

HADRONIC τ DECAYS INTO 2 & 3 MESON MODES WITHIN $R_{\chi T}$

Work done in collaboration with D. Gómez-Dumm, A. Pich, J. Portolés

See Phys.Rev.D69:073002,2004 ; AIP Conf.Proc.964:40-46,2007 ; Work to appear soon

YOUNG RESEARCHERS WORKSHOP
Frascati May 11th 2009

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SUMMARY:

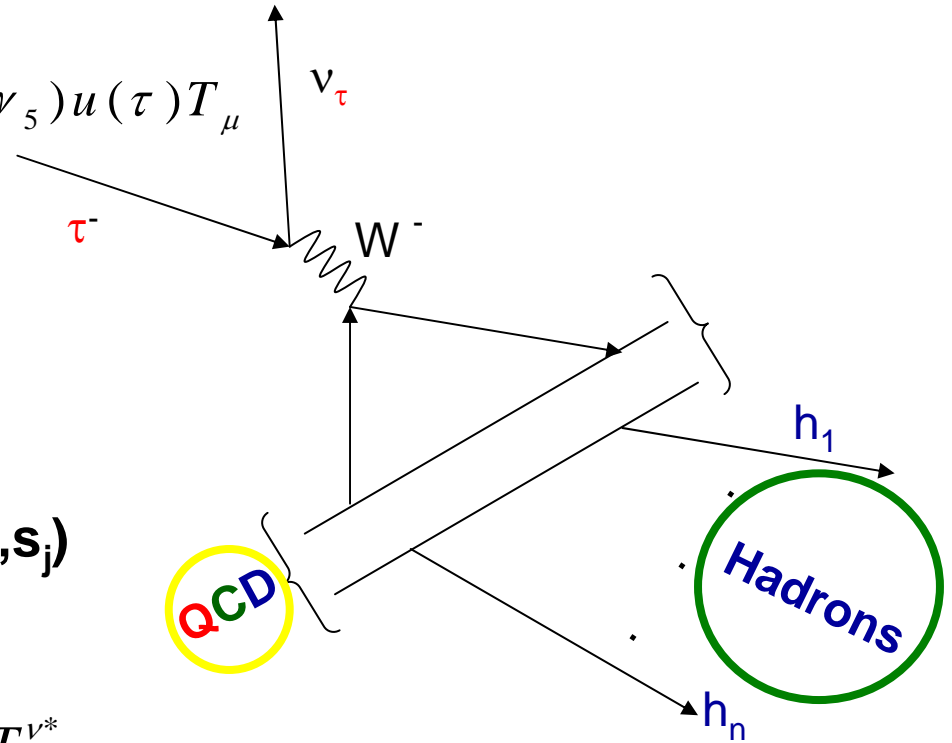
- Hadronic decays of the τ lepton
- ~~Kühn-Santamaría Model in TAUOLA~~
- **Our study:**
 1. Tools : χ PT, Large N_c , $R_\chi T$
 2. Two meson processes: $\tau^- \rightarrow (\pi \pi, \pi K)^- \nu_\tau$
 3. Three meson processes: $\tau^- \rightarrow (3\pi, KK\pi)^- \nu_\tau$
- Conclusions

HADRONIC DECAYS OF THE τ LEPTON

$$\mathfrak{M} = \frac{G_F}{\sqrt{2}} V_{CKM} \bar{u}(v_\tau) \gamma^\mu (1 - \gamma_5) u(\tau) T_\mu$$

$$T_\mu = \langle \text{Hadrons} | (V-A)_\mu e^{iS_{QCD}} | 0 \rangle = \sum_i (\text{Lorentz Structure})^i F_i(Q^2, s_j)$$

$$d\Gamma = \frac{G_F^2}{4M_\tau^2} |V_{CKM}|^2 d\Phi^{(n+1)} L_{\mu\nu} T^\mu T^{\nu*}$$

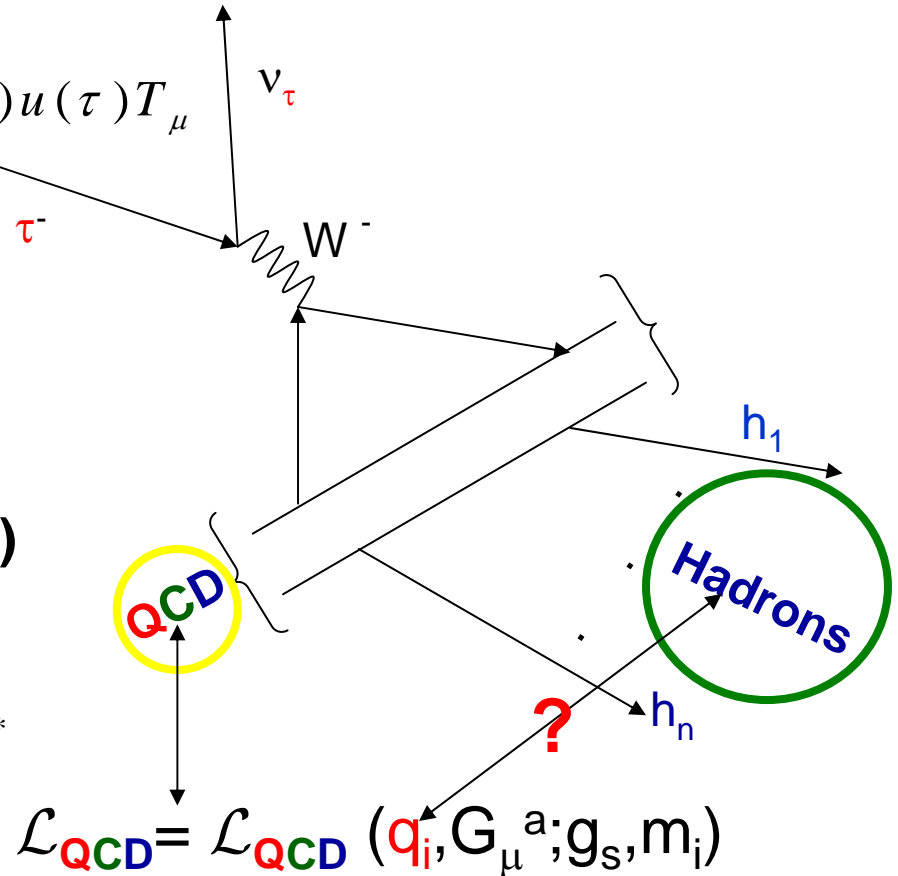


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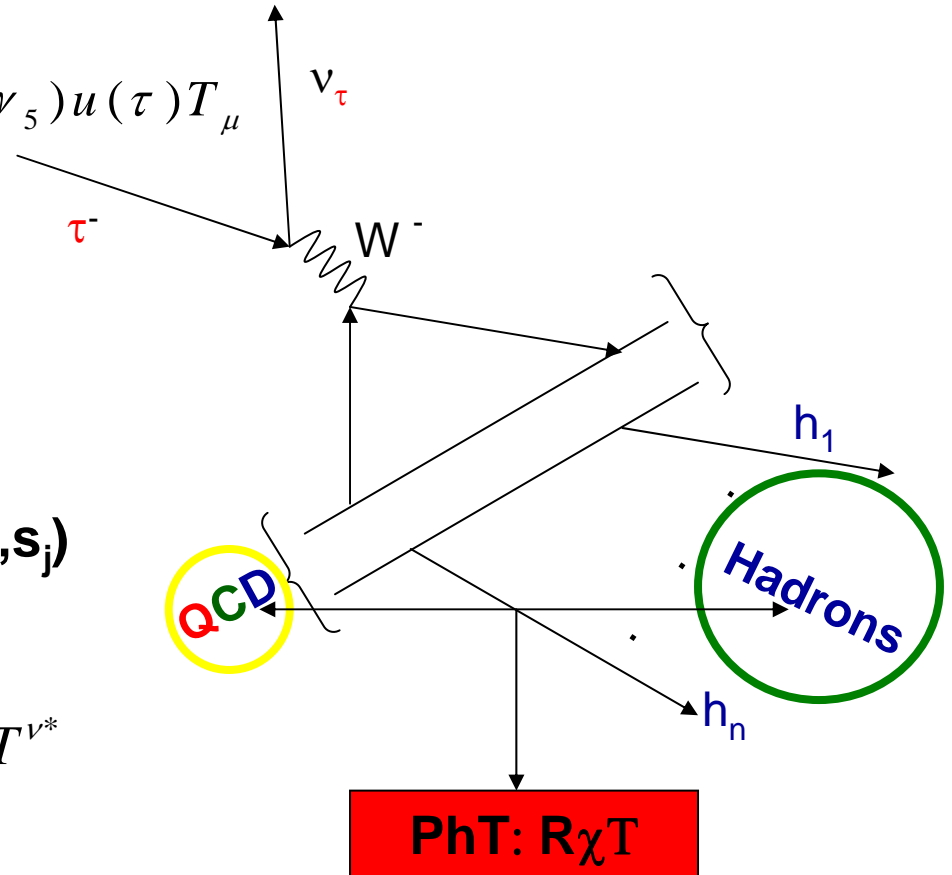
$$\mathcal{L}_{QCD} = \mathcal{L}_{QCD}(q_i, G_\mu^a, g_s, m_i)$$

HADRONIC DECAYS OF THE τ LEPTON

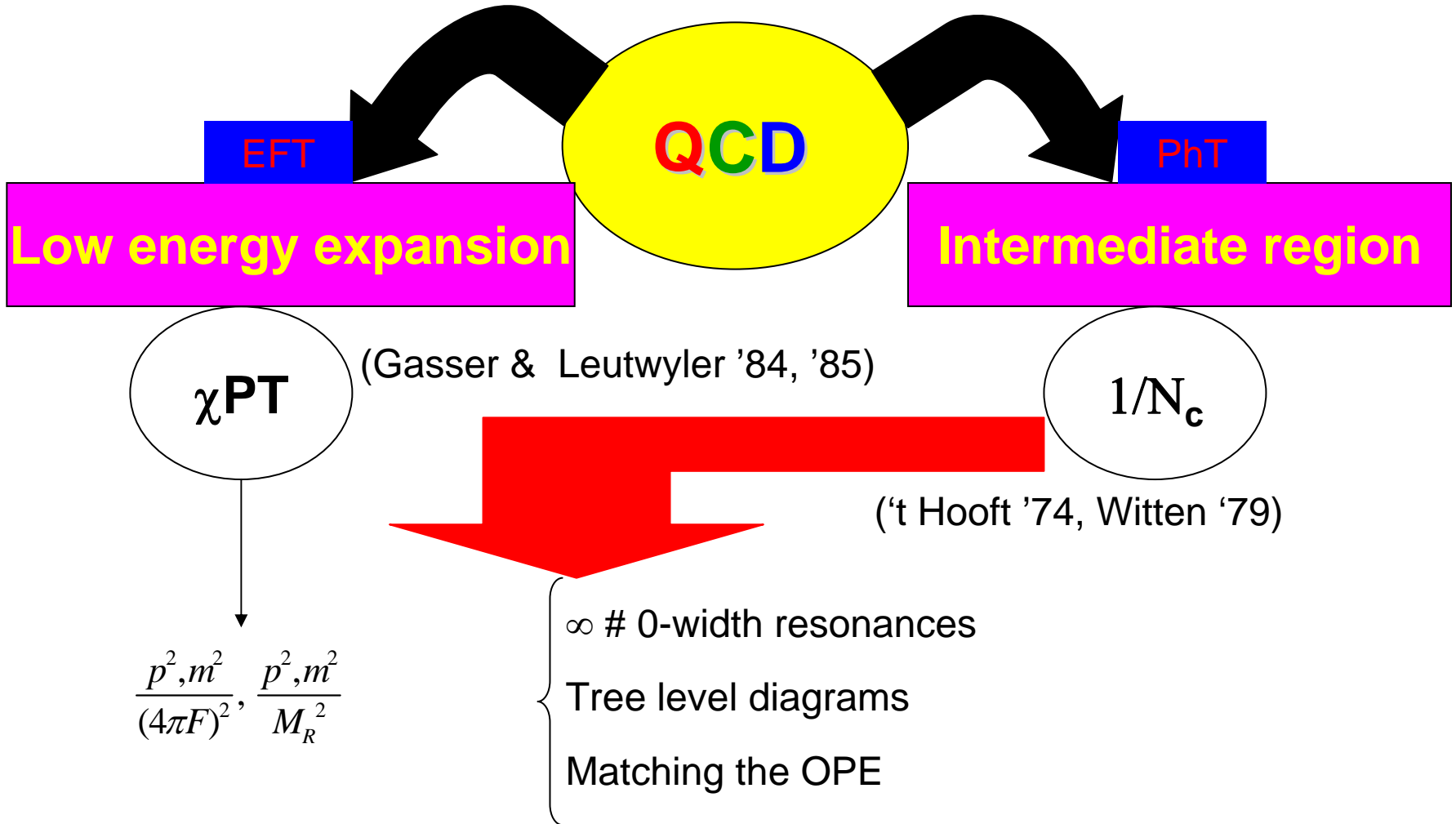
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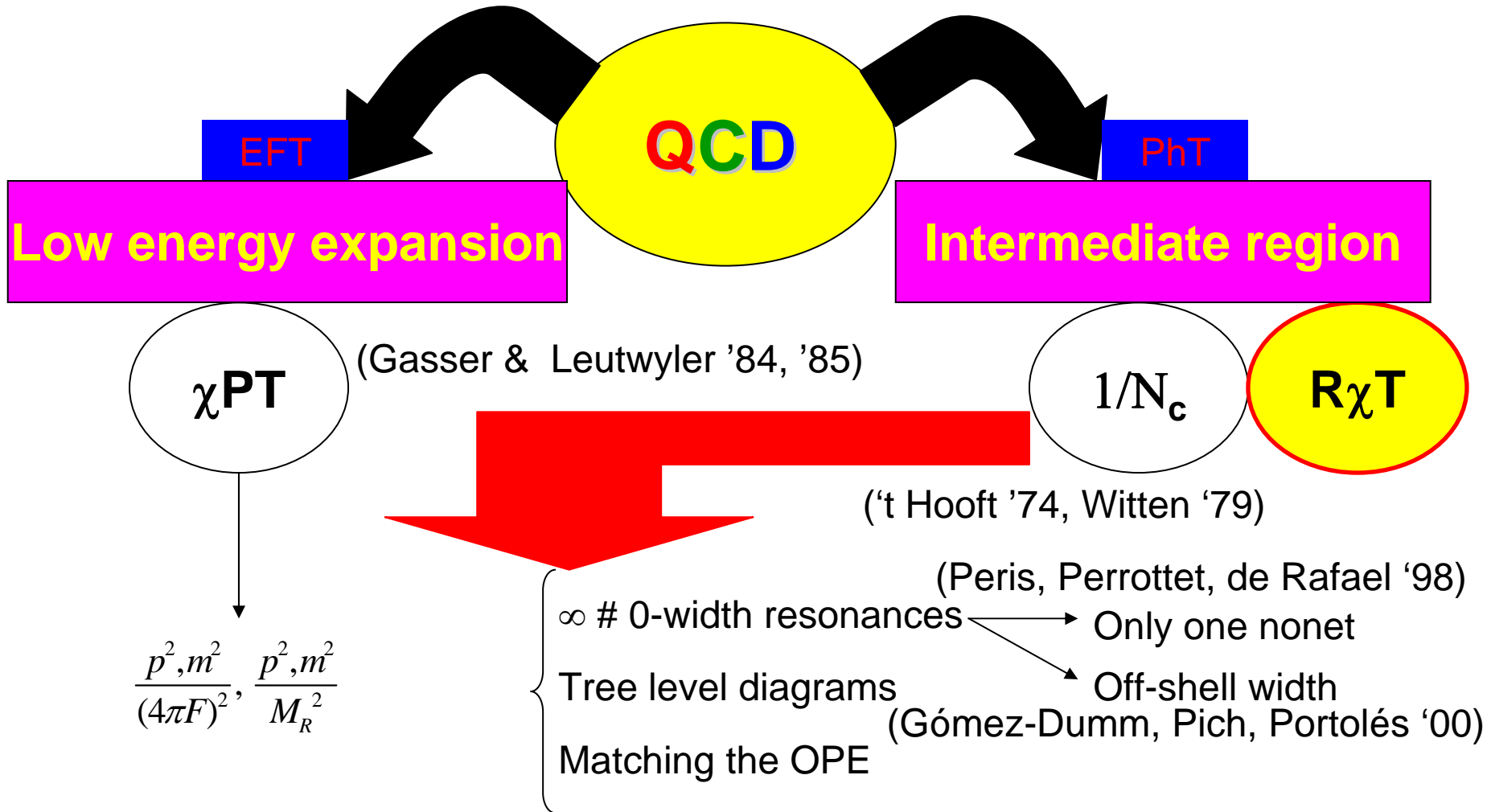
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TOOLS: χ PT, Large N_c , $R\chi T$



