bar{m}}$	$1.24 \pm 0.07$	$1.24 \pm 0.07$





## Fitting the couplings...

The fit is performed directly on the coupling “g” that are derived from PDG06 using the formula:

$$\Gamma(P \rightarrow V \gamma) = \frac{g^2}{4\pi} |p_\gamma|^3 \qquad \Gamma(V \rightarrow P \gamma) = \frac{1}{3} \frac{g^2}{4\pi} |p_\gamma|^3$$

$$g_{\rho^0 \pi^0 \gamma} = g_{\rho^+ \pi^+ \gamma} = \frac{1}{3} g, \quad g_{\omega \pi \gamma} = g \cos \phi_V, \quad g_{\phi \pi \gamma} = g \sin \phi_V,$$

$$g_{K^{*0} K^0 \gamma} = -\frac{1}{3} g z_K \left(1 + \frac{\bar{m}}{m_s}\right), \quad g_{K^{*+} K^+ \gamma} = \frac{1}{3} g z_K \left(2 - \frac{\bar{m}}{m_s}\right),$$

$$g_{\rho \eta \gamma} = g z_q X_\eta, \quad g_{\rho \eta' \gamma} = g z_q X_{\eta'}$$

$$g_{\omega \eta \gamma} = \frac{1}{3} g \left( z_q X_\eta \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right), \quad \mathbf{1) \text{ No correlation taken into account}}$$

$$g_{\omega \eta' \gamma} = \frac{1}{3} g \left( z_q X_{\eta'} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right), \quad \mathbf{2) \text{ Some parameters added (g, } z_K), \text{ they disappear in the}}$$

$$g_{\phi \eta \gamma} = \frac{1}{3} g \left( z_q X_\eta \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right), \quad \mathbf{\text{disappear in the}}$$

$$g_{\phi \eta' \gamma} = \frac{1}{3} g \left( z_q X_{\eta'} \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right), \quad \mathbf{\text{ratio.}}$$





# No $P \rightarrow \gamma\gamma$ measurement. Fit done with gluonium.

**this fit**

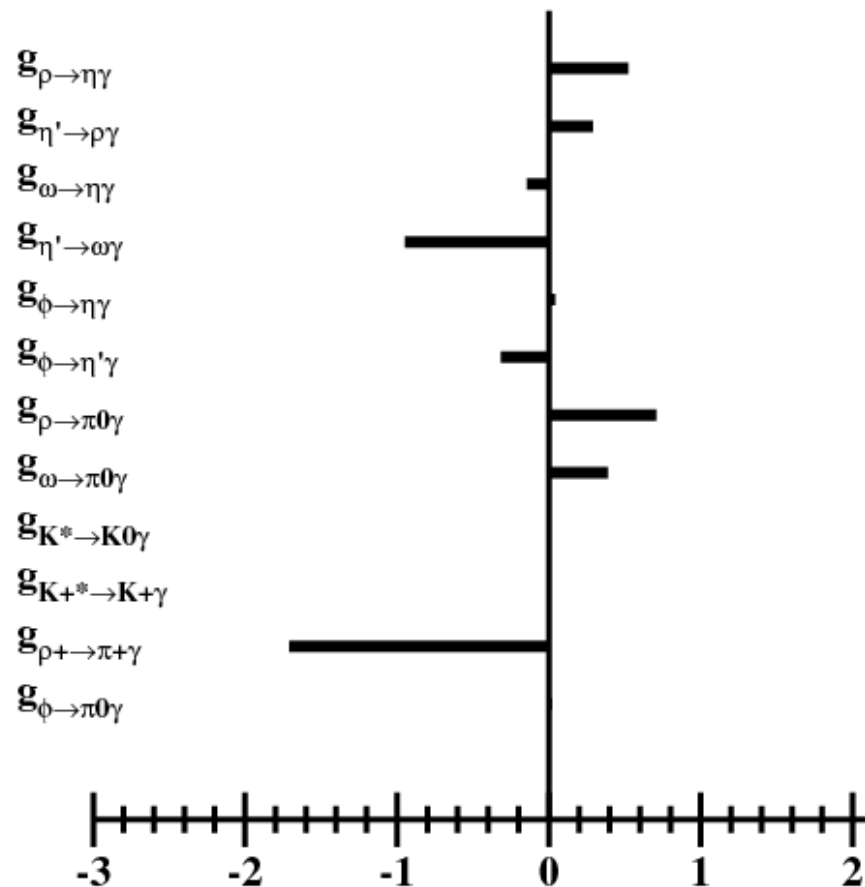
$\chi^2/\text{ndf} = 4.7/4$

**escribano**

(JHEP 0705:006,2007)

