

Report on the Madrid workshop: theoretical issues and experiment

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The SM as an effective theory

$$\mathcal{L}_{SM}^{\text{eff}} = \mathcal{L}_{SM}^{\text{ren}} + \frac{h_{ij}}{\Lambda} (H L_i)(H L_j) + \dots$$

$$m_\nu = h_\nu \cdot \frac{v}{\Lambda}$$

$$\Lambda \sim 0.5 \cdot 10^{15} \text{ GeV } h \left(\frac{0.05 \text{ eV}}{m_\nu} \right)$$

- Measure the physical parameters; what do we learn?
- Probe the set up
- Non-oscillation (new physics) effects?

Physical observables in the lepton sector

$$m_e, m_\mu, m_\tau, m_1, m_2, m_3, \theta_{23}, \theta_{12}, \theta_{13}, \delta, \alpha, \beta$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -s_{23}c_{12} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 \\ e^{i\alpha} \\ e^{i\beta} \end{pmatrix}$$

$$(0 \leq \theta_{12}, \theta_{23}, \theta_{13} \leq \pi/2, \quad 0 \leq \delta \leq 2\pi)$$

$$L \supset -m_{e_i} \bar{e}_i^c e_i - \frac{g}{\sqrt{2}} U_{ij} \bar{e}_i \hat{W} P_L \nu_j - \frac{1}{2} m_i \nu_i \nu_i$$

$m_{e,\mu,\tau}$

$$\Delta m_{21}^2$$

$$|\Delta m_{32}^2|$$

$$\text{sign}(\Delta m_{32}^2)$$

$$\theta_{12}, \theta_{23}, \theta_{13}, \delta$$

m_{lightest}

α

β

$m_{e,\mu,\tau}$

$$\begin{aligned} & \Delta m_{21}^2 \\ & |\Delta m_{32}^2| \\ & \text{sign}(\Delta m_{32}^2) \\ & \theta_{12}, \theta_{23}, \theta_{13}, \delta \end{aligned}$$

m_{lightest}

α

β

$m_{e,\mu,\tau}$

$$\Delta m_{21}^2$$

$$|\Delta m_{32}^2|$$

$$\text{sign}(\Delta m_{32}^2)$$

$$\theta_{12}, \theta_{23}, \theta_{13}, \delta$$

m_{lightest}

α

β

$$\nu_{\mu} \rightarrow \nu_e$$

T2K upgrade of K2K with a more intense beam and OA

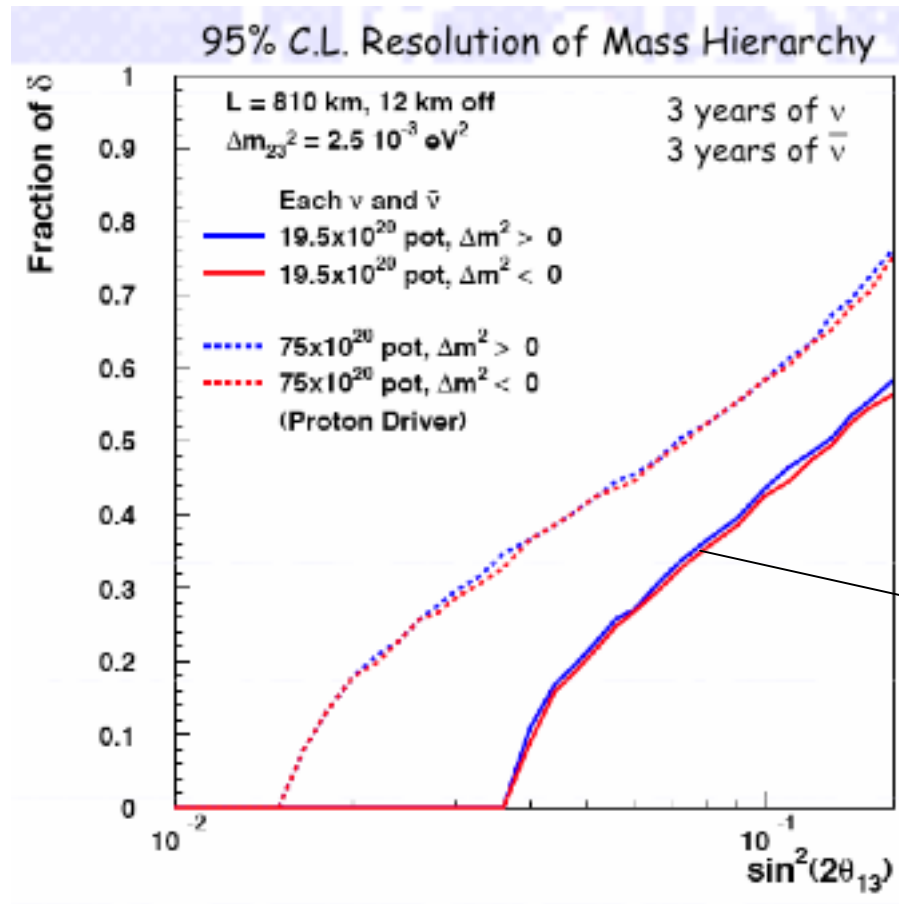
NOvA upgrade of MINOS with a better detector and OA

3σ CL

	L(km)	$\sin^2 2\theta_{13}$	δ	$\text{sign}(\Delta_{23})$	$\text{sign}(\cos 2\theta_{23})$
T2K-I (2008)	295	~ 0.01 0.02	-	-	-
NOvAI (2011)	810	0.003 0.02	-	some	-

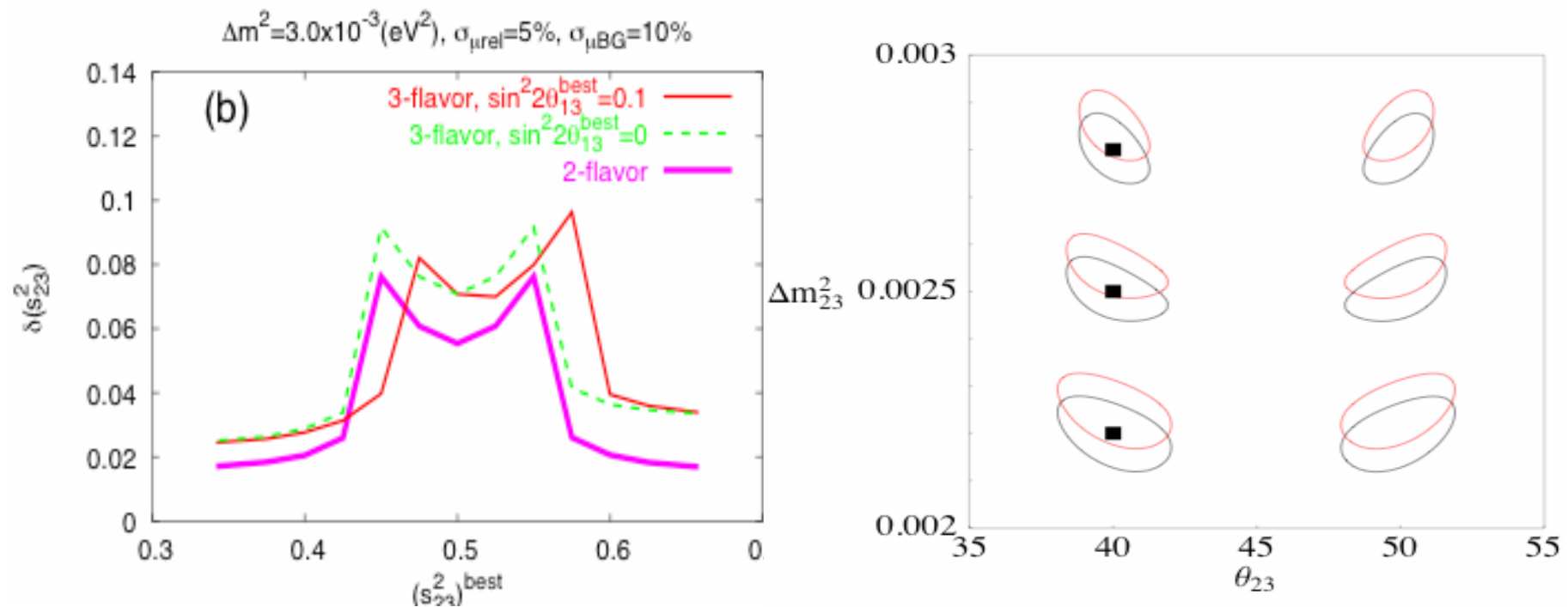
Sensitivity to θ_{13} strongly depends on δ in both cases and also on $\text{sign}(\Delta_{23})$ in NOvA

Hierarchy at NOvA-I



NOvA-I

Only for $\sin^2 2\theta_{13} > 0.04$ and some values of δ

Sensitivity to $\sin^2\theta_{23}$ 

Minakata, Sonoyama

Fernandez-Martinez et al

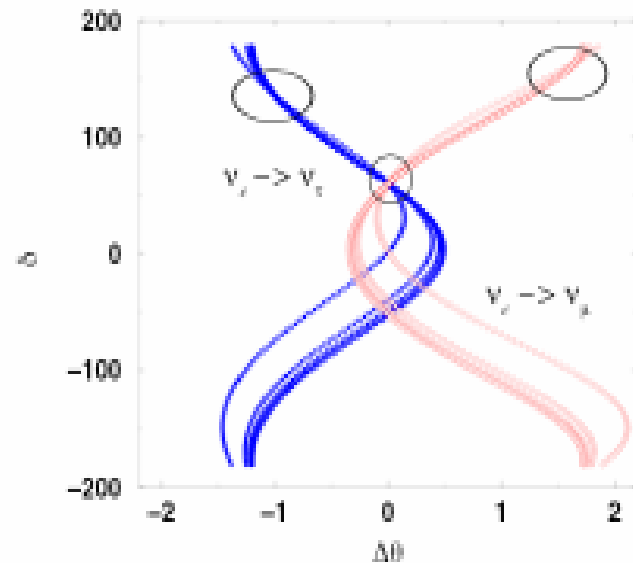
For $42^\circ < \theta_{23} < 50^\circ$ the error on s_{23}^2 remains $O(10\text{-}20\%)$ which is not much better than the present error!