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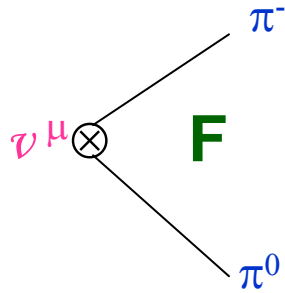
Two meson processes: $\tau^- \rightarrow (\pi \pi)^- \nu_{\tau}$

A long story of successes in VFF of $\pi \pi$: See complete Bibliography in (Portolés, '05)

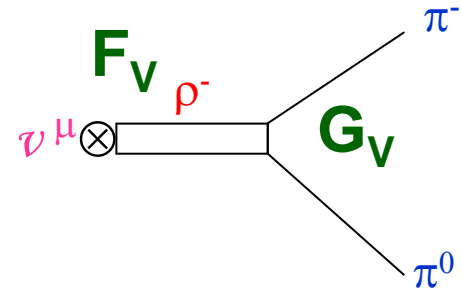
$$\langle \pi^- \pi^0 | \bar{d} \gamma^\mu u | \emptyset \rangle = \sqrt{2} F(s) (p_{\pi^-} - p_{\pi^0})^\mu$$

$\underline{\tau}^- \rightarrow (\underline{\pi \pi})^- \underline{\nu}_{\underline{\tau}}$ (Ecker, Gasser, Pich, De Rafael '89)

$$\langle \pi^- \pi^0 | \bar{d} \gamma^\mu u | 0 \rangle = \sqrt{2} F(s) (p_{\pi^-} - p_{\pi^0})^\mu$$



$$F(s) = 1 + \frac{F_V G_V}{F^2} \frac{s}{M_V^2 - s}$$

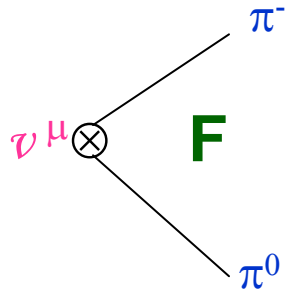


$$F(s) \xrightarrow{s \rightarrow \infty} \frac{const}{s} \Rightarrow F_V G_V = F^2$$

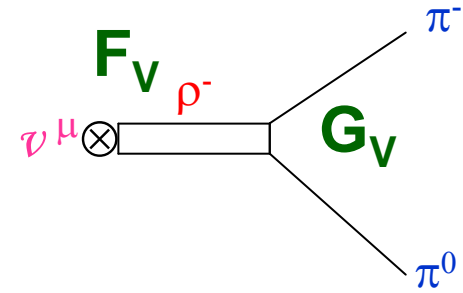
$$F(s)^{VMD} = \frac{M_\rho^2}{M_\rho^2 - s}$$

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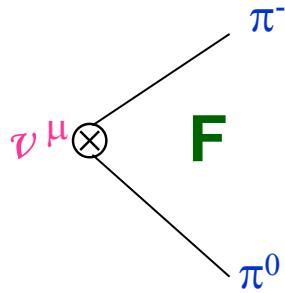


(Gasser & Leutwyler '84, '85)

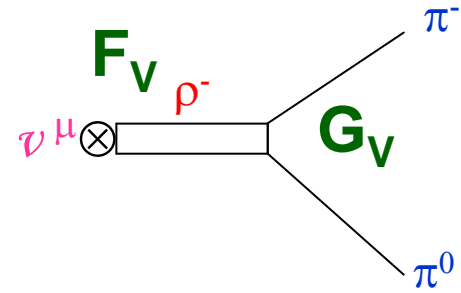
$$F(s)^{\text{ChPT}} = 1 + \frac{2L_9^r(\mu)}{f_\pi^2} s - \frac{s}{96\pi^2 f_\pi^2} \left[A(m_\pi^2/s, m_\pi^2/\mu^2) + \frac{1}{2} A(m_K^2/s, m_K^2/\mu^2) \right]$$

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(Guerrero, Pich '97)

$\mathcal{O}(p^4)$ χ PT Omnès resummed

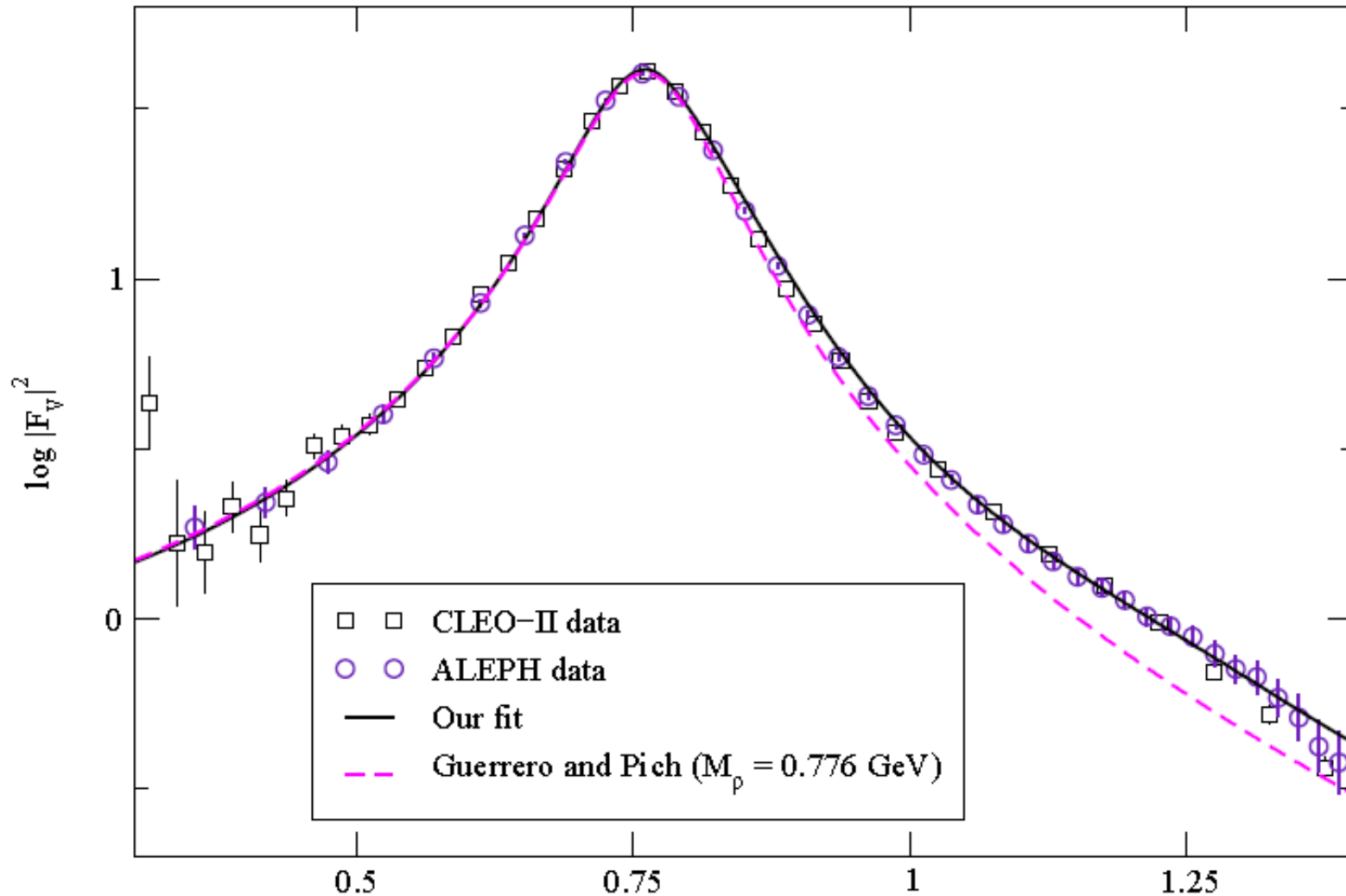
$$F(s)^{R\chi T} = \frac{M_\rho^2}{M_\rho^2 - s - iM_\rho \Gamma_\rho(s)} \exp \left\{ \frac{-s}{96\pi^2 F^2} \left[\Re A \left(\frac{m_\pi^2}{s}, \frac{m_\pi^2}{M_\rho^2} \right) + \frac{1}{2} \Re A \left(\frac{m_K^2}{s}, \frac{m_K^2}{M_\rho^2} \right) \right] \right\}$$

HADRONIC τ DECAYS WITHIN $R\chi T$
Pablo Roig (INFN)

(Guerrero, Pich '97)



(Pich, Portolés '01, '03)



\sqrt{s} (GeV)

HADRONIC τ DECAYS WITHIN $R_{\chi T}$

Pablo Roig (INFN)

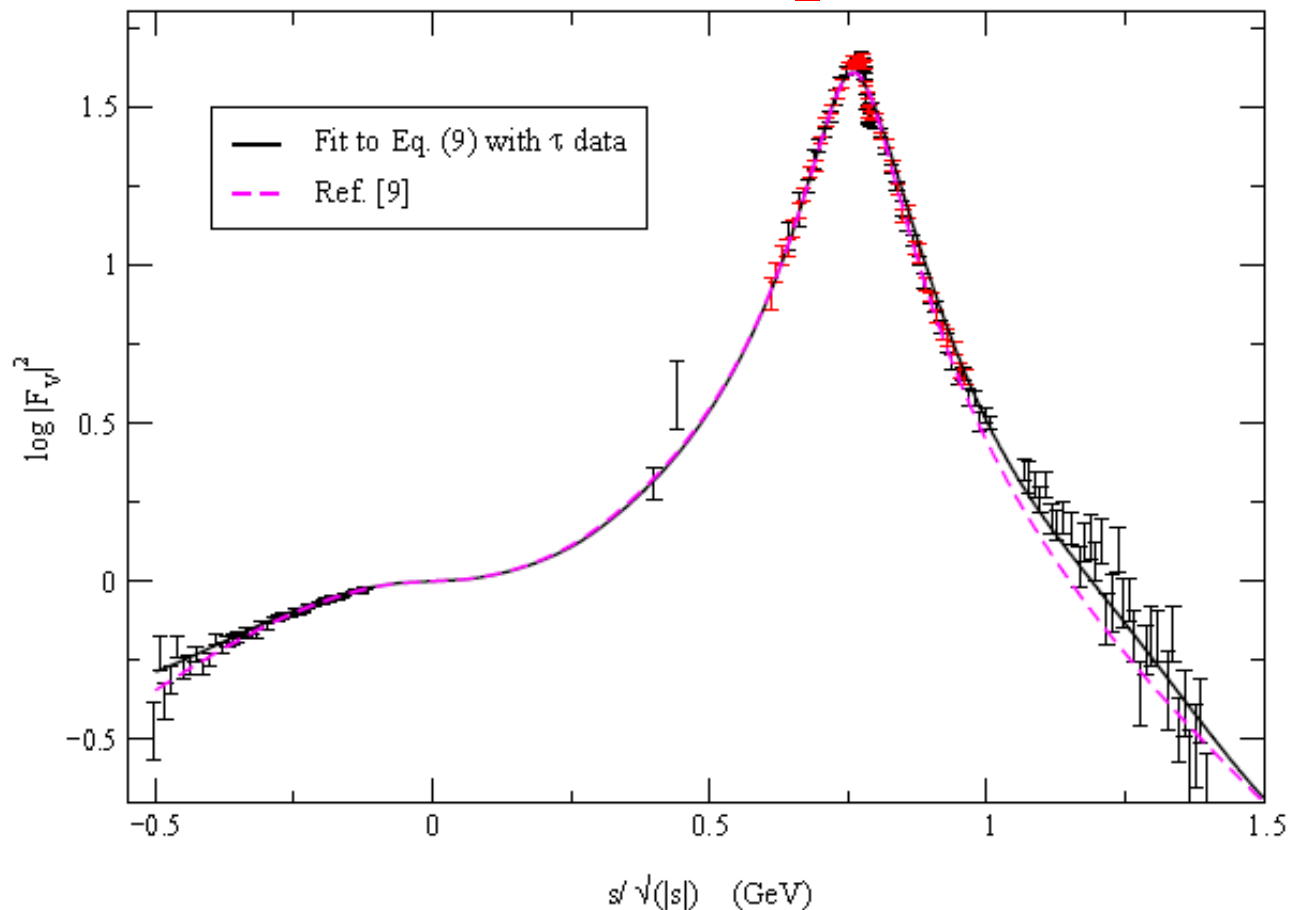


Figure 2: Comparison of the result of our fit with the experimental data on $F_V(s)$ from $e^+e^- \rightarrow \pi^+\pi^-$ (time-like) [15] and $e^-\pi^\pm \rightarrow e^-\pi^\pm$ (space-like) [16]. The result of Ref. [9] ($M_\rho = 775$ MeV) is also shown. In the region $-0.4 \text{ GeV} \lesssim s/\sqrt{|s|} \lesssim 0.8 \text{ GeV}$ both curves are almost indistinguishable.