$\chi^2/\text{ndf} = 4.4/5$

$\phi_G$	$(11 \pm 11)^\circ$	$(12 \pm 13)^\circ$
$\phi_P$	$(41.5 \pm 1.1)^\circ$	$(41.4 \pm 1.3)^\circ$
$Z_q$	$0.86 \pm 0.03$	$0.86 \pm 0.03$
$Z_s$	$0.78 \pm 0.05$	$0.79 \pm 0.05$
$\phi_V$	$(3.18 \pm 0.10)^\circ$	$(3.2 \pm 0.1)^\circ$
$\frac{m_s}{\bar{m}}$	$1.24 \pm 0.07$	$1.24 \pm 0.07$
$Z_K$	$0.89 \pm 0.03$	$0.89 \pm 0.03$
$g$	$0.719 \pm 0.010$	$0.72 \pm 0.01$





# $P \rightarrow \gamma\gamma$ measurement included in the fit.

$$\frac{\Gamma(\eta' \rightarrow \gamma\gamma)}{\Gamma(\pi^0 \rightarrow \gamma\gamma)} = \frac{1}{9} \left( \frac{m_{\eta'}}{m_{\pi}} \right)^3 \left( 5 \sin(\phi_P) \cos(\phi_G) + \sqrt{2} \frac{f_q}{f_s} \cos(\phi_P) \cos(\phi_G) \right)^2 \quad \text{E. Kou, Phys. Rev. D 63 (2001) 54027}$$

**without glue**      **with glue**  
 $\chi^2/\text{ndf} = 13/5$  (2.3%)     $\chi^2/\text{ndf} = 7.2/4$

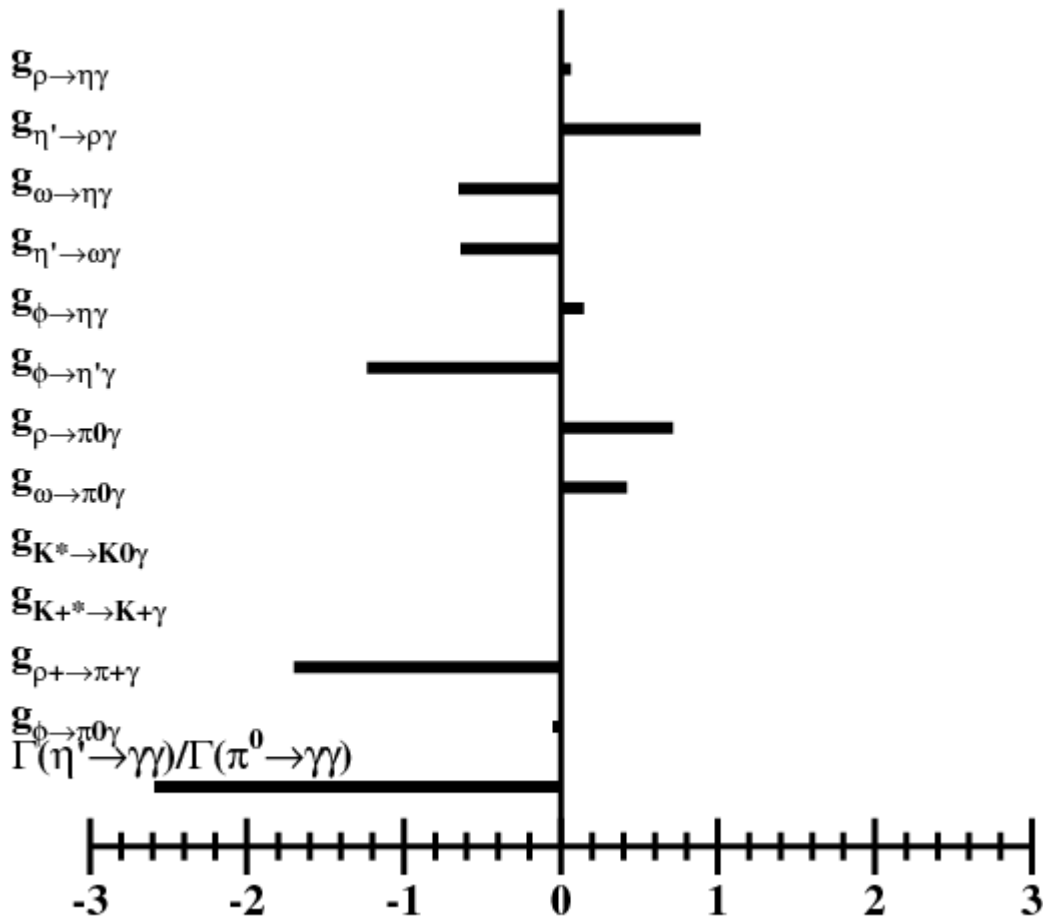
$\phi_G$	fixed at 0	$(20 \pm 4)^\circ$
$\phi_P$	$(40.1 \pm 0.9)^\circ$	$(41.2 \pm 1.1)^\circ$
$Z_q$	$0.85 \pm 0.024$	$0.88 \pm 0.03$
$Z_s$	$0.80 \pm 0.05$	$0.79 \pm 0.05$
$\phi_V$	$(3.2 \pm 0.1)^\circ$	$(3.18 \pm 0.10)^\circ$
$\frac{m_s}{\bar{m}}$	$1.24 \pm 0.07$	$1.24 \pm 0.07$
$Z_K$	$0.89 \pm 0.03$	$0.89 \pm 0.03$
$g$	$0.72 \pm 0.01$	$0.719 \pm 0.010$