Ultimate anti-degeneracy machine

vFACT & 40K Ton iron calorimeter 2800km (Golden) $\nu_e \rightarrow \nu_\mu$

vFACT & 4Ton Emulsion 730km(Silver) $\nu_e \rightarrow \nu_\tau$

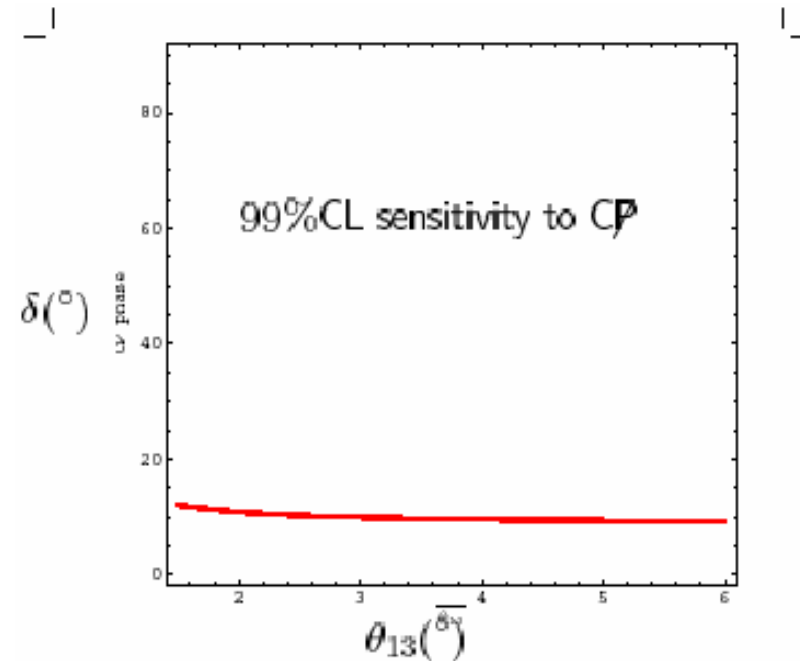
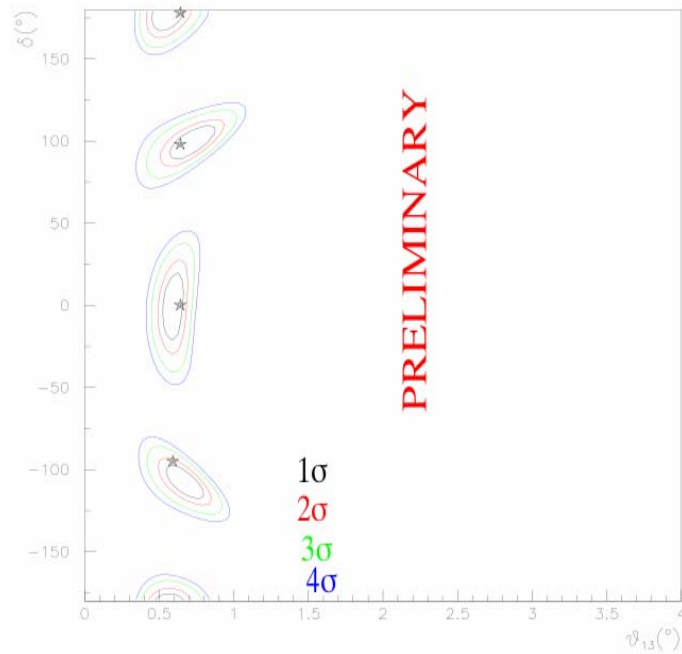
SPL&Megaton Cerenkov (Bronze) 130km $\nu_\mu \rightarrow \nu_e$



The intrinsic and the θ_{23} octant ambiguities are resolved (up to uncertainties) if the $e\mu$ and $e\tau$ are combined

Donini, Meloni, Migliozzi

θ_{13} sensitivity down to 0.3° !



Mena

Hierarchy and octant solved for $\theta_{13} > 1^\circ - 2^\circ$

Overconstraining: $e\mu, ee, e\tau, \mu\tau, \mu e, \mu\mu$ for ν and $\bar{\nu}$!

The new era (discovery)
 (roughly...depends on the actual value of the parameters)

	θ_{13}	δ	$\text{sign}(\Delta_{23})$	θ_{23}
~2013	$> 4^\circ$	marginal	$\theta_{13} > 6^\circ$ (0%) $\theta_{13} > 13^\circ$ (50%)	40° - 50° deg.
~202?	> 0.3 - 0.6°	$ \delta > 10^\circ$ large θ_{13}	$\theta_{13} > 1^\circ$ - 2° (100%)	

While T2K-I seems to be a rather optimal setup for the next generation superbeam, the “optimal” next-to-new generation experiment is still under investigation

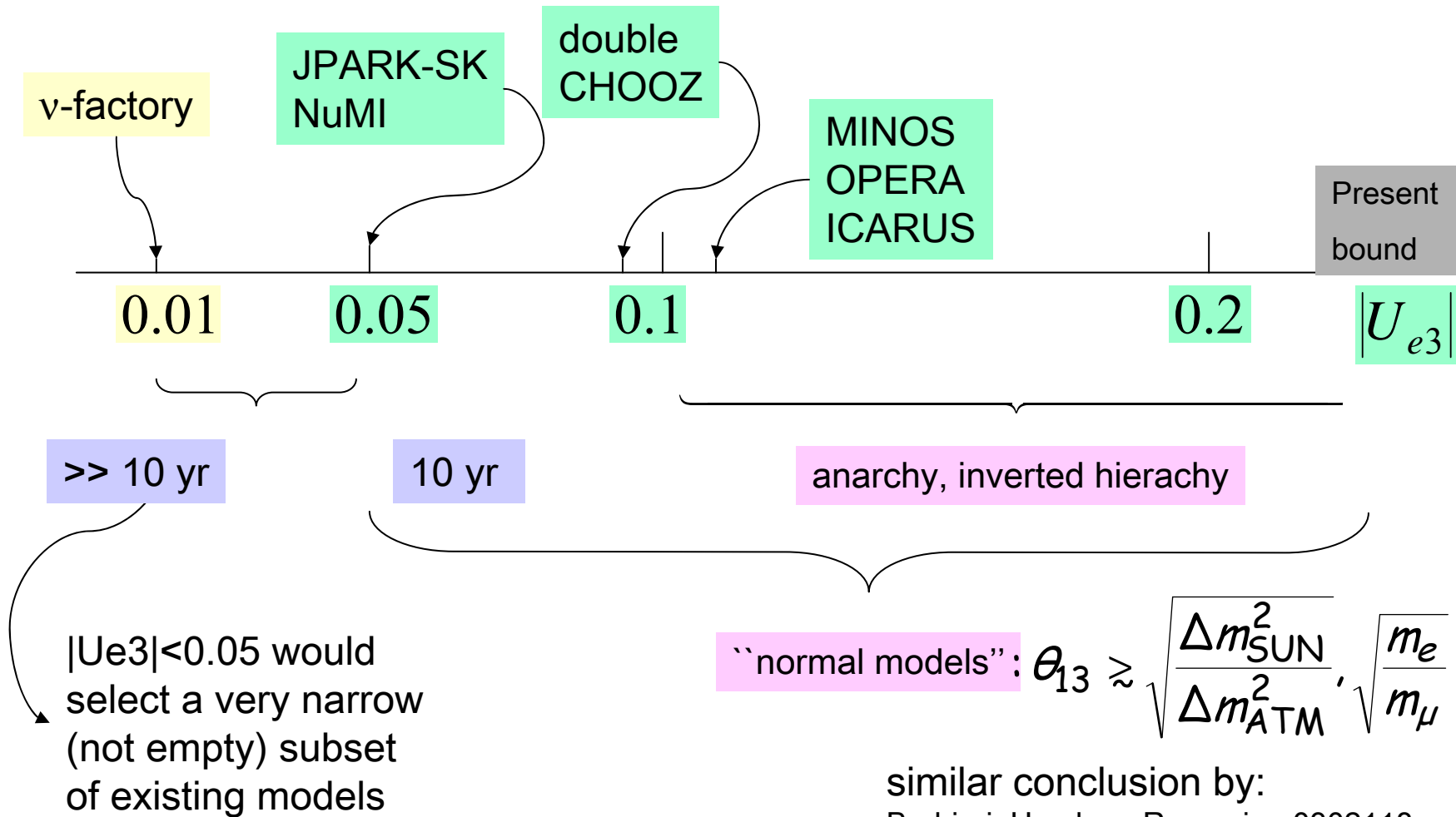
- θ_{13}
- θ_{23}
- θ_{12}
- Normal vs Inverse hierarchy

as handles on the origin of masses and mixings

$$\theta_{13}$$

- Phenomenology
 - Access leptonic CP-violation
 - Supernova signals
 - Subleading effects
 - Origin of masses and mixing
 - (Discriminate models - too many)
 - **Size** of θ_{13} : "normal" models vs "special" models
 - Test models with **precise** predictions (if not too many)
- in particular:
- Probe the origin of the solar and atmospheric angles
 - The Neutrino mass pattern