HADRONIC τ DECAYS WITHIN $R_{\chi T}$

Two meson processes: $\tau^- \rightarrow (\mathbf{K} \pi)^- \nu_\tau$

$$\langle \pi^-(p_2) K_S(p_1) | V_\mu e^{iL_{QCD}} | 0 \rangle = \frac{1}{\sqrt{2}} \left[\left(q_\mu - \frac{m_K^2 - m_\pi^2}{Q^2} Q_\mu \right) \underbrace{F_+^{K\pi}(q^2)}_{J^P=1^-} + Q_\mu \underbrace{F_0^{K\pi}(q^2)}_{J^P=0^+} \right]$$

$$q_\mu = (p_1 - p_2)_\mu, \quad Q_\mu = (p_1 + p_2)_\mu$$

$J^P=1^-$

[M. Finkemeier,
E. Mirkes, 1996]

$$\longrightarrow F_+^{K\pi}(s) = \frac{F_+^{K\pi}(0)}{1 + \beta} \left[BW_{K^*(892)}(s) + \beta BW_{K^*(1410)}(s) \right]$$

$J^P=0^+$

[D. Aston et al, 1988]

$$\longrightarrow \begin{cases} F_0^{K\pi}(s) = \lambda \frac{\sqrt{s}}{q_{K\pi}(s)} \left[\sin \delta_B e^{i\delta_B} + e^{i2\delta_B} BW_{K^*(1430)}(s) \right] \\ \cot \delta_B = \frac{1}{a q_{K\pi}(s)} + \frac{b q_{K\pi}(s)}{2} \end{cases}$$

LASS
parameterization

$$\underline{\tau^-} \rightarrow (\underline{K \pi})^- \underline{\nu_{\tau}} \quad (\text{Jamin, Pich \& Portolés, 08})$$

1) Vector form factor [M. Jamin, A. Pich, J.P., 2006]

K*(892)

↓

K*(1410)

↓

$$F_+^{K\pi}(s) = \left[\frac{M_{K^*}^2 + \gamma s}{M_{K^*}^2 - s - iM_{K^*}\Gamma_{K^*}(s)} - \frac{\gamma s}{M_{K^{**}}^2 - s - iM_{K^{**}}\Gamma_{K^{**}}(s)} \right] e^{\frac{3}{2}\text{Re}[\overline{H}_{K\pi}(s) + \overline{H}_{K\eta}(s)]}$$

Resonance Chiral Theory (R χ T)

chiral symmetry + Brodsky-Lepage asymptotic
behaviour + Large-N_C + analyticity

}

↑

1-loop χ PT
Omnès resummed

$$\underline{\tau^-} \rightarrow (\underline{K \pi})^- \underline{\nu_{\tau}} \quad (\text{Jamin, Pich \& Portolés, 08})$$

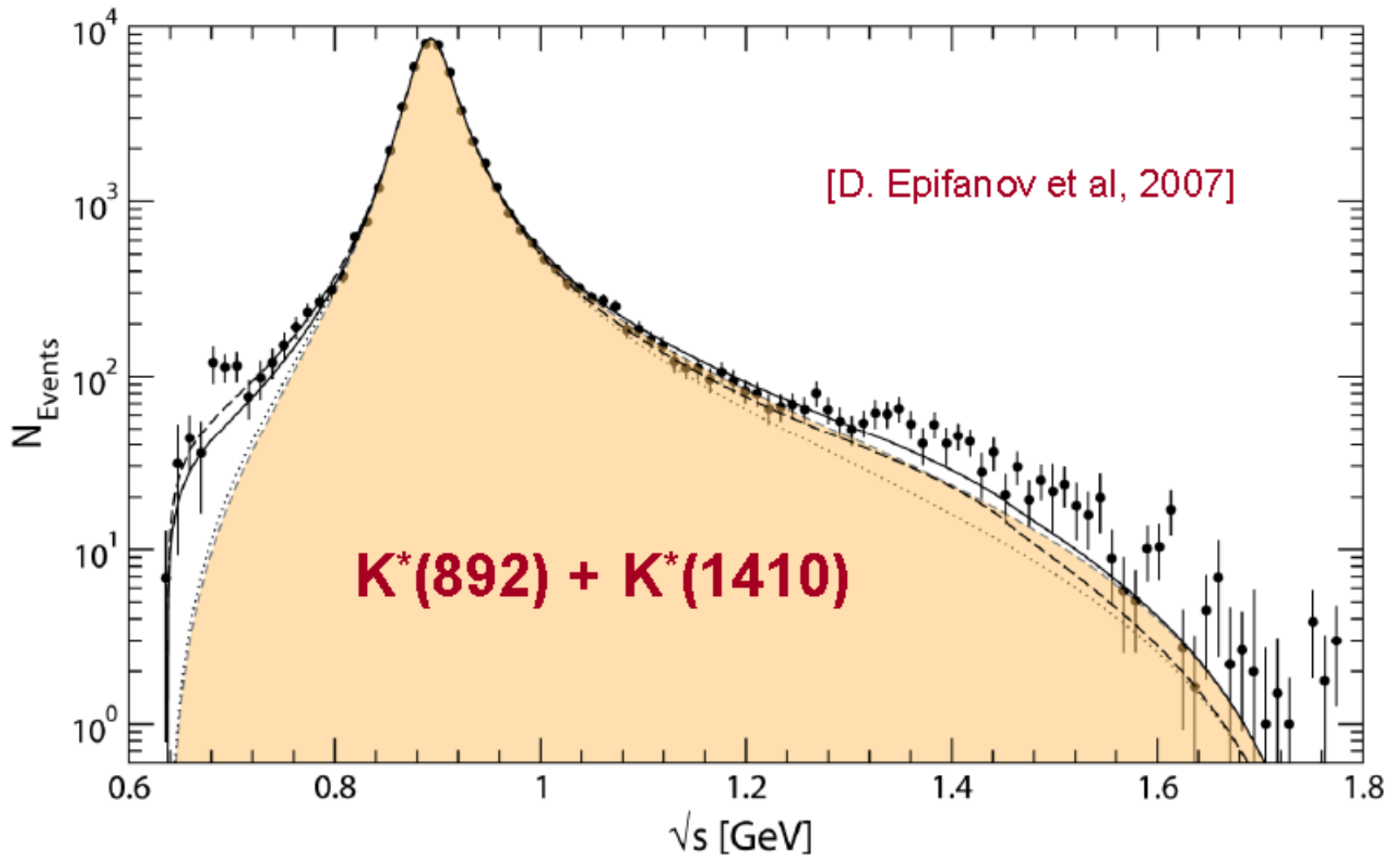
2) Scalar form factor [M. Jamin, J.A. Oller, A. Pich, 2002, 2006]

Coupled channel determination ($\underline{K\pi}$, $\underline{K\eta}$ and $\underline{K\eta'}$)

- Chiral constraints
- Resonance Chiral Theory matching
- Analyticity and unitarity strictures

$$\tau^- \rightarrow (\underline{K \pi})^- \nu_{\tau}$$

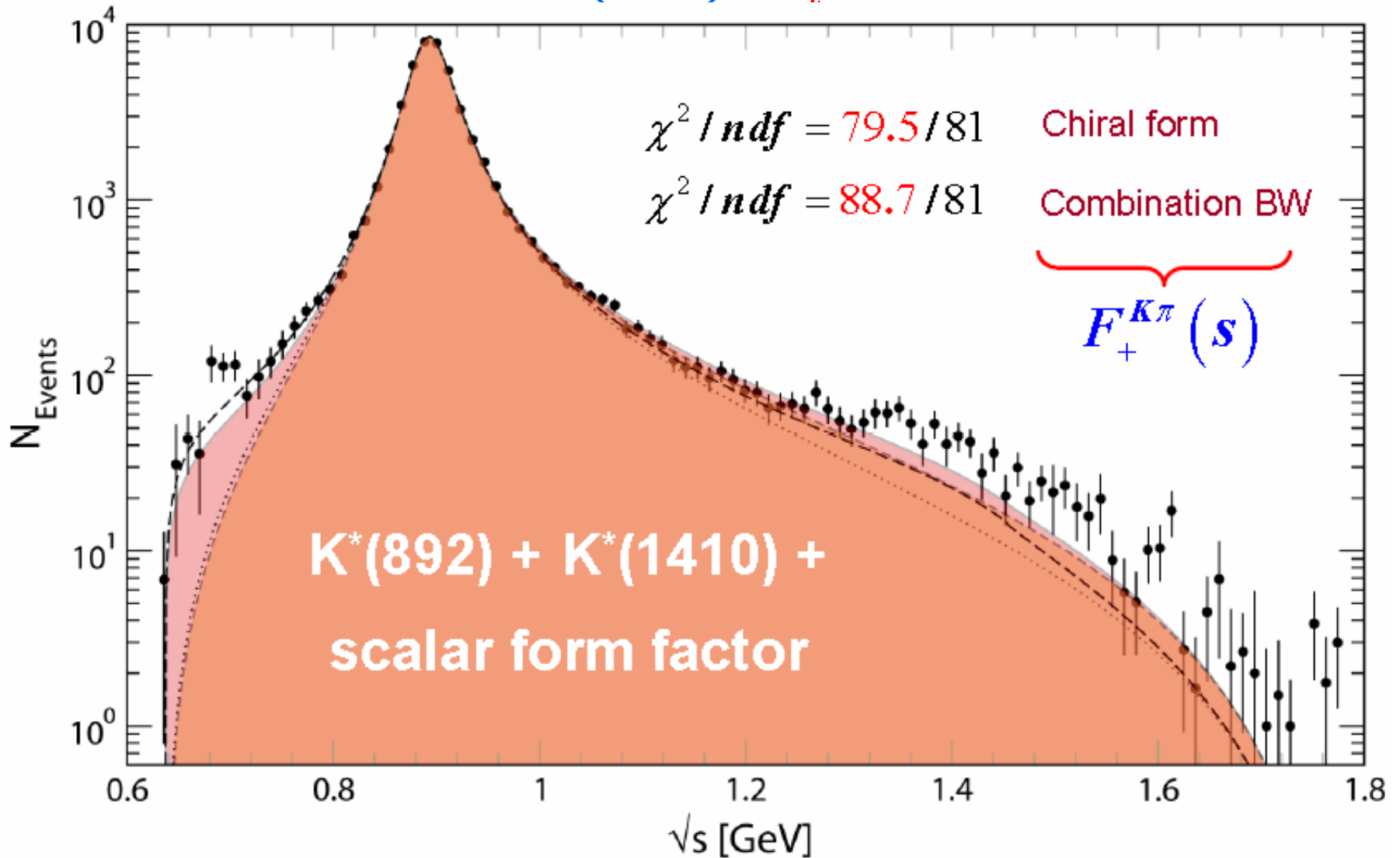
(Jamin, Pich & Portolés, 08)



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HADRONIC τ DECAYS WITHIN $R_{\chi T}$
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$\tau^- \rightarrow (K \pi)^- \nu_\tau$ (Jamin, Pich & Portolés, 08)



$$\underline{\tau^-} \rightarrow (\underline{K \pi})^- \underline{\nu_\tau} \quad (\text{Jamin, Pich \& Portolés, 08})$$

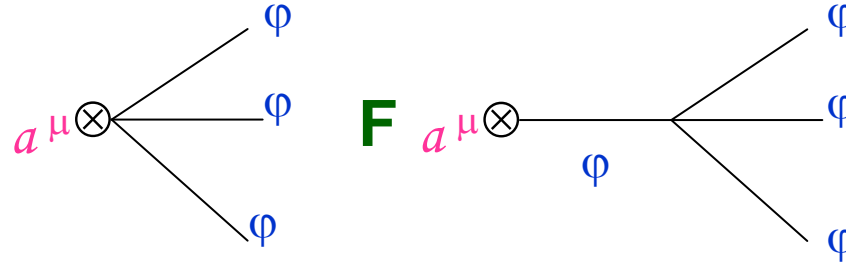
(MeV)	Our results	Our results BW combination	PDG
$M_{K^*(892)}$	895.28(20)	895.12(19)	891.66(26)
$\Gamma_{K^*(892)}$	47.50(41)	46.79(41)	50.8(9)
$M_{K^*(1410)}$	1307(17)	1598(25)	1414(15)
$\Gamma_{K^*(1410)}$	206(49)	224(47)	232(21)