$$Z_{\eta'}^2 = 0.11 \pm 0.05$$

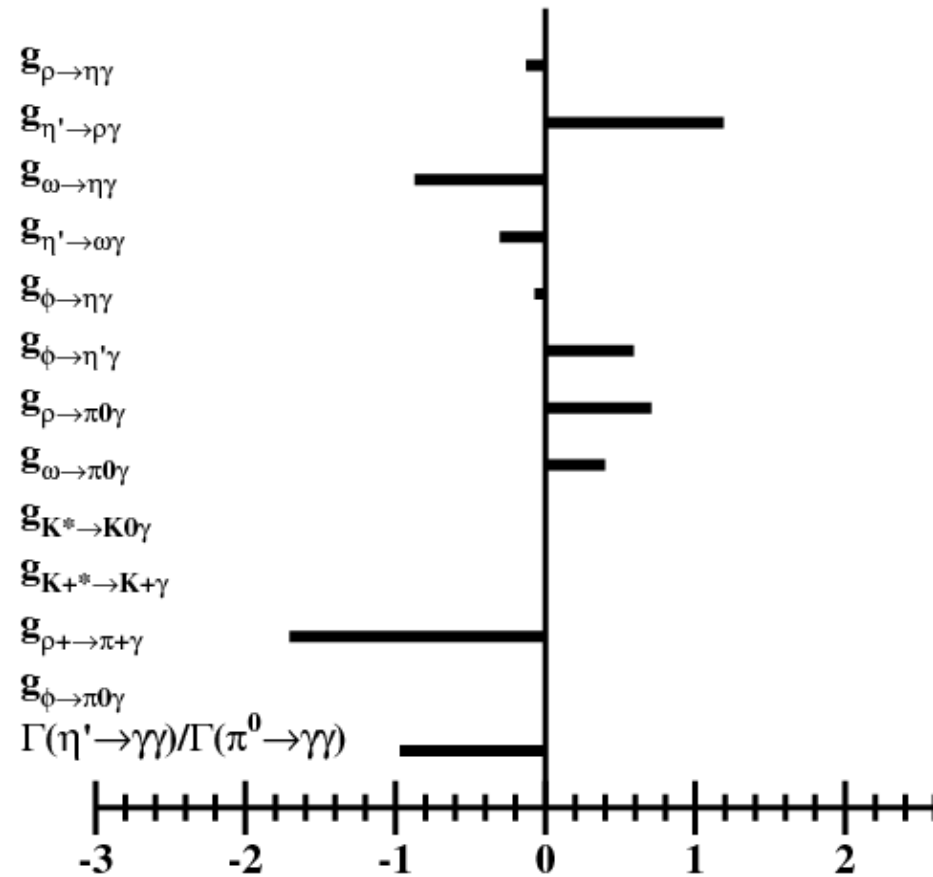


# Fit pulls comparison.

without glue



with glue





# Conclusions

- The difference between KLOE and Escribano result due to the choice to include  $P \rightarrow \gamma\gamma$
- Leaving free  $z_q$  and  $z_s$  parameter doesn't have important effects
- A question to Bass  
Could the glue involved in  $V \rightarrow P\gamma$  different than the one seen in  $\eta' \rightarrow \gamma\gamma$ ?