- Most of plausible range for U_{e3} explored in 10 yr from now



similar conclusion by:

Barbieri, Hambye, Romanino 0302118

Ibarra, Ross 0307051

Chen, Mahanthappa 0305088

Lebed, Martin 0312219

Joshipura @ NOON 2004

Example of "normal" models (θ_{23} from ν 's)

Normal hierarchy: $m_\nu \propto \begin{pmatrix} \varepsilon & \varepsilon' \\ \varepsilon & B & A \\ \varepsilon' & A & 1 \end{pmatrix}$ θ_{23}^V large : $A \sim B \sim 1$
 $m_2 \ll m_3 : A^2 - B \ll 1$

We expect: $\theta_{13} \sim \frac{\tan \theta_{23}}{2} \sin 2\theta_{12} \left(\frac{\Delta m_{21}^2}{\Delta m_{32}^2} \right)^{1/2} > 0.07$

Inverse hierarchy: $m_\nu = \begin{pmatrix} A & B \\ A & B \\ B \end{pmatrix} + \text{corrections}$ $\tan \theta_{23} = \frac{B}{A}$

We expect: $s_{13} \supset s_{12}^e s_{23} \sim \frac{45^\circ - \theta_{12}}{2} \sim \text{expl limit}$

A small θ_{13} presumably indicates that the atmospheric angle comes from the charged sector

Yet another contribution to θ_{13}

$$m_D = \dots \begin{pmatrix} 0 & \varepsilon' \\ \varepsilon' & \varepsilon \\ & & 1 \end{pmatrix} \text{ is successful: } \theta_c \approx \sqrt{\frac{m_d}{m_s}} \text{ (precise)} \quad [\text{Gatto Sartori}]$$

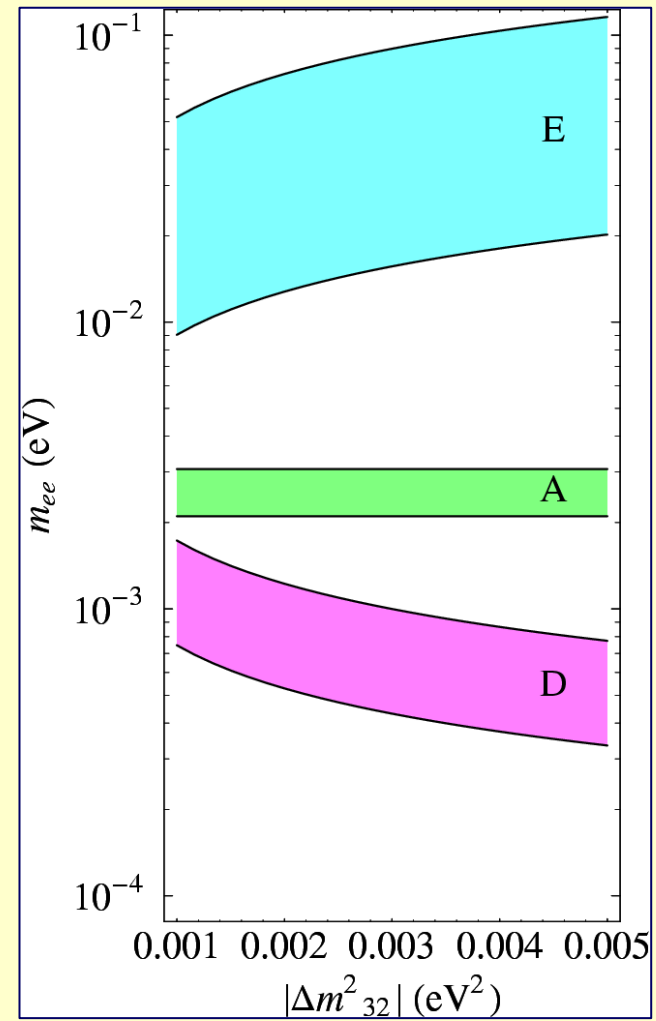
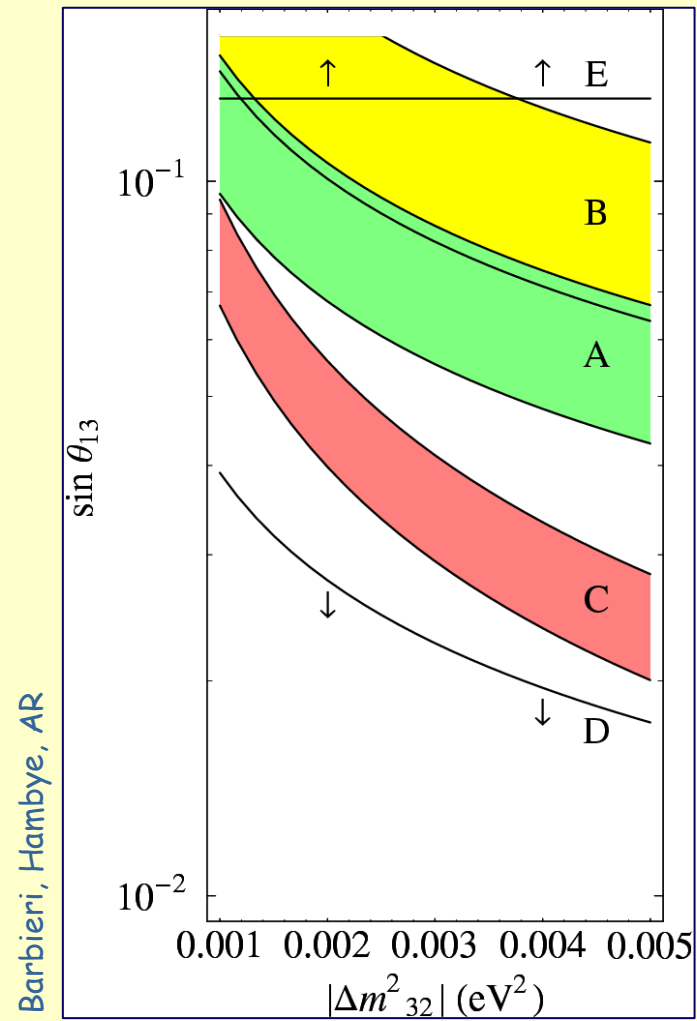
Implementing the same pattern in m_E (e.g. SU(5))

$$\theta_{12}^e \approx \sqrt{\frac{m_e}{m_\mu}} = \frac{1}{3} \sqrt{\frac{m_d}{m_s}} \approx \frac{\theta_c}{3}$$

$$\theta_{13} \supset s_{23} \sqrt{\frac{m_e}{m_\mu}} \sim \frac{1}{3} \times \text{explimit} \sim 3^\circ$$

Central value observable with superbeams (but $> O(1)$ uncertainty)

Predictive models



Is the atmospheric angle large or maximal?

- Large = $O(\pi/4)$; maximal = $\pi/4 \pm \text{correction} \ll 1$

- SK: $\sin^2 2\theta_{23} > 0.9$ not enough

$$\tan\theta_{23} = a/b \quad a \sim b \leftrightarrow \text{large } \theta_{23}; \quad a = b \leftrightarrow \text{maximal } \theta_{23}$$

$$1 - \varepsilon < a/b < 1 + \varepsilon \quad \sin^2 2\theta_{23} > 1 - \varepsilon^2$$

$$0.7 < a/b < 1.4 \quad \sin^2 2\theta_{23} > 0.9$$

$$0.9 < a/b < 1.1 \quad \sin^2 2\theta_{23} > 0.99$$

- Obtaining a maximal atm angle in a 3 neutrino context is non-trivial. A maximal angle would set a powerful constraint on the origin of lepton mixing (non-abelian horizontal symmetries?)

- Example: inverse hierarchy

$$m_\nu = \begin{pmatrix} & a & b \\ a & & \\ b & & \end{pmatrix} + \text{corrections} \quad \tan\theta_{23} = \frac{b}{a}$$

Is there a relation between θ_{12} and θ_c ?