Three meson processes: $\tau^- \rightarrow (3\pi)^- \nu_\tau$

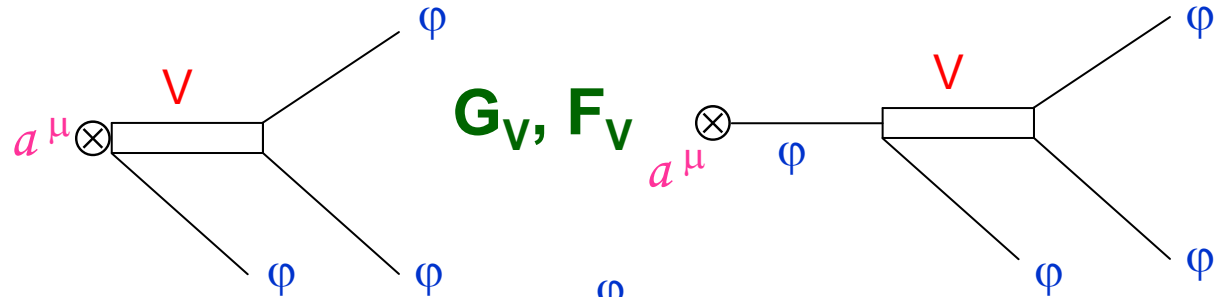
(Our work)

(Gómez-Dumm, Pich, Portolés '04)

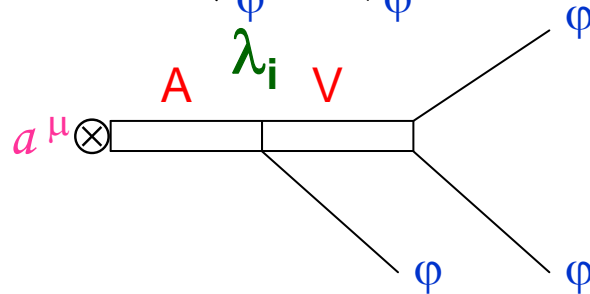
χ PT $\mathcal{O}(p^2)$



$R\chi$ T, 1R



$R\chi$ T, 2R



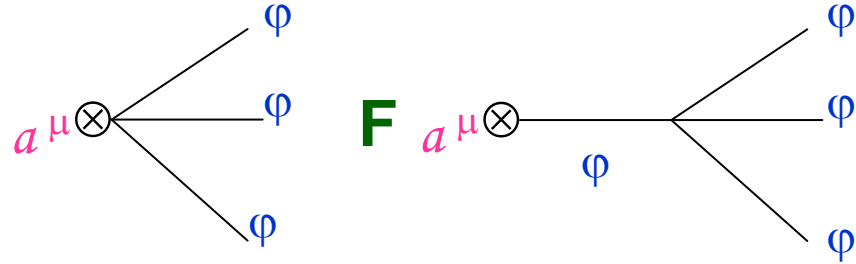
HADRONIC τ DECAYS WITHIN $R\chi$ T
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Three meson processes: $\tau^- \rightarrow (3\pi)^- \nu_\tau$

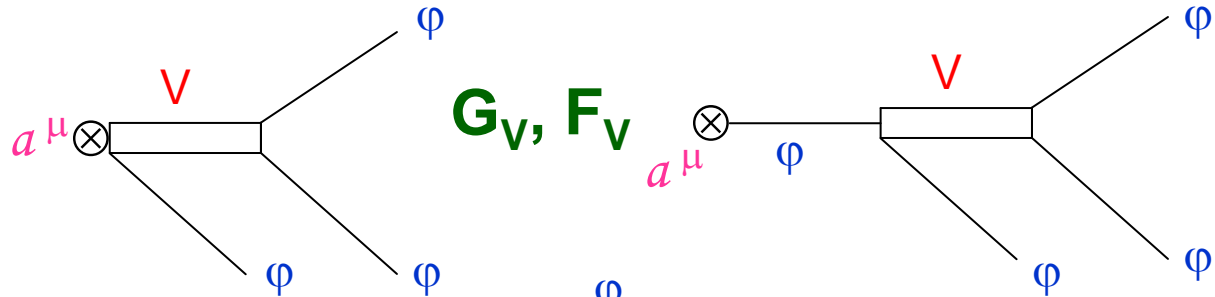
(Our work)

(Gómez-Dumm, Pich, Portolés '04)

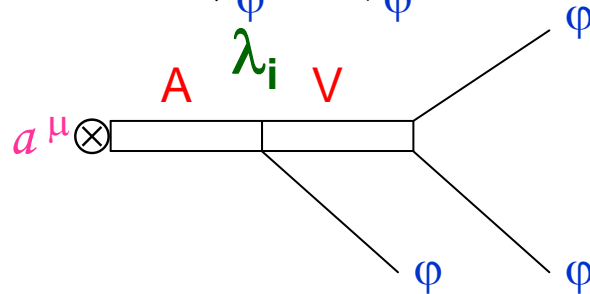
χ PT $\mathcal{O}(p^2)$



$R\chi$ T, 1R



$R\chi$ T, 2R



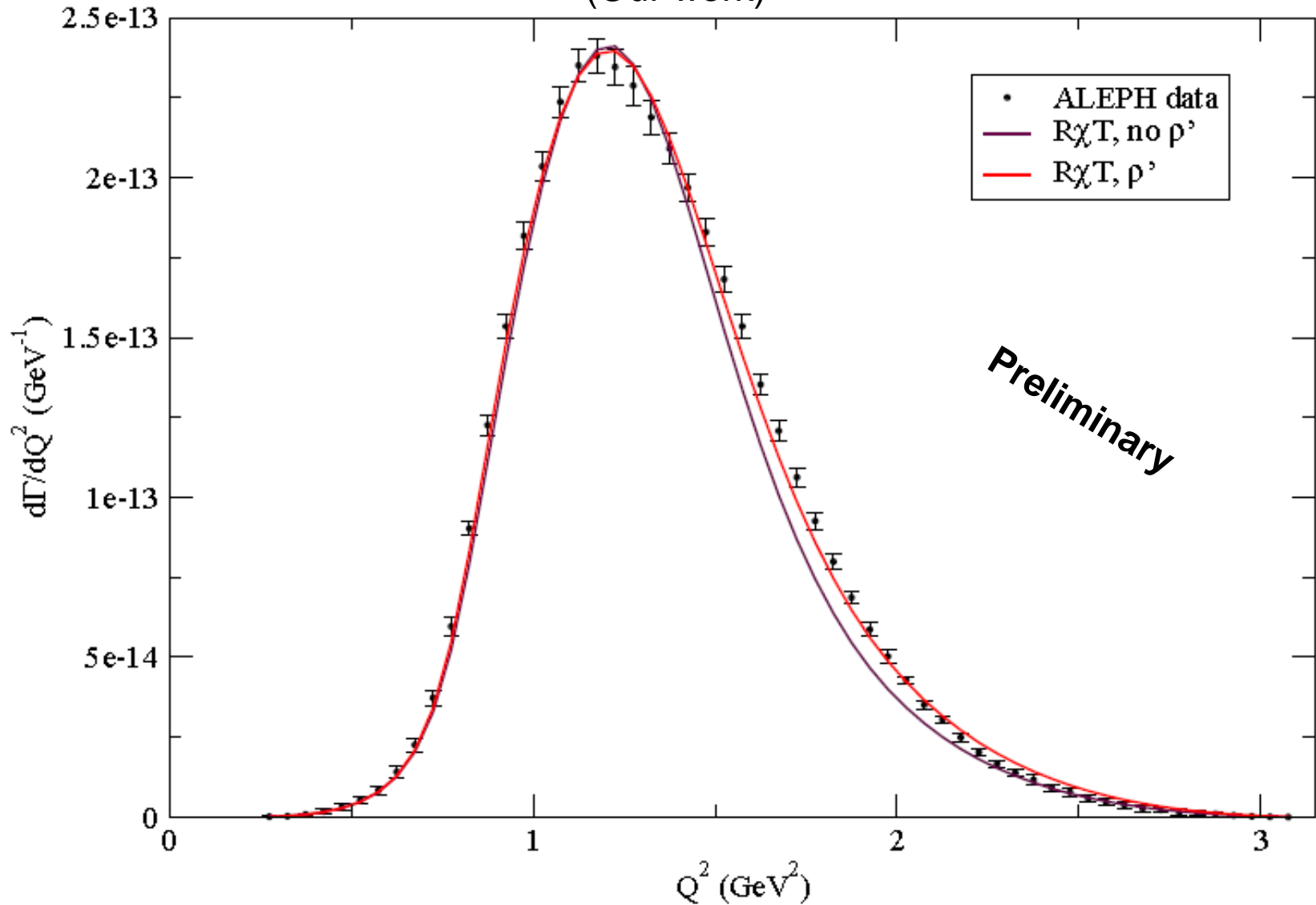
7 unknown couplings

Computation + Brodsky-Lepage demanded to the Form Factors ($7-6 = 1$ coupling).

HADRONIC τ DECAYS WITHIN $R\chi$ T
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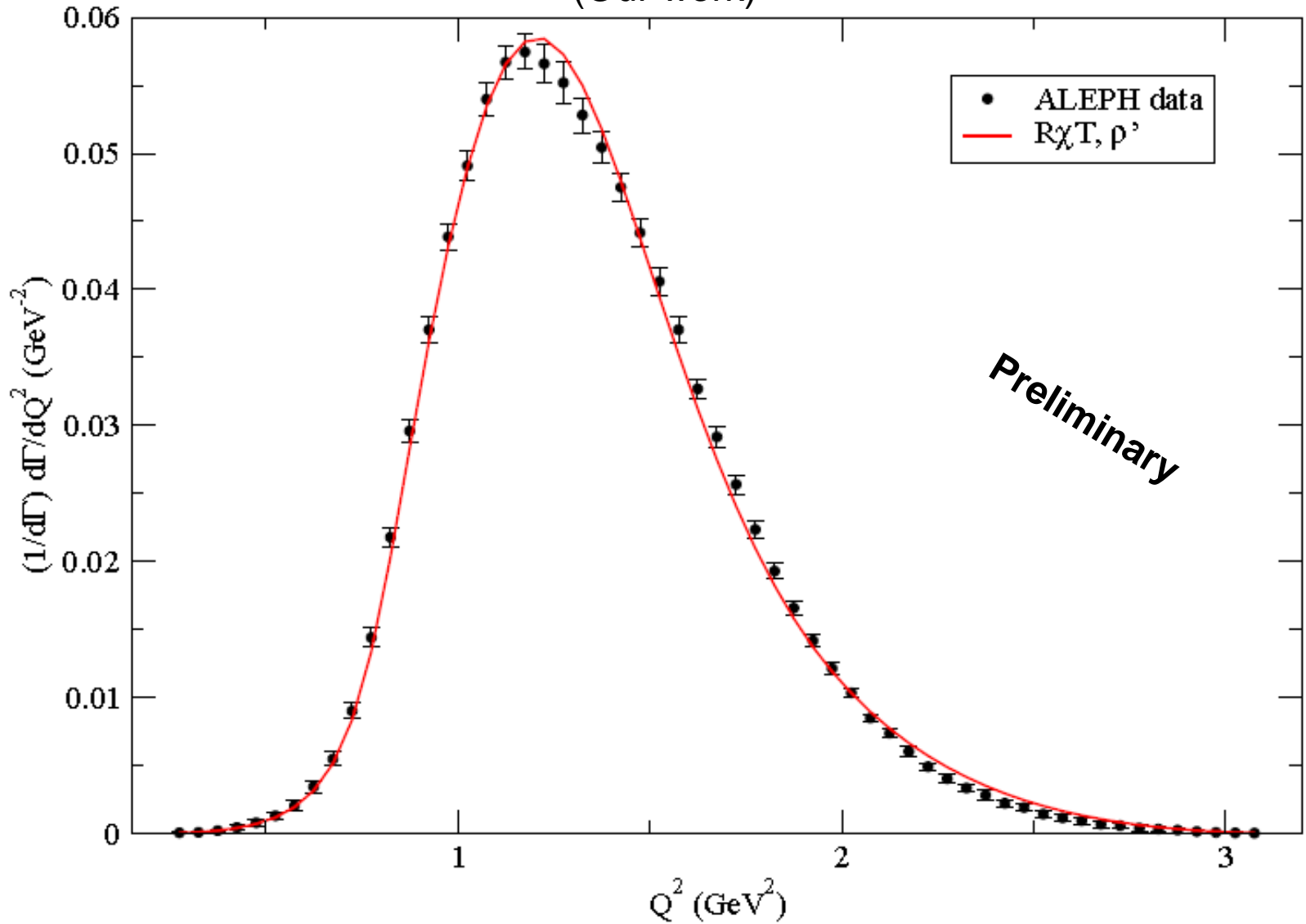
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(Our work)



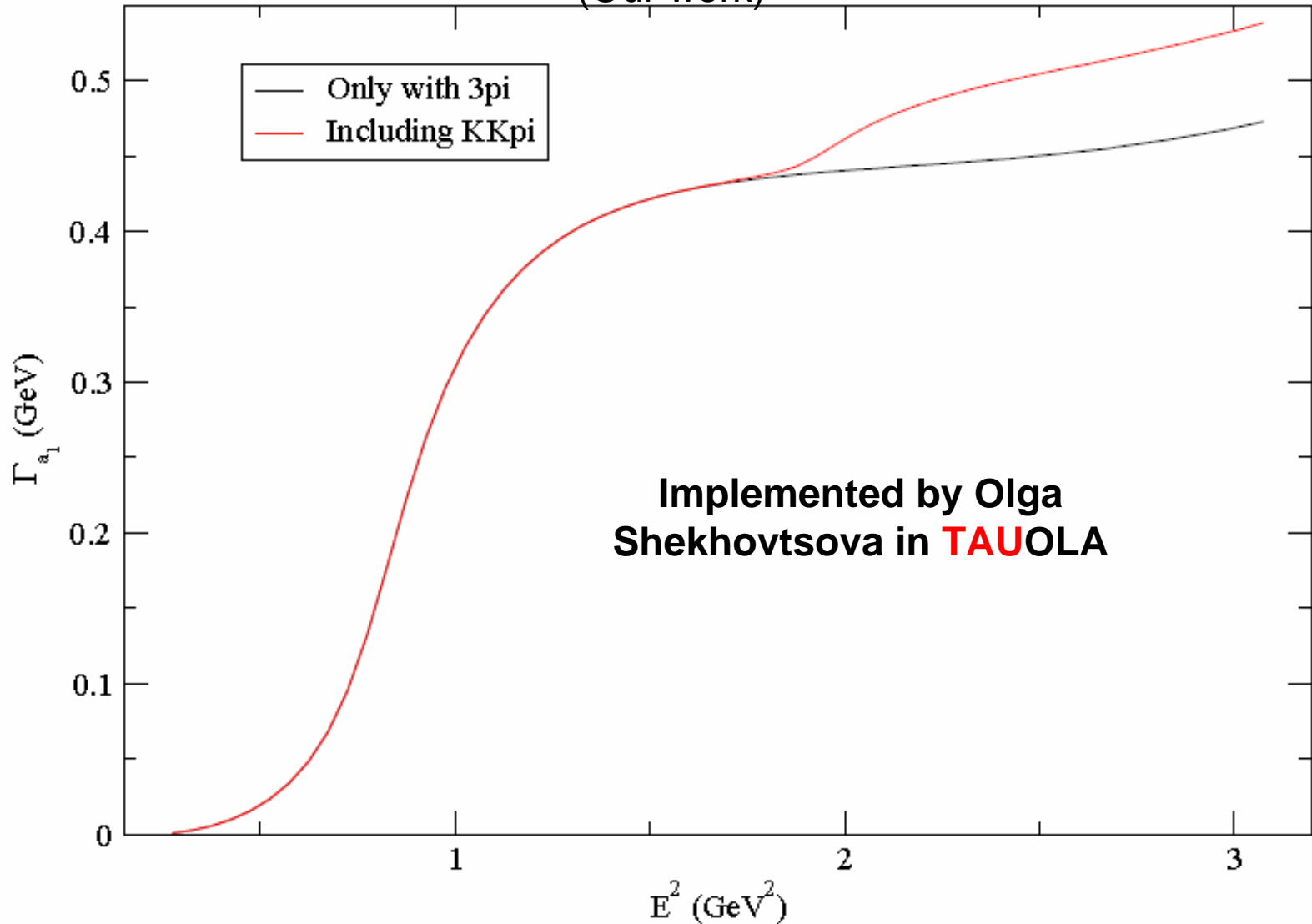
Three meson processes: $\tau^- \rightarrow (3\pi)^- \nu_\tau$

(Our work)



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(Our work)



Three meson processes: $\tau^- \rightarrow (KK\pi)^- \nu_{\tau}$ (Our work)

1. Computation of the involved process within $R_{\chi T}$ ($23-8=15$ couplings).
2. Brodsky-Lepage behaviour demanded to the Form Factors ($15-9=6$ couplings).
3. Computation and fit to $\text{Br}(\omega \rightarrow 3\pi)$ completing (Pich, Portolés, Ruiz-Femenía '03). Use of some constraints from this work for $\langle VVP \rangle$ ($6-3=3$ couplings).
4. **Axial-form factor fixed** by $\tau \rightarrow 3\pi \nu_{\tau}$ ($3-1=2$ couplings). (Gómez-Dumm, Pich, Portolés '04) (Cirigliano, Ecker, Eidemüller, Pich, Portolés '04).

Three meson processes: $\tau^- \rightarrow (KK\pi)^- \nu_\tau$ (Our work)

1. Computation of the involved process within $R\chi T$ (**23-8 = 15 couplings**).
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Trying to do it with

$$\lambda_0 \sim 1/8$$

$$\Gamma_{a_1}(Q^2) \leftarrow R\chi T$$

Three meson processes: $\tau^- \rightarrow (KK\pi)^- \nu_{\tau}$ (Our work)

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$$\lambda_0 \sim 1/8$$



$$\Gamma_{a_1}(Q^2) \leftarrow R\chi T$$

Three meson processes: $\rightarrow (KK\pi)^-\nu_\tau$ & $e^+e^- \rightarrow KK\pi$

(Our work)

1. **Vector-form factor fixed** thanks to $\text{br}(\tau \rightarrow K^+K^-\pi^-\nu_\tau)$ and $\text{br}(\tau \rightarrow K^-K^0\pi^0\nu_\tau)$ (**2-2=0 couplings**).
2. **CVC** allows to relate $e^+e^- \rightarrow KK\pi$ with $\tau^- \rightarrow (KK\pi)^-\nu_\tau$.
BaBar has recently ('07) published very precise data on $e^+e^- \rightarrow KK \pi/\eta$ using **ISR** events. Furthermore, their Dalitz-plot fit has allowed to separate cleanly the $l=0,1$ contributions, which let us check the couplings obtained in 1.

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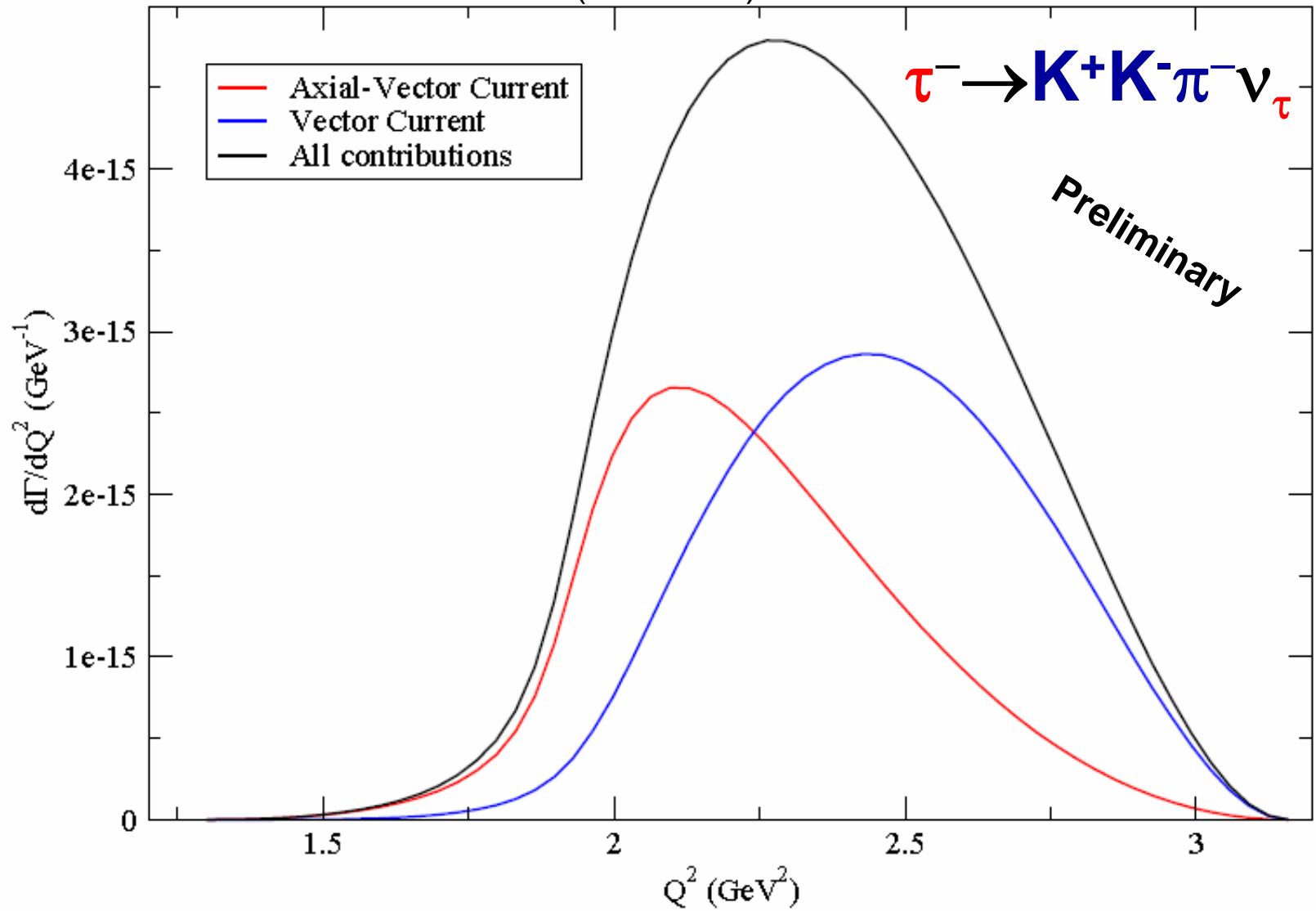
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Hence, we predict: i) the **spectra** of the $KK\pi$ modes

$$\text{ii) } (\Gamma_V/\Gamma_T) \sim 0.55$$

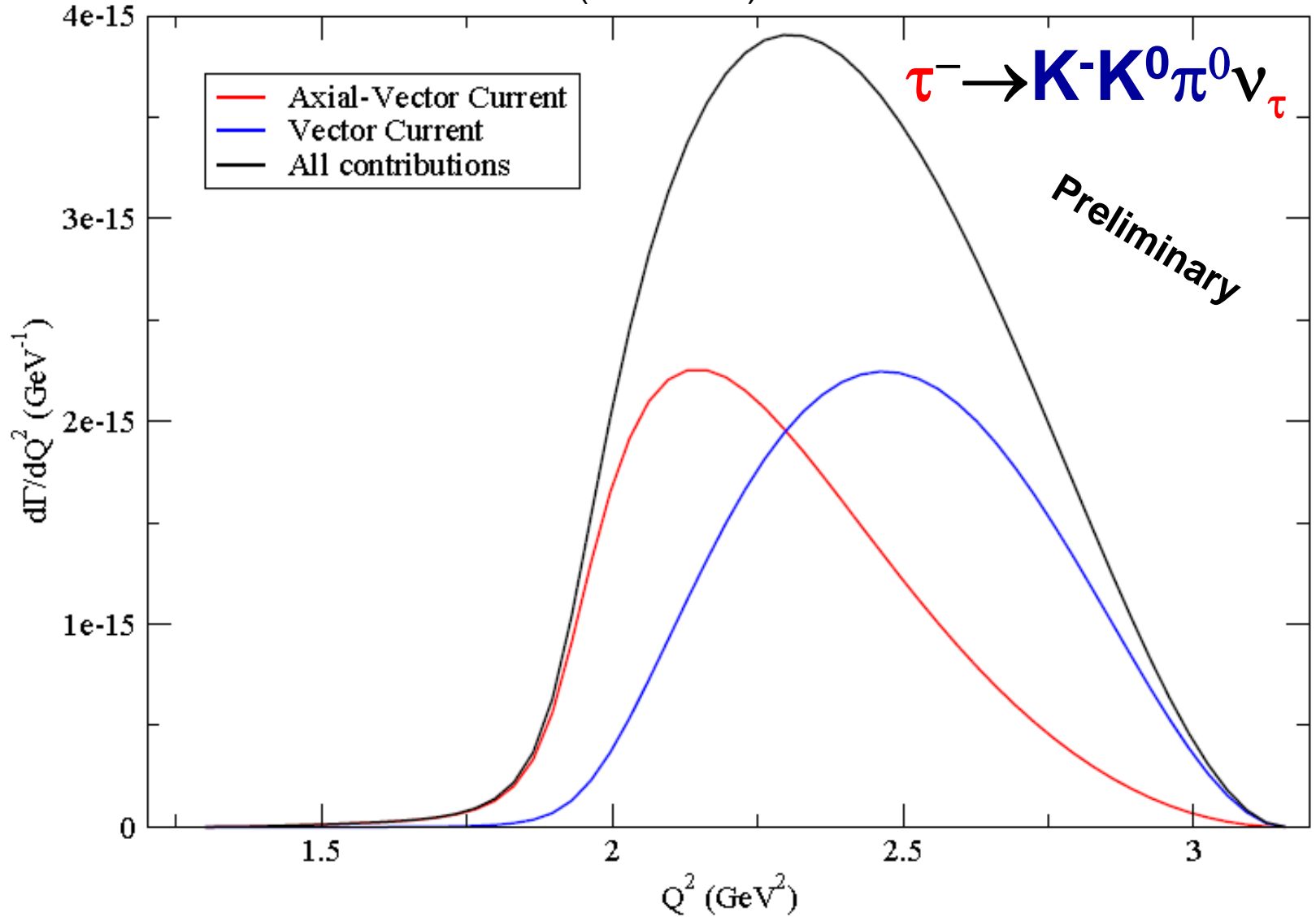
Three meson processes: $\rightarrow (KK\pi)^-\nu_\tau$ & $e^+e^-\rightarrow KK\pi$

(Our work)



Three meson processes: $\rightarrow (KK\pi)^-\nu_\tau$ & $e^+e^-\rightarrow KK\pi$

(Our work)



CONCLUSIONS

- Current analyses of $\tau^- \rightarrow (3\pi^-, K^+K^-\pi^-) \nu_\tau$ data using the **KS**(-like) model in **TAUOLA** have shown theoretical inconsistencies. We liked to improve the description of hadronization used.
- We have studied them within **R χ T** with a **Large N_c**-inspired **QCD**-guided approach (as it was done for $\tau^- \rightarrow (\pi\pi, K\pi) \nu_\tau$). We have improved the off-shell **a₁** width and revisited $\tau^- \rightarrow 3\pi^- \nu_\tau$. Using the available experimental data, we are able to predict the spectra of all **KK π** charge channels.
- Our **resonance widths** (**V** and **A-V**) have been implemented in **TAUOLA** (matrix elements on the way) and all them may be used by the (super)**B-factories**.
- Our expressions are easy to extend to the **e⁺e⁻** scattering below 2 GeV and thus might be of use for **PHOKHARA**.
- **LHC, BABAR, BELLE, BES-III...** are & will be providing testing grounds for our predictions.
- Promising & exciting future: **V_{us}, m_s** and, of course, **hadronization of QCD**.