Lepton mixings

Parameter	Best-fit value	3σ range
θ_{12}	33.2°	$28.7^\circ \dots 38.1^\circ$
θ_{23}	45.0°	$35.7^\circ \dots 55.6^\circ$
θ_{13}	2.6°	$0^\circ \dots 12.5^\circ$

at present: large
uncertainty for θ_{12}

Quark mixings

Parameter	Best-fit value	2σ range
θ_{12}^q	12.88°	$12.75^\circ \dots 13.01^\circ$
θ_{23}^q	0.21°	$0.17^\circ \dots 0.25^\circ$
θ_{13}^q	2.36°	$2.25^\circ \dots 2.48^\circ$

Is there a relation $\theta_{12} + \theta_c = 45^\circ$ hidden behind the large uncertainties?

'Quark-lepton complementarity'

Recent papers: Raidal ('04), Smirnov, Minakata ('04),
Mohapatra, Frampton ('04), Ferrandis, Pakvasa ('04), ...

- **Future: few % accuracy for $\sin^2\theta_{12}$ possible**, e.g. from reactor experiments; could test of 'quark-lepton complementarity' to high precision
see e.g.: [Minakata et al, hep-ph/0407326](#)
- If 'confirmed' (not accidental):
 - Relation between quark and lepton mixing angles would point towards unification
 - Challenging for model building. However, we could learn a great deal ...
(predictions at M_U modified by RG running!)

Challenges for Quark-Lepton Complementarity

- **Approach:** $\theta_{12}^{\nu} = \pi/4$ from the neutrino sector, deviation induced by θ_{12}^e related to θ_C
- **Using a Georgi Jarlskog (Clebsch) factor of -3 for $(Y_e)_{22}$:** no QLC predicted

Note: same operators lead to entries in Y_e and Y_d !

Assume: $\theta_{12}^{\nu} = \pi/4$ (and large θ_{23}^{ν}), e.g. with inverted neutrino mass hierarchy:

$$Y_d \sim \begin{pmatrix} 0 & 1\lambda^4 & \lambda^4 \\ * & 1\lambda^3 & \lambda^2 \\ * & * & 1 \end{pmatrix}, \quad Y_e \sim \begin{pmatrix} 0 & \lambda^4 & \lambda^4 \\ * & -3\lambda^3 & \lambda^2 \\ * & * & 1 \end{pmatrix}, \quad m_{LL} \sim \begin{pmatrix} 0 & m & m' \\ m & 0 & 0 \\ m' & 0 & 0 \end{pmatrix}$$

$\theta_{12}^d = \lambda = \theta_C$

$\theta_{12}^e = 1/3 \lambda = 1/3 \theta_C$

- **In addition:** one has to 'shift' R_{12}^e to the right $\Delta\theta_{12} \Rightarrow$ additional factor $1/\sqrt{2}$

$$U_{MNS} \approx R_{12}^{e\dagger} R_{23}^{\nu} U_{13}^{\nu} R_{12}^{\nu} P_0^{\nu} \Rightarrow s_{12} \approx \frac{1}{\sqrt{2}} - \frac{1}{2}\theta_{12}^e \rightarrow \theta_{12} \approx \frac{\pi}{4} - \frac{1}{\sqrt{2}}\theta_{12}^e$$

$$\theta_{12} \approx \frac{\pi}{4} - \frac{1}{\sqrt{2}}\frac{1}{3}\theta_C \Rightarrow \Delta\theta_{12} = \frac{1}{\sqrt{2}}\frac{1}{3}\theta_C \approx 3^\circ$$

Too small for explaining observed deviation from $\theta_{12} = \pi/4$
- in particular: no QLC!

$$U_{PMNS} = \begin{pmatrix} \sqrt{\frac{2}{3}} & \frac{1}{\sqrt{3}} & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{pmatrix} + O\left(\frac{\text{VEV}}{\Lambda}\right)^2$$

$$\vartheta_{13} \approx O\left(\frac{\text{VEV}}{\Lambda}\right)^2$$

$$\vartheta_{23} \approx \frac{\pi}{4} + O\left(\frac{\text{VEV}}{\Lambda}\right)^2$$

[Harrison, Perkins, Scott 2002]

$$\tan^2 \vartheta_{12} = 0.5 + O\left(\frac{\text{VEV}}{\Lambda}\right)^2$$

$$\frac{\text{VEV}}{\Lambda} \approx \lambda \quad \text{expected}$$

$$\tan^2 \vartheta_{12} = 0.45 \pm 0.05 \quad [\text{exp}]$$

Another example of precise prediction for θ_{12}

ν spectrum is between normal and degenerate

$$m_1 \approx a + d \quad m_2 \approx a \quad m_3 \approx -a + d \quad \left[\text{units } \frac{v_u^2}{\Lambda} \right]$$

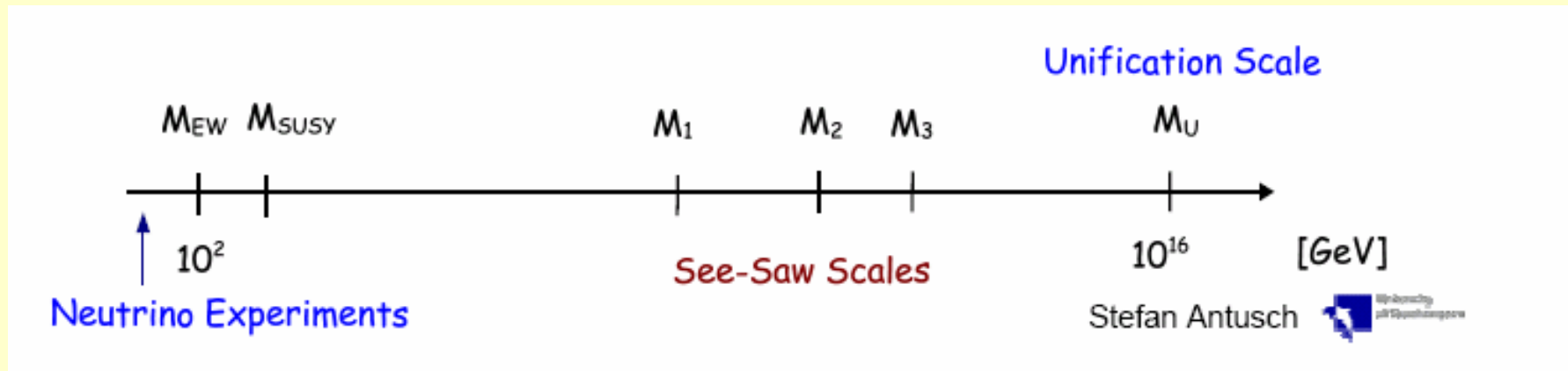
$$d \approx -2a \quad \text{to reproduce} \quad \frac{\Delta m_{sol}^2}{\Delta m_{atm}^2} \approx \frac{1}{35}$$

prediction:

$$|m_3|^2 = |m_{ee}|^2 + \frac{10}{9} \Delta m_{atm}^2 \left(1 - \frac{\Delta m_{sol}^2}{\Delta m_{atm}^2} \right)$$

Caveat: RGE running corrections

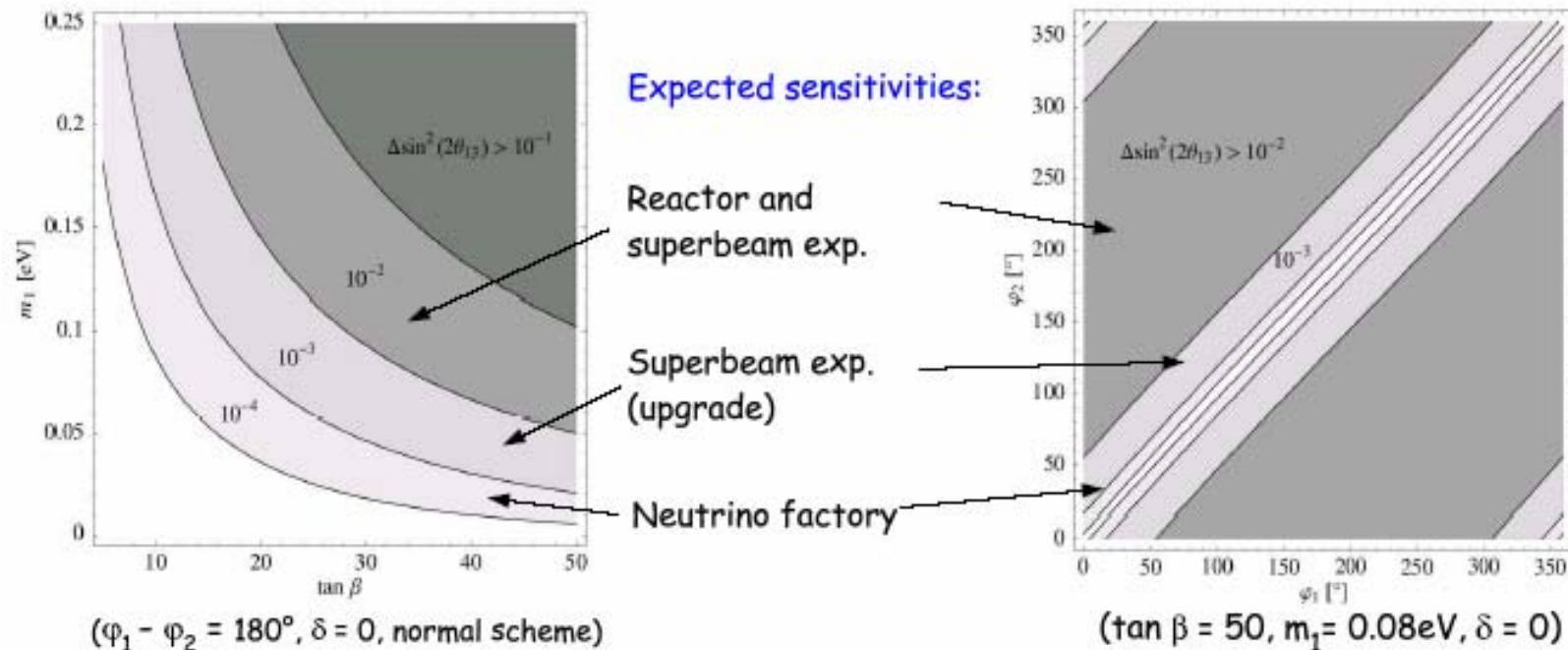
Intrinsic limitation on the use of precise data as an handle on the origin of masses and mixings: the theoretical uncertainty on the connection with high energy