HADRONIC τ DECAYS WITHIN R χ T
Pablo Roig (INFN)

BACKUP

SLIDES

HADRONIC DECAYS OF THE τ LEPTON

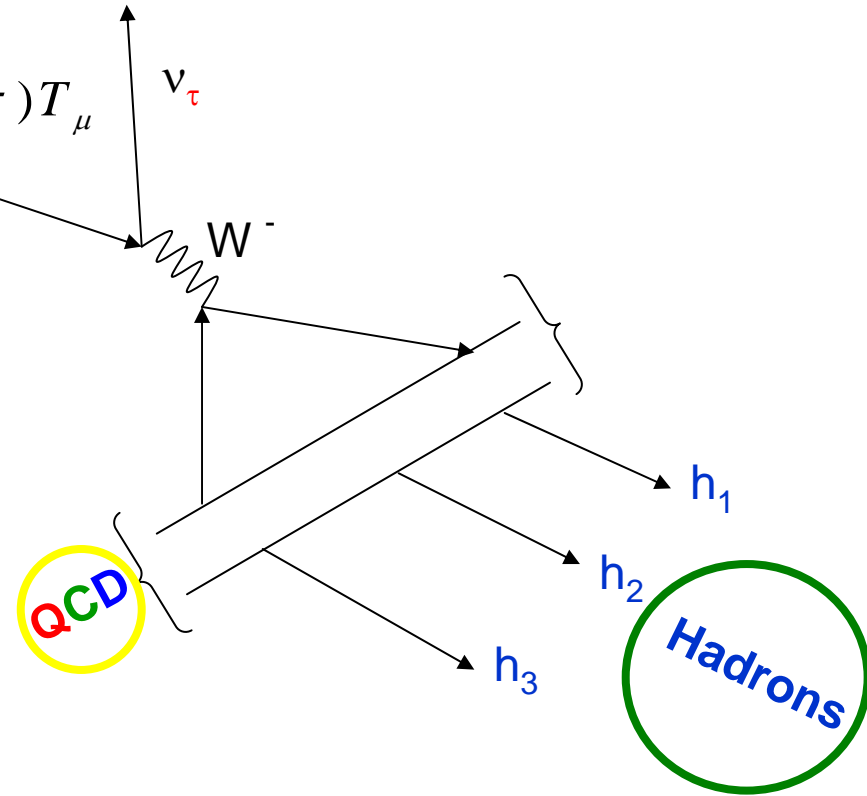
$$\mathfrak{M} = \frac{G_F}{\sqrt{2}} V_{CKM} \bar{u}(v_\tau) \gamma^\mu (1 - \gamma_5) u(\tau) T_\mu$$

$$\tau^- \rightarrow h_1(p_1) h_2(p_2) h_3(p_3) \nu_\tau$$

$$(p_1 + p_2 + p_3)^\mu = Q^\mu, \quad V_{2^\mu} = \left(g_{\mu\nu} - \frac{Q_\mu Q_\nu}{Q^2} \right) (p_2 - p_1)^\nu$$

$$T_\mu = V_{1\mu} F_1 + V_{2\mu} F_2 + Q_\mu F_P + i \varepsilon_{\mu\nu\rho\sigma} p_1^\nu p_2^\rho p_3^\sigma F_V$$

$$\frac{d\Gamma}{dQ^2} = \frac{G_F^2 |V_{CKM}|^2}{128(2\pi)^5 M_\tau^3} \int ds dt f(I_{0^-}, I_{1^+}, I_{1^-})$$



(Kühn, Santamaría '90)(KS)

(Gómez-Cadenas, González-García, Pich '90) (GGP)

KÜHN-SANTAMARÍA MODEL in TAUOLA

(Kühn-Santamaría '90)

$(2\pi, 3\pi)$

(Gómez-Dumm, Pich, Portolés '04)



χ PT $\mathcal{O}(p^2)$



χ PT $\mathcal{O}(p^4)$



Vector Meson Dominance

(Sakurai '69, Kühn & Wagner '84, Pich '87)

KS



Asymptotic behaviour ruled by QCD

(Brodsky-Farrar '73, B-Lepage '80)



$$BW_R(x^2) = \frac{M_R^2}{M_R^2 - x^2 - i\sqrt{x^2}\Gamma_R(x^2)}$$

(Gounaris-Sakurai '68)



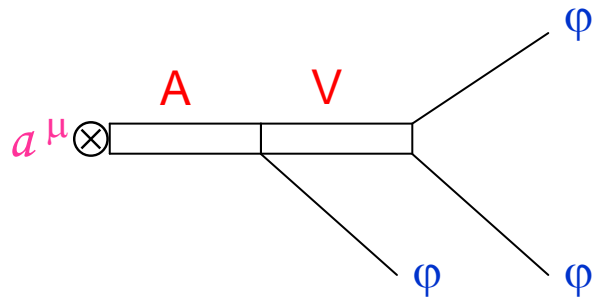
Ad-hoc off-shell widths

HADRONIC τ DECAYS WITHIN $R_\chi T$
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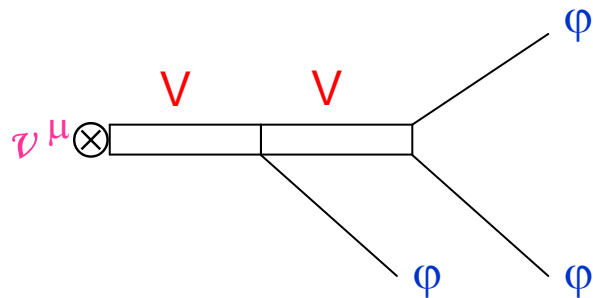
K-S-like MODEL IN TAUOLA

(Finkemeier, Mirkes '95,'96)

(Finkemeier, Kühn, Mirkes '96)



$$\rightarrow V_{1 \quad 2^\mu} = \left(g_{\mu\nu} - \frac{Q_\mu Q_\nu}{Q^2} \right) (p_2 - p_1)^\nu$$



$$\rightarrow i \varepsilon_{\mu\nu\rho\sigma} p_1^\nu p_2^\rho p_3^\sigma$$

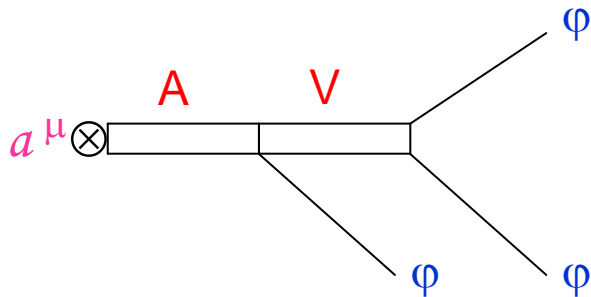
χ , 1R & 2R
obtained from:

$$\frac{M_{R1}^2}{M_{R1}^2 - x^2 - i\sqrt{x^2} \Gamma_{R1}(x^2)} \frac{M_{R2}^2}{M_{R2}^2 - y^2 - i\sqrt{y^2} \Gamma_{R2}(y^2)}$$

K-S-like MODEL IN TAUOLA

(Finkemeier, Mirkes '95,'96)

(Finkemeier, Kühn, Mirkes '96)



Some allowed contributions are lacking:



$\phi \phi \phi$

V-exchanged

missing in

$K^+K^-\pi^-$

ρ^0

$V_{2\mu}$

K^{*0}

$V_{1\mu}$

$K^-K^0\pi^0$

K^{*0}

$V_{1\mu}$

ρ^-

$V_{1\mu}$

$K^-\pi^-\pi^+$

K^{*0}

$V_{1\mu}$

$\overline{K}^0\pi^0\pi^-$

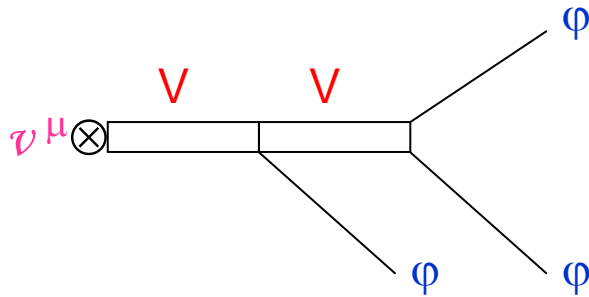
ρ^-

$V_{1\mu}$

K-S-like MODEL IN TAUOLA

(Finkemeier, Mirkes '95,'96)

(Finkemeier, Kühn, Mirkes '96)



$$M_{\rho'}^{V_\mu} \neq M_{\rho'}^{A_\mu}$$

$$\Gamma_{\rho'}^{V_\mu} \neq \Gamma_{\rho'}^{A_\mu}$$

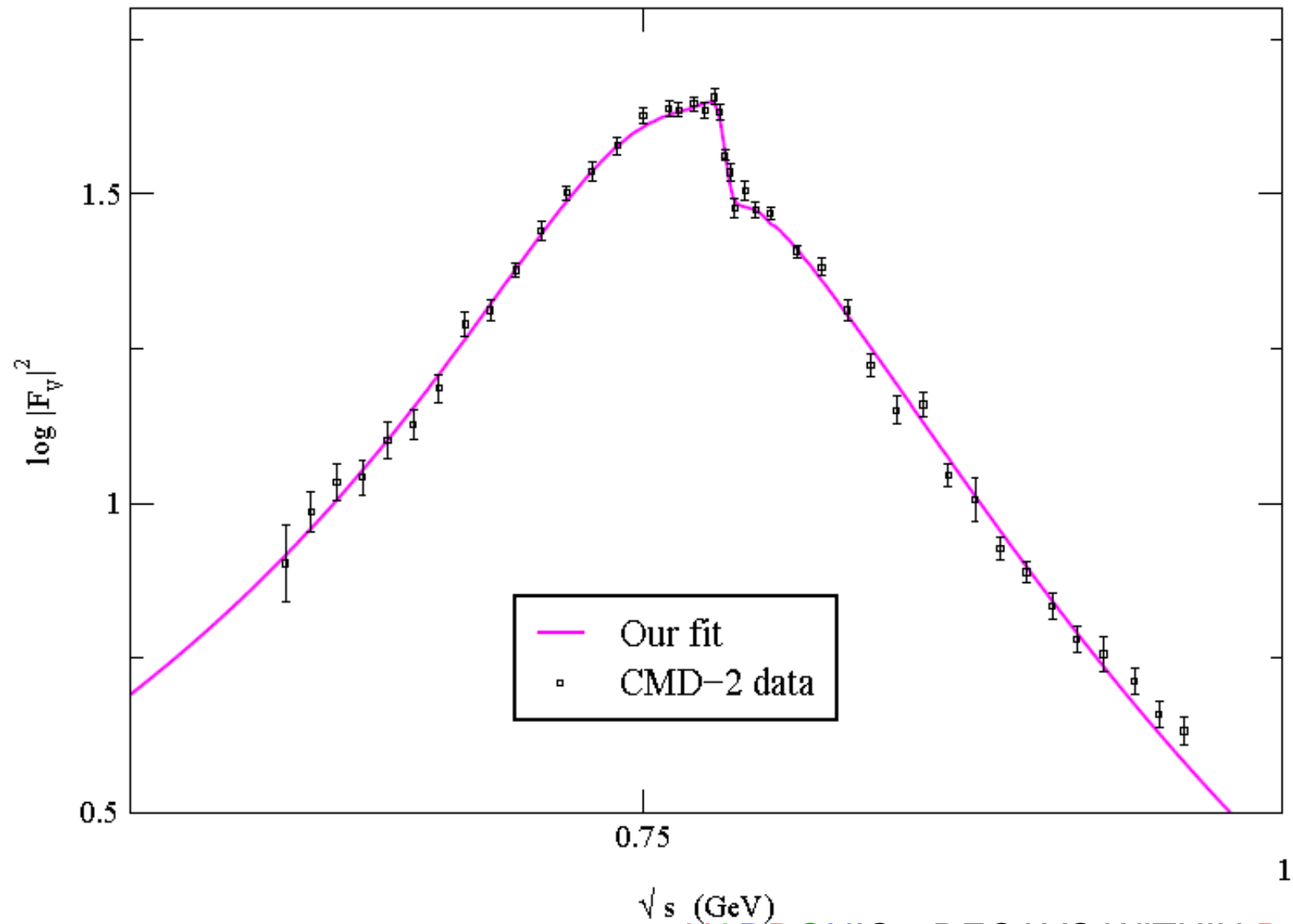
$$3 \text{ Multiplets}^{V_\mu} \neq 2 \text{ Multiplets}^{A_\mu}$$



We are involved in an ambitious program for describing within a **theoretical framework** as close as possible to **QCD** the considered decays.

$$\tau^- \rightarrow (\pi \pi)^- \nu_\tau$$

(Pich, Portolés '01, '03)



$$\underline{\tau^-} \rightarrow (\underline{K \pi})^- \underline{\nu_\tau}$$

Many works on $\underline{K \pi}$ FF: See complete Bibliography in (Jamin, Pich & Portolés, '06, '08)

The axial-form factor and the $a_1: \tau^- \rightarrow (3\pi)^- \nu_\tau$

(Our work)

(Gómez-Dumm, Pich, Portolés '04)

**7 unknown
couplings**



Computation + Brodsky-Lepage demanded to the Form Factors (**7-6 = 1 coupling**).

The axial-form factor and the $a_1: \tau^- \rightarrow (3\pi)^- \nu_\tau$ (Our work)

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Computation + Brodsky-Lepage demanded to the Form Factors (**7-6 = 1 coupling**).

λ_0

~12

(Gómez-Dumm, Pich, Portolés '04)

Gives a pretty accurate description of ALEPH spectral function and structure functions

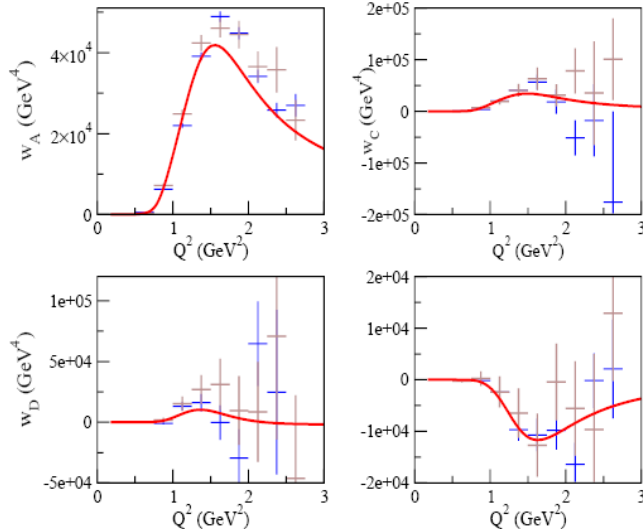
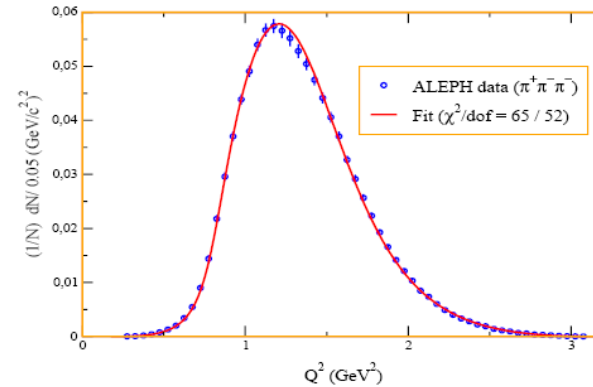
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Procedure and results [Gómez Dumm, Pich, Portolés, 2004]

Fit to the spectrum and BR
[ALEPH, 1998] $\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$

input



[CLEO-II,2000,(blue)] [OPAL,1997,(grey)]

output

$\tau^- \rightarrow \pi^- \pi^- \pi^0 \pi^0 \nu_\tau$

Structure Functions

PDG06

$M_{a_1} = (1.204 \pm 0.007) \text{ GeV}$
 $\Gamma_{a_1}(M_{a_1}) = (0.48 \pm 0.02) \text{ GeV}$

$\lambda_0 = 11.9 \pm 0.4$

Implemented in SHERPA

IFIC - Instituto de Física Corpuscular

HADRONIC τ DECAYS WITHIN $R_\chi T$
 Pablo Roig (INFN)

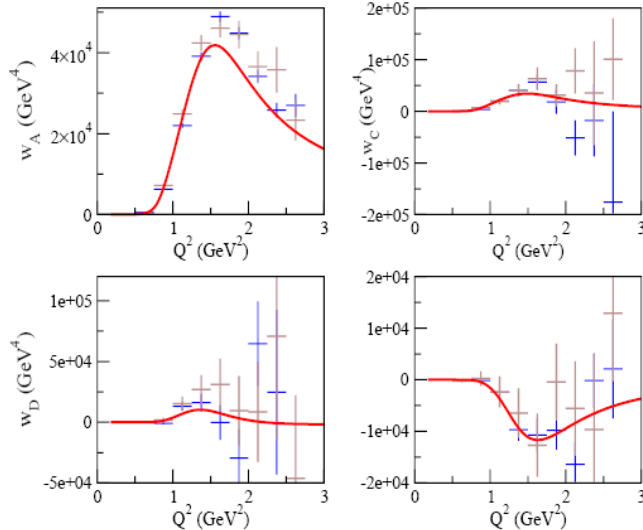
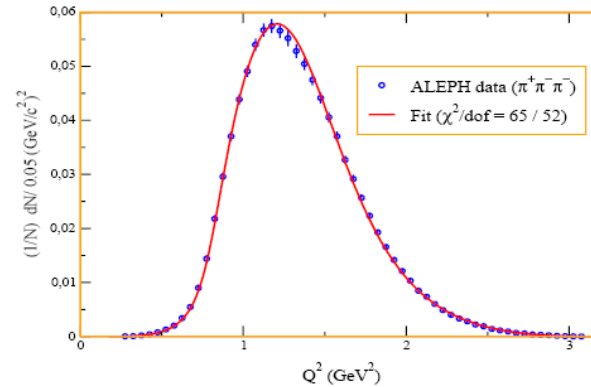
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[CLEO-II,2000,(blue)] [OPAL,1997,(grey)]

output

Caveat:

$F_{1,2} \approx \lambda_0 \frac{m_\pi^2}{Q^2}$

$\tau^- \rightarrow \pi^- \pi^0 \pi^0 \nu_\tau$

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PDG06

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HADRONIC τ DECAYS WITHIN $R_\chi T$

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The axial-form factor and the $a_1: \tau^- \rightarrow (3\pi)^- \nu_{\tau}$ (Our work)

However, $\lambda_0 \sim 1/8$ (Cirigliano, Ecker, Eidemüller, Pich, Portolés '04) <VAP>

and the proposed a_1 width was just χ based

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Models and parameterizations

➤ [Gounaris, Sakurai, 1968] Pion form factor (resonance dynamics)

➤ [Tsai, 1971] Current Algebra parameterization

➤ [Fischer, Wess, Wagner, 1980]

[Berger, 1987]

[Braaten, Oakes, Tse, 1990]

[Colangelo, Finkemeier, Urech, 1996]

Chiral symmetry

+

Modelization VMD

$\pi\pi$

$\pi\pi\pi$

➤ [Kühn, Wagner, 1984]

[Pich et al, 1989, 1990]

[Kühn, Santamaría, 1990]

[Decker, Finkemeier, Kühn,
Mirkes, Was..., 1990-2000]

➤ [Bruch, Khodjamirian, Kühn, 2004]

Kühn & Santamaría model

Parameterization of 2P, 3P

TAUOLA

(KS,GS) modified – dual QCD($N_C \rightarrow \infty$)

Models and parameterizations

➤ [Beldjoudi, Truong, 1995]

Current Algebra + Dispersion Relations
($\pi\pi$, $K\pi$, $K\eta$, 3π , $K\pi\pi$)

➤ [Guerrero, Pich, 1997]

[Pich, Portolés, 2001]

χ PT + $R\chi$ T + Dispersion Relations
(Pion form factor)

➤ [Sanz-Cillero, Pich, 2003]

[Rosell, Sanz-Cillero, Pich, 2004]

$R\chi$ T + large- N_C expansion
(Pion form factor)

➤ [Gómez Dumm, Pich, Portolés, 2004]

$R\chi$ T (chiral symmetry)
Large- N_C expansion
Asymptotic behaviour ruled by QCD
(3π) \longrightarrow all 3P

About TAUOLA

- Kühn & Santamaría model

$$\text{F.F.} = \frac{M_R^2}{M_R^2 - q^2 - i\sqrt{q^2}\Gamma_R(q^2)}$$

- Low-energy expansion in $\tau \rightarrow \pi\pi\pi\nu_\tau$

$$F_1^A(Q^2, s_1, s_2)_{KS} = 1 + \frac{s_1}{M_V^2} + \frac{Q^2}{M_A^2} + \mathcal{O}\left(\frac{q^4}{M_R^4}\right)$$

$$F_1^A(Q^2, s_1, s_2)_{\chi PT} = \underbrace{1}_{\mathcal{O}(p^2)_{\chi PT}} + \underbrace{\frac{3}{2} \frac{s_1}{M_V^2}}_{\mathcal{O}(p^4+\dots)_{\chi PT}} + \mathcal{O}\left(\frac{q^4}{M_R^4}\right)$$

HADRONIC τ DECAYS WITHIN $R_{\chi T}$
Pablo Roig (INFN)

$\tau^- \rightarrow (\pi\pi\pi)^- \nu_\tau$: Axial-vector form factors

$$\langle \pi_{p_1}^- \pi_{p_2}^- \pi_{p_3}^+ | (\mathbf{V}_\mu^- - \mathbf{A}_\mu^-) e^{iL_{QCD}} | 0 \rangle = \left(g_{\mu\nu} - \frac{Q_\mu Q_\nu}{Q^2} \right) \left[F_1^A(Q^2, s_1, s_2) (p_1 - p_3)^\nu + F_1^A(Q^2, s_2, s_1) (p_2 - p_3)^\nu \right]$$

$$Q = p_1 + p_2 + p_3$$

$$s_i = (Q - p_i)^2$$

$$+ \cancel{F_2^A} Q_\mu \quad + \quad i \cancel{F_3^V} \varepsilon_{\mu\alpha\beta\gamma} p_1^\alpha p_2^\beta p_3^\gamma$$

$m_\pi = 0$ $SU(2)_I$

Kühn & Santamaría Model

$$F_1^A(Q^2, s_1, s_2) = N|_{\chi O(p^2)} BW_{a_1}(Q^2) \frac{BW_\rho(s_1) + \alpha BW_{\rho'}(s_1) + \beta BW_{\rho''}(s_1)}{1 + \alpha + \beta}$$

HADRONIC τ DECAYS WITHIN R χ T
Pablo Roig (INFN)

χ PT: The low-energy

EFT of QCD

(Gasser & Leutwyler '84, '85)

$$\phi(x) = \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2\eta_8}{\sqrt{6}} \end{pmatrix}$$

**Goldstone
Bosons**

$$SU(3)_L \otimes SU(3)_R \rightarrow SU(3)_V$$

$$u(x) = \exp\left(\frac{i\phi(x)}{\sqrt{2}F}\right), \quad u_\mu = i\left[u^\dagger(\partial_\mu - ir_\mu)u - u(\partial_\mu - il_\mu)u^\dagger\right]$$

$$\chi = 2B_0(s + ip), \quad \chi_\pm = u^\dagger \chi u^\dagger \pm u \chi u$$

$$f_\pm^{\mu\nu} = u F_L^{\mu\nu} u^\dagger \pm u^\dagger F_R^{\mu\nu} u$$

$$\mathcal{L}_\chi^{(2)} = \frac{F^2}{4} \langle u_\mu u^\mu + \chi_+ \rangle$$

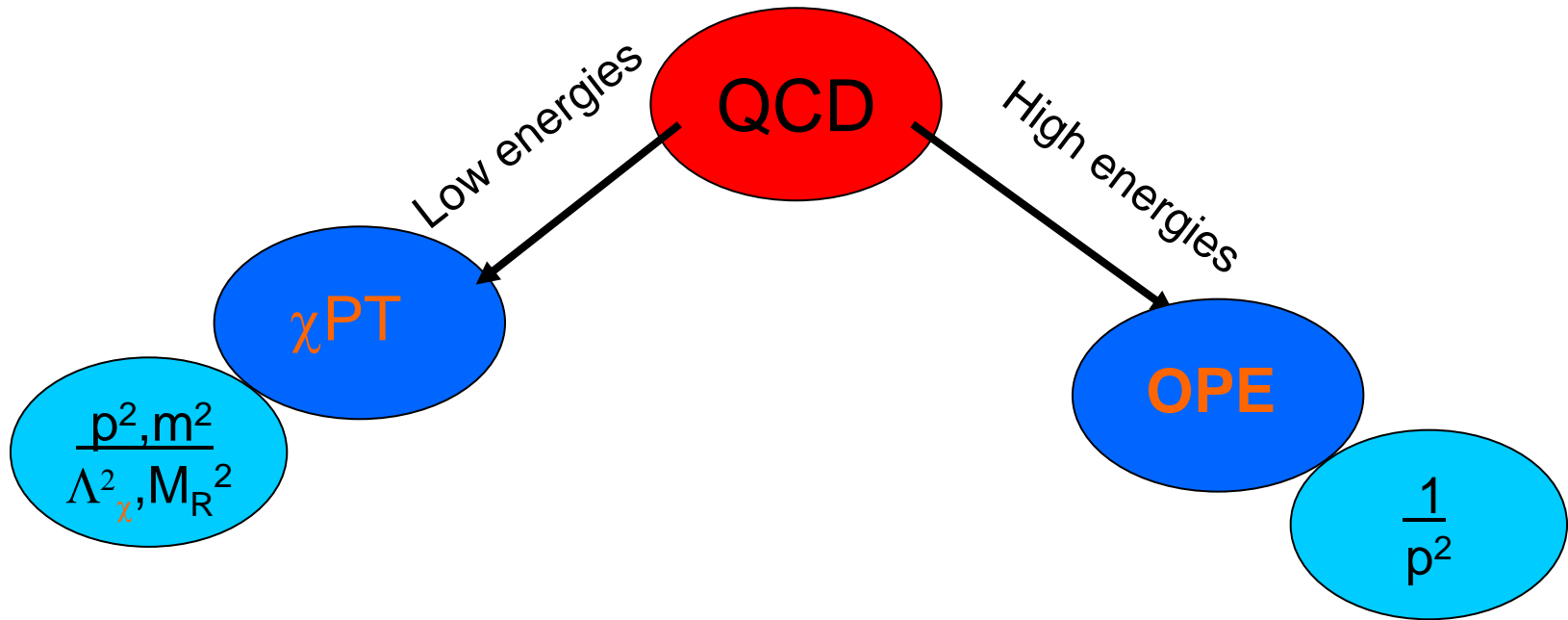
$$X \rightarrow h(g, \Phi) X h(g, \Phi)^\dagger$$

$$\mathcal{L}_\chi^{(4)} = L_1 \langle u_\mu u^\mu \rangle^2 + \dots + L_4 \langle u_\mu u^\mu \rangle \langle \chi_+ \rangle + \dots + L_7 \langle \chi_- \rangle^2 + \dots - iL_9 \langle f_+^{\mu\nu} u_\mu u_\nu \rangle + \dots$$