RG Corrections to $\theta_{13} = 0$ @ High Energy

Graphical illustration of RG corrections ($\Delta \sin^2(2\theta_{13})$)

(running of dim. 5 operator between $\Lambda = 10^{12}$ GeV and M_{EW} in the MSSM)



Even for $\theta_{13} = 0$ @ high energy, RG running \Rightarrow in general non-zero θ_{13} @ low energy

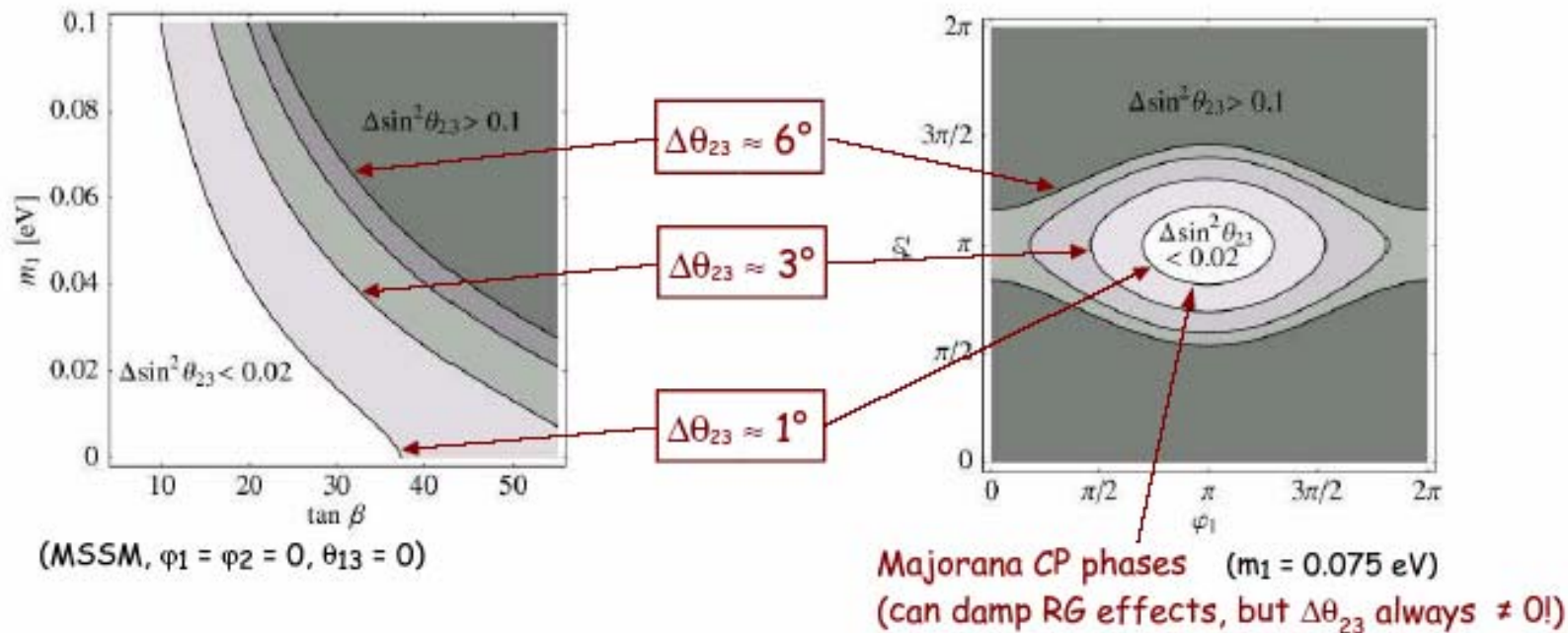
RG Corrections to Maximal Mixing $\theta_{23} = 45^\circ$

Analytical Approximation (below see-saw scales): $\Delta\theta_{23} = \dot{\theta}_{23} \ln(\Lambda/M_{EW})$

$$\dot{\theta}_{23} \approx -\frac{y_\tau^2}{32\pi^2} \sin 2\theta_{23} \frac{1}{\Delta m_{atm}^2} [c_{12}^2 |m_2 e^{i\varphi_2} + m_3|^2 + s_{12}^2 |m_1 e^{i\varphi_1} + m_3|^2] + \mathcal{O}(\theta_{13})$$

Note: $\Delta\theta_{23} > (<) 0$ for $\Delta m_{atm}^2 < (>) 0$

Example: Conservative estimate (ignore Y_ν contributions) of RG corrections (MSSM)



S.A., J. Kersten, M. Lindner, M. Ratz (hep-ph/0305273)

S.A., M. Huber, J. Kersten, T. Schwetz, W. Winter (hep-ph/0404268)

The uncertainties on the running can significantly affect t_{12} only if it originates from an unstable pattern

$$\begin{pmatrix} 1 + \varepsilon & \varepsilon \\ \varepsilon & 1 + \varepsilon \end{pmatrix}$$

Unstable (angles depend on the epsilons)

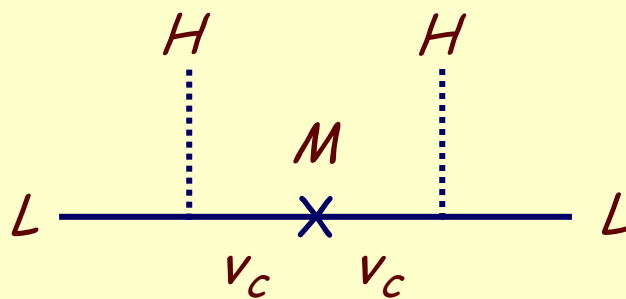
$$\begin{pmatrix} \varepsilon & 1 + \varepsilon \\ 1 + \varepsilon & \varepsilon \end{pmatrix}$$

Stable (angles do not depend on the epsilons)

Probing the origin of neutrino masses

$$\mathcal{L}_{SM}^{\text{eff}} = \mathcal{L}_{SM}^{\text{ren}} + \frac{h_{ij}}{\Lambda} (H L_i)(H L_j) + \dots$$

Does $\frac{h_{ij}}{\Lambda} (H L_i)(H L_j)$ originate from the see-saw mechanism?



$$\frac{h}{\Lambda} \rightarrow -\lambda^T \frac{1}{M} \lambda$$

$$m_\nu = -m_D^T \frac{1}{M} m_D$$

To believe seesaw

(Sufficient conditions but not necessary)



- LHC finds SUSY, LC establishes SUSY
 - no more particles beyond the MSSM at TeV scale
 - Gaugino masses unify (two more coincidences)
 - Scalar masses unify for 1st, 2nd generations (two for 10, one for 5*, times two)
 - Scalar masses unify for the 3rd generation 10 (two more coincidences)
- ⇒ strong hint that there are no additional particles beyond the MSSM below M_{GUT} except for gauge singlets.

To believe seesaw (cont.)

(Sufficient conditions but not necessary)

- $0\nu\beta\beta$ seen, neutrinos are Majorana
 - LBL oscillation finds θ_{13} soon just below the CHOOZ limit
 - determines the **normal hierarchy** and finds **CP violation**
 - Scalar masses unify for the 3rd generation 5^* up to the neutrino Yukawa coupling $y_3 \sim 1$ above $M_3 = y_3^2 v^2 / m_3$
- \Rightarrow neutrino parameters consistent with leptogenesis

...

Probing the origin of neutrino masses

$$\mathcal{L}_{SM}^{\text{eff}} = \mathcal{L}_{SM}^{\text{ren}} + \frac{h_{ij}}{\Lambda} (H L_i)(H L_j) + \dots$$

Is $\frac{h_{ij}}{\Lambda} (H L_i)(H L_j)$ really the origin of neutrino masses?

$$\Lambda \gg \langle H \rangle ?$$

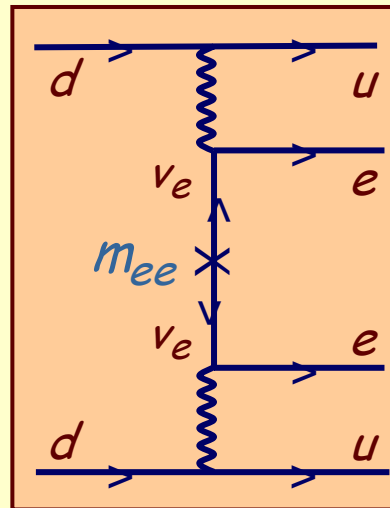
Probe the Majorana nature of neutrinos

$0\nu 2\beta$ decay

$$(A, Z) \rightarrow (A, Z + 2) + 2e^-; \text{ e.g.: } ^{76}\text{G} \rightarrow ^{76}\text{Se} + 2e^-$$

$$\Gamma \propto |m_{ee}|^2 \langle Q \rangle^2$$

$$m_{ee} = U_{eh}^2 m_h = c_{13}^2 (m_1 c_{12}^2 + m_2 s_{12}^2 e^{2i\alpha}) + m_3 s_{13}^2 e^{2i\beta}$$



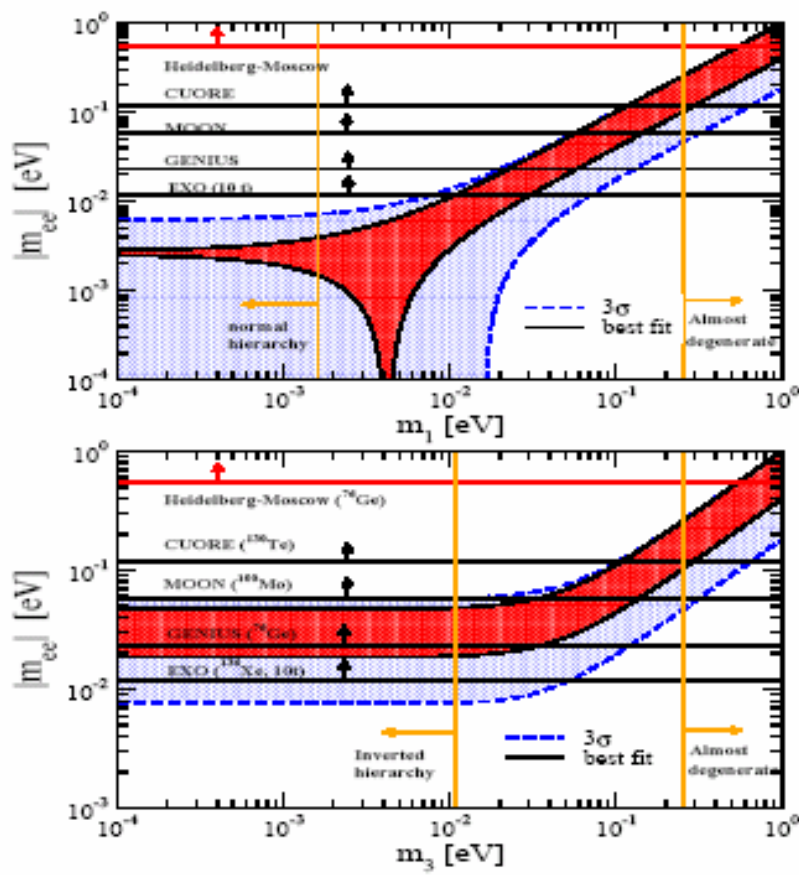
Present Limits :

Candidate nucleus	Detector type	(kg yr)	Present $T_{1/2}^{0\nu\beta\beta}$ (yr)	$\langle m \rangle$ (eV)
^{48}Ca	Ge diode	~30	$>9.5 \cdot 10^{21}$ (76%CL)	$<0.39^{+0.17}_{-0.28}$
^{76}Ge			$>1.9 \cdot 10^{25}$ (90%CL)	
^{82}Se			$>9.5 \cdot 10^{21}$ (90%CL)	
^{100}Mo			$>5.5 \cdot 10^{22}$ (90%CL)	
^{116}Cd			$>7.0 \cdot 10^{22}$ (90%CL)	
^{128}Te	TeO ₂ cryo	~3	$>1.1 \cdot 10^{23}$ (90%CL)	$<1.1 - 2.6$
^{130}Te	TeO ₂ cryo	~3	$>2.1 \cdot 10^{23}$ (90%CL)	
^{136}Xe	Xe scint	~10	$>1.2 \cdot 10^{24}$ (90%CL)	<2.9
^{150}Nd			$>1.2 \cdot 10^{21}$ (90%CL)	
^{160}Gd			$>1.3 \cdot 10^{21}$ (90%CL)	

Projected/proposed

Experiment	Nucleus	Detector	$T^{0\nu}$ (y)	$\langle m_\nu \rangle$ eV
CUORE	^{130}Te	.77 t of TeO_2 bolometers (nat)	7×10^{26}	.014-.091
EXO	^{136}Xe	10 t Xe TPC + Ba tagging	1×10^{28}	.013-.037
Gertha	^{76}Ge	1 t Ge diodes in LN	1×10^{28}	.013-.050
Majorana	^{76}Ge	1 t Ge diodes	4×10^{27}	.021-.070
MOON	^{100}Mo	34 t nat.Mo sheets/plastic sc.	1×10^{27}	.014-.057
DCBA	^{150}Nd	20 kg Nd-tracking	2×10^{25}	.035-.055
CAMEO	^{116}Cd	1 t CdWO_4 in liquid scintillator	$> 10^{26}$.053-.24
COBRA	^{116}Cd , ^{130}Te	10 kg of CdTe semiconductors	1×10^{24}	.5-2.
Candles	^{48}Ca	Tons of CaF_2 in liq. scint.	1×10^{26}	.15-.26
GSO	^{116}Cd	2 t $\text{Gd}_2\text{SiO}_5:\text{Ce}$ scint in liq scint	2×10^{26}	.038-.172
Xmass	^{136}Xe	1 t of liquid Xe	3×10^{26}	.086-.252

$\beta\beta_{0\nu}$ decay sensitivities of tritium & cosmo



Klapdor, Paes, Smirnov, ... **Bilenky, Faessler, Simkovic hep-ph/0402250**

can not yet reconstruct majorana phases Barger, Glashow, Langacker, Marfatia, PLB540 (2002) 247

Alternative origin of small neutrino masses

- If $\Lambda \gg \langle H \rangle$ is not the reason of the smallness of neutrino masses \Rightarrow small couplings
- Example: Dirac neutrinos

$$\lambda v_c LH \rightarrow m_\nu = \lambda v \quad (\text{as for the other fermions})$$

need $\lambda < 10^{-11}$ and $M_R \ll \langle H \rangle$

- Why? L conserved +
 - $\lambda v_c LH$ forbidden by a symmetry (e.g. because it has charge n under some $U(1)$ symmetry)

$$\lambda v_c LH \rightarrow \lambda \left(\frac{\phi}{\Lambda} \right)^n v_c LH \quad Q_\phi = -1 \quad \rightarrow \quad \lambda_{eff} = \lambda \left(\frac{\langle \phi \rangle}{\Lambda} \right)^n$$

Late neutrino mass

- Seesaw formula: $m_\nu = v^2/\Lambda \ll v$ because $v \ll \Lambda$
- Another way to get small mass with O(1) coupling:


$$m_\nu = v(\langle\phi\rangle/\Lambda)^n \text{ (Dirac)}$$

$$m_\nu = v^2(\langle\phi\rangle^n/\Lambda^{n+1}) \text{ (Majorana)}$$

Even if $\Lambda \sim \text{TeV}$, $\langle\phi\rangle \ll v$ works.

- “Late” neutrino mass because $\langle\phi\rangle \ll v$ implies a late time phase transition
- *e.g.*, $n=2$, $\Lambda \sim \text{TeV} \Rightarrow \langle\phi\rangle \sim \text{MeV}$

Viabile

- 
- Remarkably, phenomenological constraint weak despite the low scale
 - For $m_\phi > 1 \text{ MeV}$, $\phi \rightarrow \nu\nu$ above BBN, OK
 - SN1987A limit OK because ϕ couples with strength $\propto m_\nu$
 - If gauged, the domain walls are becoming important only now, possible imprint on CMB anisotropy

(Checko, Hall, Okui, Oliver)
(Davoudiasl, Kitano, Kribs, HM)

(Alternative origin of small neutrino masses, continues)

ξ_i are small due to geometry

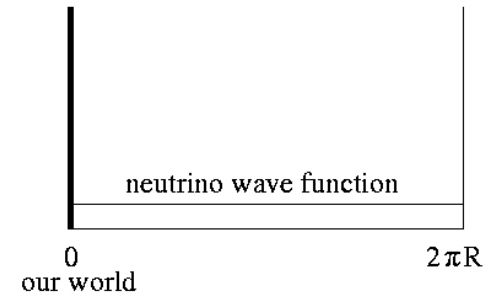
$\Lambda_F \equiv$ scale of flavour physics [unknown at present]

$E \approx \Lambda_F$ a four-dimensional description of particle interactions might break down

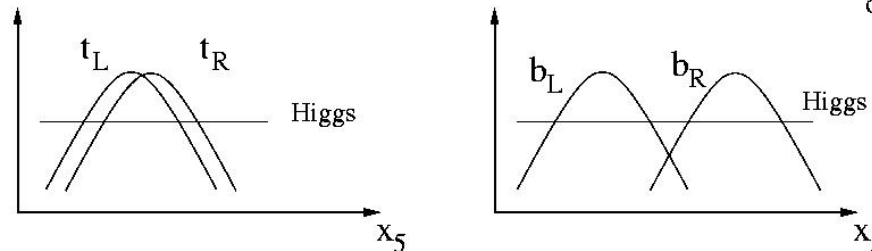
❖ Large Extra Dimensions

$$\frac{y_{\nu_e}}{y_e} \approx \frac{1}{\sqrt{2\pi R \Lambda}} \ll 1 \quad \text{if } R \gg \frac{1}{\Lambda}$$

flat zero mode for ν^c



❖ localized fermion zero modes



❖ Yukawa coupling in string theory

matter as twisted states in orbifold compactification of heterotic string

matter from intersecting D branes in type IIA strings

$$y_{ij} = e^{-A_{ij}}$$

Ibanez; Hamidi, Vafa; Dixon, Friedan, Martinec, Shenker; Casas, Munoz; Cremades, Ibanez, Marchesano; Abel, Owen

- it could provide an explanation to $N_g = 3$
- relation to flavour symmetries possible but not straightforward
- connection with data unclear, worth to explore

extra dimension could be tiny

Alternative origin of small neutrino masses

- If $\Lambda \gg \langle H \rangle$ is not the reason of the smallness of neutrino masses \Rightarrow small couplings
- Example: Dirac neutrinos

$$\lambda \nu_c LH \rightarrow m_\nu = \lambda v \quad (\text{as for the other fermions})$$

need $\lambda < 10^{-11}$ and $M_R \ll \langle H \rangle$

- Example: additional light sterile neutrinos
 - Also not protected by the electroweak symmetry
 - LSND?
 - A small mixing (independent of LSND) can be probed at a nufact

□ 3 active neutrinos $N = 2.984 \pm 0.009$ $(m_t, m_H) = (174.3, 115)$ GeV
 (invisible Z width)

□ all experiments but LSND explained by 3 ν_a
 LSND \rightarrow 3 ν_a + [at least] 1 ν_s

□ inclusion of ν_s worsens the fits

❖ solar: $\nu_e \rightarrow \sin^2 \vartheta_s \nu_s + \dots$ $\sin^2 \vartheta_s < 0.1$ (1σ) [Bahcall&Pena-Garay 2003]

❖ atm: $\nu_\mu \rightarrow \nu_\tau$ favoured over $\nu_\mu \rightarrow \nu_s$
 - zenith angle dependence of high-energy ν_μ [SK,MACRO] 3σ
 (no matter effects for ν_s)
 - no NC interactions for ν_s [SK]
 - τ -like CC events [SK] 2σ

❖ 2+2 and 3+1 fits have a poor quality [Cirelli,Marandella,Strumia,Vissani 2004]

□ WMAP + LSS $\sum m_\nu < 1.4$ eV (95% CL) for $3\nu_a + 1\nu_s$

[Hannestad&Raffelt 2004
 Crotty, Lesgourgues, Pastor 2004]

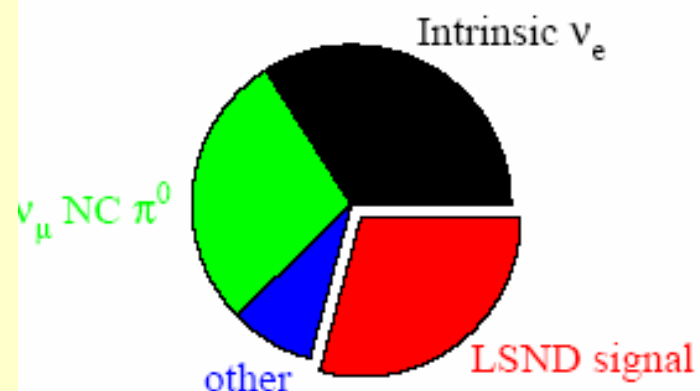
□ LSND soon checked by MiniBooNE (1st event September 2002)

no room for LSND with 3 ν_a (CPT violation disfavoured by now)

[Pakvasa&Valle 0301061, Barenboim, Borissov, Lykken 0212116]

MiniBooNE $\nu_\mu \rightarrow \nu_e$ Search

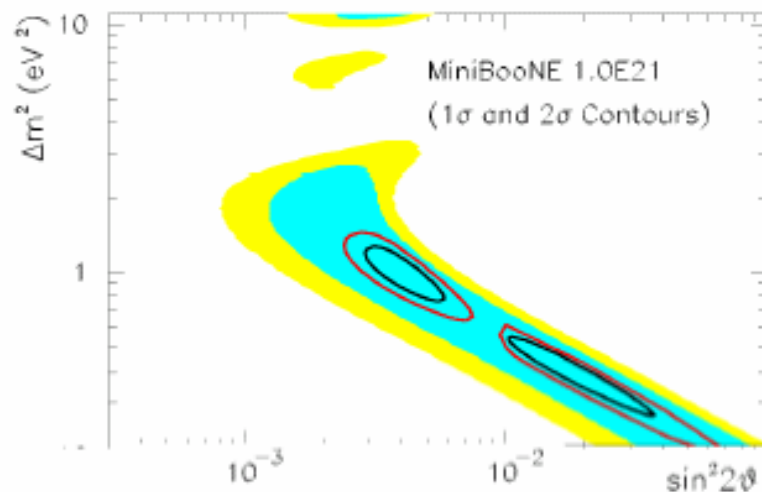
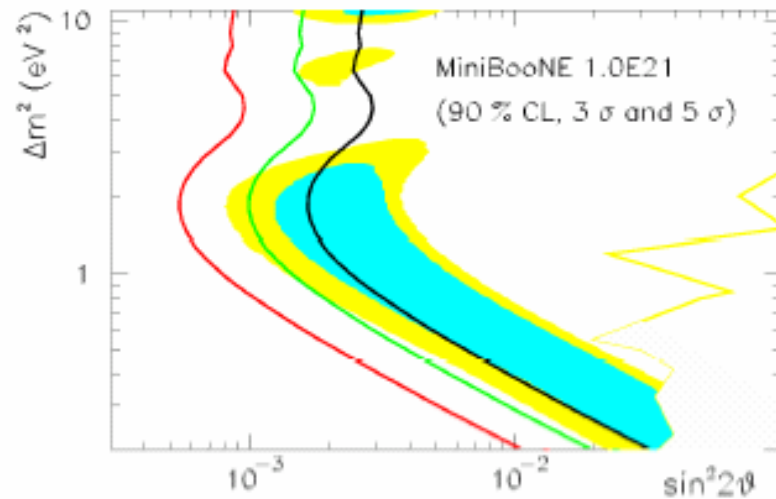
- **Goal:** Confirm or refute in a **definitive** and **independent** way the LSND evidence for $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillations
- **Challenge:** $\langle P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \rangle_{\text{LSND}} = (0.264 \pm 0.067 \pm 0.045)\%$, a small number!!
- **Signal and backgrounds:**
Expectations for 10^{21} protons on target (currently: $N_{\text{pot}} = 5.5 \cdot 10^{20}$, $dN_{\text{pot}}/dt = 0.08 \cdot 10^{20}/\text{week}$)



- $\simeq 300$ signal events (if LSND is correct)
- $\simeq 700$ background events
- Intrinsic ν_e component in the beam and ν_μ NC π^0 production are main backgrounds
- Signal and backgrounds have different energy distributions

Oscillation Sensitivity: Null and Positive Scenarios

- Fit energy distribution to extract signal. Estimates based on 10^{21} pot



Null MiniBooNE result:

- 4 σ sensitivity to entire LSND 90% CL allowed region
- Combined analysis of MiniBooNE + LSND would show incompatibility at 99% CL, in CP and CPT-conserving scenarios

MiniBooNE confirms LSND:

- Should see $> 5\sigma$ excess at LSND central value
- Distinguish 1 eV² from 0.4 eV² at 2 σ

New physics effects?

$$\mathcal{L}_{SM}^{\text{eff}} = \mathcal{L}_{SM}^{\text{ren}} + \frac{h_{ij}}{\Lambda} (H L_i)(H L_j) + \dots$$

Can we see additional effects independent of oscillations and neutrino masses?

New physics in neutrino oscillations

- Solar

Wolfenstein, Valle, Fukugita Yanagida, Roulet, Guzzo Masiero Petcov, Barger Phillips Whisnant, Degl'Innocenti Ricci, Fogli Lisi, Krastev Bahcall, Bergmann, Bergmann, Berezhiani, Raghavan, Rossi

- Atmospheric

Ma Roy, Brooijmans, Gonzalez-Garcia et al, Lipari Lusignoli, Fornengo et al, Bergmann Grossman Pierce

- LSND

Bergmann Grossman

- Supernovae

Mansour Kuo, Bergmann Kagan, Fogli et al

- Accelerators

- production, detection

Bueno et al, Bigi et al, Formaggio et al, Datta et al, Gonzalez-Garcia et al, Ota Sato Yamashita

- propagation in matter

Ota Sato Yamashita, Gago, Huber Valle, Huber Schwetz Valle

gives rise to an unmistakable signal at high energy

Campanelli AR

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Enhancement of NP effects at high energy

$$\nu_\alpha f \rightarrow \nu_\beta f \Rightarrow V_{\alpha\beta} = \varepsilon_{\alpha\beta} V_{\text{MSW}} \quad (f = u, d, e)$$

$$M_{\text{eff}}^2 = \Delta m_{32}^2 \begin{pmatrix} s_{13}^2 + (E/E_{\text{res}})(1 + \varepsilon_{ee}) & s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{e\mu} & s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{e\tau} \\ s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{\mu e} & 1/2 + (E/E_{\text{res}})\varepsilon_{\mu\mu} & 1/2 + (E/E_{\text{res}})\varepsilon_{\mu\tau} \\ s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{\tau e} & 1/2 + (E/E_{\text{res}})\varepsilon_{\tau\mu} & 1/2 + (E/E_{\text{res}})\varepsilon_{\tau\tau} \end{pmatrix}$$

$$E_{\text{res}} \approx 8 \text{ GeV} \left(\frac{\Delta m_{31}^2}{2 \times 10^{-3} \text{ eV}^2} \right) \left(\frac{1.65 \text{ g/cm}^3}{\rho Y_e} \right), \quad \Delta m_{21}^2 = 0, \quad \theta_{23} = \frac{\pi}{4}$$

The MSW term and the new effects are enhanced at large E/E_{res}

$$\text{if } \varepsilon_{\alpha\beta} = 0: \quad \theta_{\alpha\beta} \rightarrow 1/E \quad P_{\alpha\beta} \rightarrow 1/E^2 \quad \text{at } E \gg E_{\text{res}}$$

$$\text{if } \varepsilon_{\alpha\beta} \neq 0: \quad \theta_{\alpha\beta} \rightarrow \text{const} \quad P_{\alpha\beta} \rightarrow 4\varepsilon_{\alpha\beta}^2 \sin^2(LV/2) \quad \text{at } E \gg E_{\text{res}}$$

FCI-oscillation confusion theorem

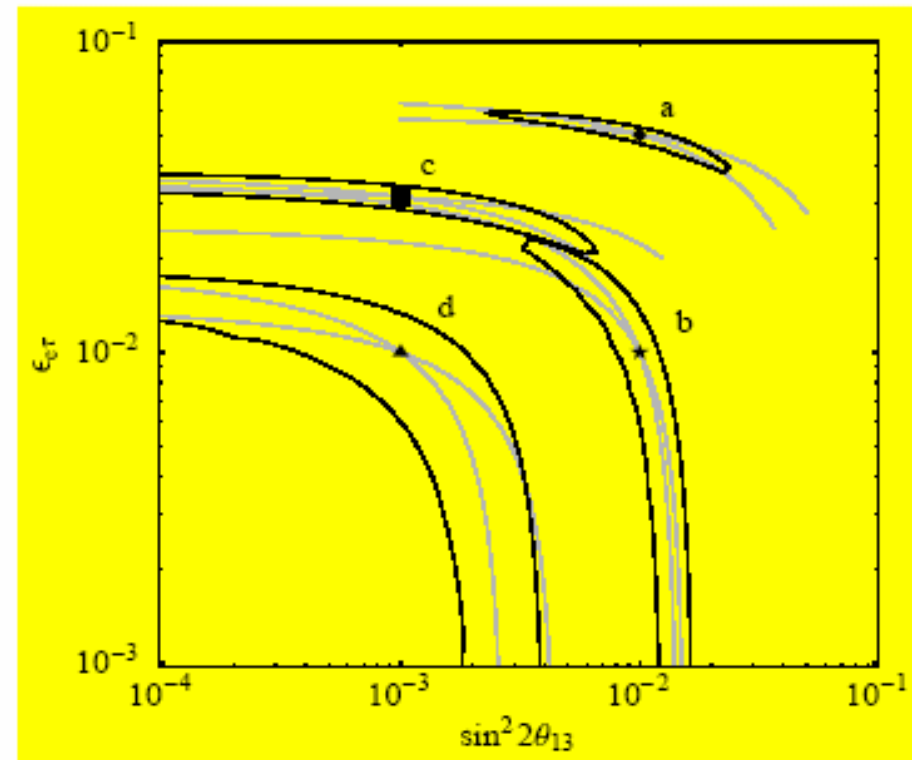


a neutrino factory is less sensitive to θ_{13} because non-standard neutrino interactions are confused with oscillations

Huber et al, PRL88 (2002) 101804

near-site programme essential

2×10^{20} mu/yr/polarity \times 5 yr, 40 kt magn iron calorim, 10% muon E-resoln above 4 GeV



However: enhancement of NP effects at high energy

$$\nu_\alpha f \rightarrow \nu_\beta f \Rightarrow V_{\alpha\beta} = \varepsilon_{\alpha\beta} V_{\text{MSW}} \quad (f = u, d, e)$$

$$M_{\text{eff}}^2 = \Delta m_{32}^2 \begin{pmatrix} s_{13}^2 + (E/E_{\text{res}})(1 + \varepsilon_{ee}) & s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{e\mu} & s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{e\tau} \\ s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{\mu e} & 1/2 + (E/E_{\text{res}})\varepsilon_{\mu\mu} & 1/2 + (E/E_{\text{res}})\varepsilon_{\mu\tau} \\ s_{13}/\sqrt{2} + (E/E_{\text{res}})\varepsilon_{\tau e} & 1/2 + (E/E_{\text{res}})\varepsilon_{\tau\mu} & 1/2 + (E/E_{\text{res}})\varepsilon_{\tau\tau} \end{pmatrix}$$

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$$\varepsilon_{e\tau} < 0.1; \text{ dominates for } E > E_{\text{NP}} \equiv \frac{s_{13}}{\sqrt{2}\varepsilon_{e\tau}} E_{\text{res}}$$

The MSW term and the new effects are enhanced at large E/E_{res}

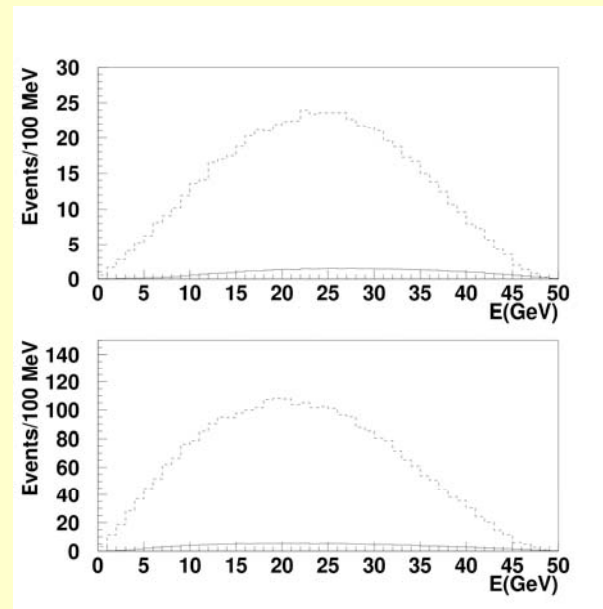
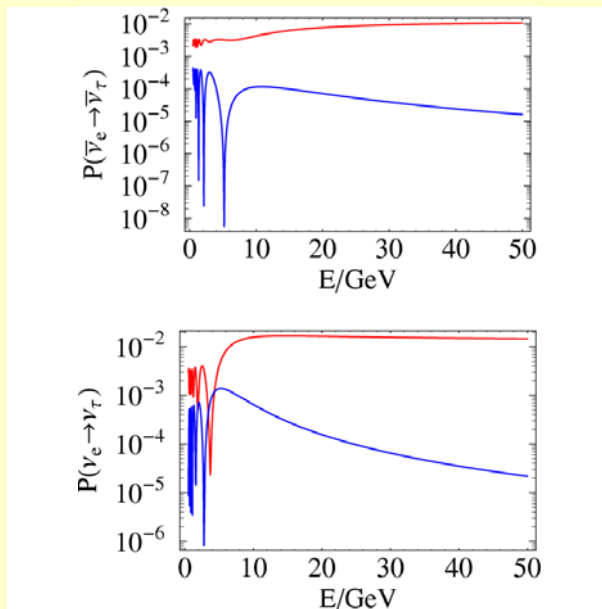
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Sensitivity at a neutrino factory

- High energy + beam purity = neutrino factory
- The high E enhancement of the ν_τ spectrum can be observed through $\tau \rightarrow \mu$ decays (BR $\sim 17\%$)
- With $E_\mu = 40 \text{ GeV}$, $L = 3000 \text{ km}$, 40 kt , the experiment would be sensitive to $\varepsilon_{e\tau} \sim 0.008$
 - e.g. for $\varepsilon_{e\tau} = 0.07$, $\sin^2(2\theta_{13}) = 10^{-3}$:

Campanelli, AR



Summary

- Neutrino precision physics goes well beyond measuring a few parameters
- It allows to address fundamental issues either directly (CP-violation, hierarchy, lepton number violation) or through "circumstantial evidence" (see-saw, origin of neutrino masses, origin of mass and mixing pattern)
- It represents one of the very few handles to address the origin of flavour.