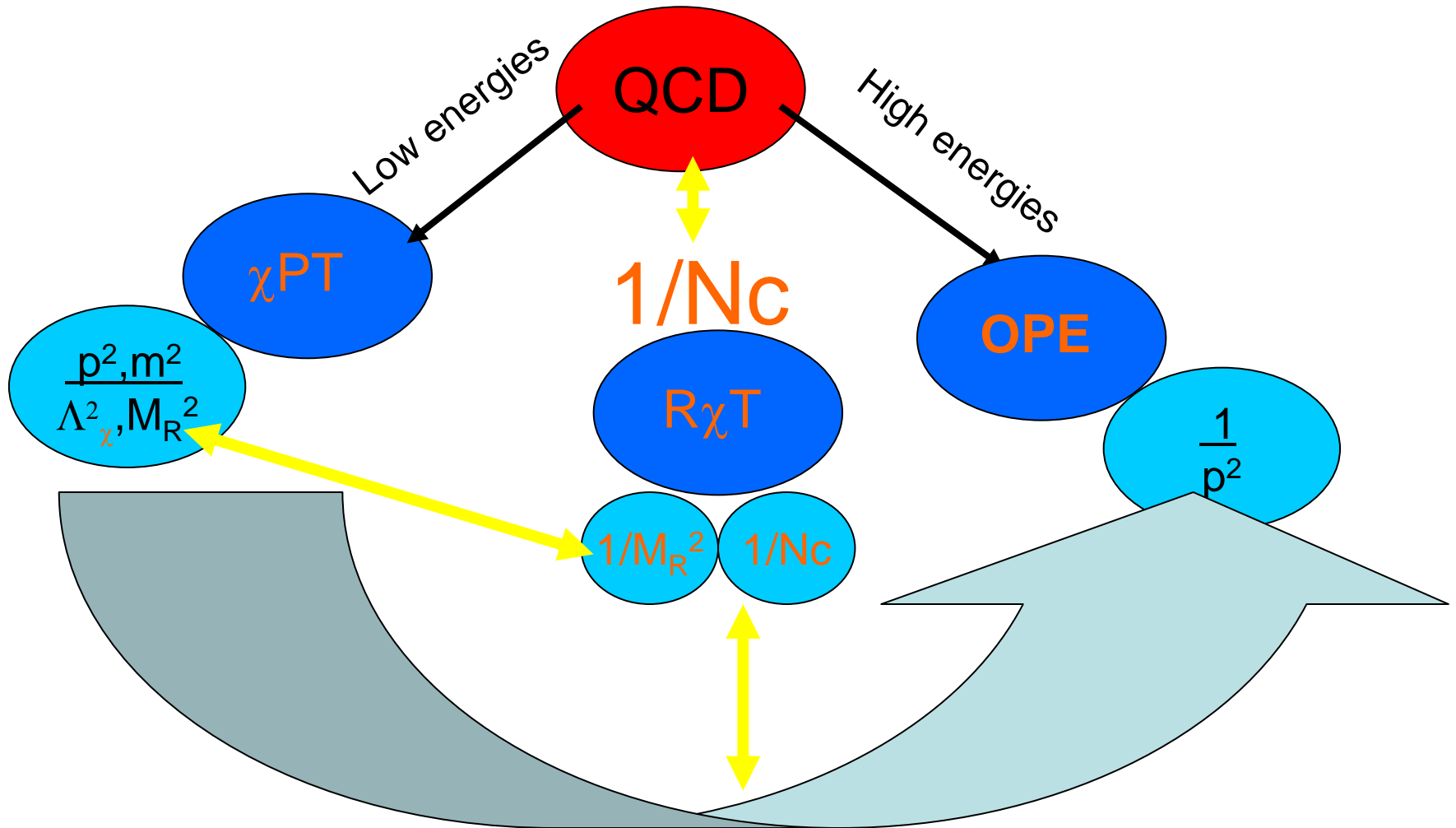
$$\mathcal{L}_\chi^{(4)} \text{, WZW in the odd-intrinsic parity sector}$$

HADRONIC τ DECAYS WITHIN $R_\chi T$
Pablo Roig (INFN)

R_χT matching to the OPE allows it to reproduce QCD high-energy behaviour:



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HADRONIC τ DECAYS WITHIN $R\chi T$
 Pablo Roig (INFN)

Resonances + Goldstone Bosons

TOOLS : R_χT

(Ecker, Gasser, Pich, De Rafael '89)

(Ecker, Gasser, Leutwyler, Pich, De Rafael '89)

$$\mathcal{L}_{R\chi T}^{(P_i=+)} = \mathcal{L}_{\chi}^{(2)} + \mathcal{L}_{V,A}^{kin} + \mathcal{L}_V + \mathcal{L}_A + \mathcal{L}_{VAP};$$

$$\mathcal{L}_V = \frac{F_V}{2\sqrt{2}} \langle V_{\mu\nu} f_+^{\mu\nu} \rangle + \frac{iG_V}{\sqrt{2}} \langle V_{\mu\nu} u^\mu u^\nu \rangle$$

$$\mathcal{L}_A = \frac{F_A}{2\sqrt{2}} \langle A_{\mu\nu} f_-^{\mu\nu} \rangle$$

Antisymmetric tensor formalism

$$\mathcal{L}_{VAP} = \sum_{i=1}^5 \lambda_i O^i(V_{\mu\nu}, A^{\mu\nu}, \phi) = \lambda_1 \langle [V_{\mu\nu}, A^{\mu\nu}] \chi_- \rangle + \dots$$

$$\mathcal{L}_{R\chi T}^{(P_i=-)} = \mathcal{L}_{\chi(WZW)}^{(4)} + \mathcal{L}_{VJP} + \mathcal{L}_{VVP} + \mathcal{L}_{VPPP};$$

$$\mathcal{L}_{VJP} = \sum_{i=1}^7 \frac{c_i}{M_V} O^i(V_{\mu\nu}, j^\nu, \partial^\mu \phi) = \frac{c_5}{M_V} \varepsilon_{\mu\nu\rho\sigma} \langle \{ \nabla_\alpha V^{\mu\nu}, f_+^{\rho\alpha} \} u^\sigma \rangle + \dots$$

$$\mathcal{L}_{VVP} = \sum_{i=1}^5 d_i O^i(V_{\mu\nu}, V_{\rho\sigma}, \phi) = d_1 \varepsilon_{\mu\nu\rho\sigma} \langle \{ V^{\mu\nu}, V^{\rho\alpha} \} \nabla_\alpha u^\sigma \rangle + \dots$$

$$\mathcal{L}_{VPPP} = \sum_{i=1}^5 \frac{g_i}{M_V} O^i(V_{\mu\nu}, \phi) = \frac{g_4}{M_V} \varepsilon_{\mu\nu\alpha\beta} \langle \{ V^{\mu\nu}, u^\alpha u^\beta \} \chi_- \rangle + \dots$$

$$V_{\mu\nu}(x) = \begin{pmatrix} \frac{\rho^0}{\sqrt{2}} + \frac{\omega_8}{\sqrt{6}} & \rho^+ & K^{*+} \\ \rho^- & -\frac{\rho^0}{\sqrt{2}} + \frac{\omega_8}{\sqrt{6}} & K^{*0} \\ K^{*-} & \bar{K}^{*0} & -\frac{2\omega_8}{\sqrt{6}} \end{pmatrix}_{\mu\nu}$$

(Gómez Dumm, Pich, Portolés '04)

VMD

(Ruiz-Femenía, Pich, Portolés '03)

(Gómez Dumm, Pich, Portolés, R. to appear)

**Resonances
+ Goldstone
Bosons**

TOOLS : R_χT

(Ecker, Gasser, Pich, De Rafael '89)

(Ecker, Gasser, Leutwyler, Pich, De Rafael '89) , ...

$$\mathcal{L}_{R\chi T}^{(P_I=+)} = \mathcal{L}_{\chi}^{(2)} + \mathcal{L}_{V,A}^{kin} + \mathcal{L}_V + \mathcal{L}_A + \mathcal{L}_{VAP};$$

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$$\mathcal{L}_A = \frac{F_A}{2\sqrt{2}} \langle A_{\mu\nu} f_-^{\mu\nu} \rangle$$

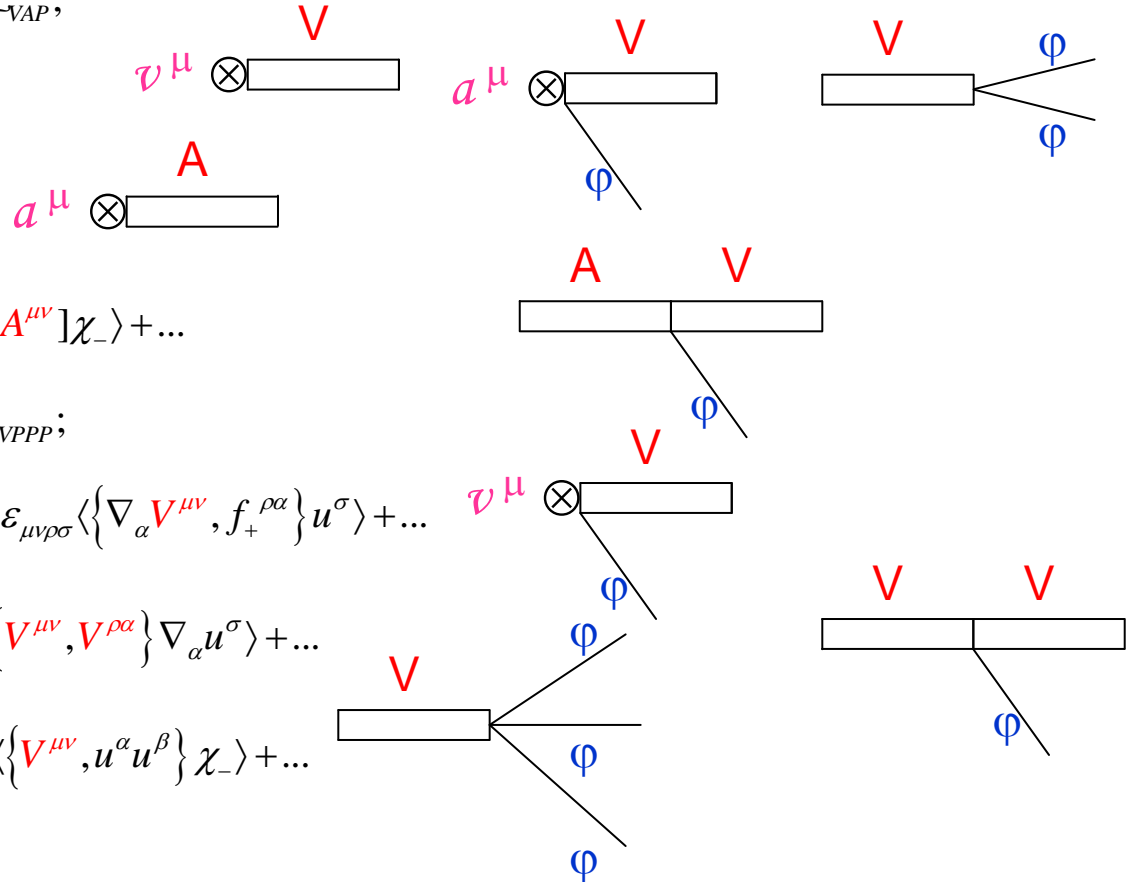
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$$\mathcal{L}_{VPPP} = \sum_{i=1}^5 \frac{g_i}{M_V} O^i(V_{\mu\nu}, \phi) = \frac{g_4}{M_V} \epsilon_{\mu\nu\alpha\beta} \langle \{ V^{\mu\nu}, u^\alpha u^\beta \} \chi_- \rangle + \dots$$



The axial-form factor and the $a_1: \tau^- \rightarrow (3\pi)^- \nu_\tau$

Our study attempts to provide a good phenomenological description of $\tau^- \rightarrow (3\pi)^- \nu_\tau$ with:

$$\lambda_0 \sim 1/8$$

$$\Gamma_{a_1}(Q^2) \leftarrow R\chi T \text{ ☺}$$

$$F_V G_V = F^2,$$

$$F_V^2 - F_A^2 = F^2,$$

$$M_V^2 F_V^2 = M_A^2 F_A^2,$$

$$\lambda' = \frac{F_V}{2\sqrt{2}F_A},$$

$$\lambda'' = \left(2\frac{F^2}{F_V^2} - 1 \right) \lambda'.$$

The axial-form factor and the $a_1: \tau^- \rightarrow (3\pi)^- \nu_\tau$

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$$\lambda_0 \sim 1/8 \quad \text{😊}$$
$$\Gamma_{a_1}(Q^2) \leftarrow R\chi T \quad \text{😊}$$

$$F_V G_V = F^2,$$

$$F_A \sim 140 \text{ MeV}, \quad F_V \sim 210 \text{ MeV}$$

$$\lambda' = \frac{F_V}{2\sqrt{2}F_A},$$

$$\lambda'' = \left(2\frac{F^2}{F_V^2} - 1 \right) \lambda'.$$

SHORT-DISTANCE CONSTRAINTS

Vector Form Factor $\langle \pi | v_\mu | \pi \rangle$:

$$F_V(t) = 1 + \sum_i \frac{F_{V_i} G_{V_i}}{f^2} \frac{t}{M_{V_i}^2 - t}$$

$$\lim_{t \rightarrow \infty} F_V(t) = 0$$



$$\sum_i F_{V_i} G_{V_i} = f^2$$

Axial Form Factor $\langle \gamma | a_\mu | \pi \rangle$:

$$G_A(t) = \sum_i \left\{ \frac{2 F_{V_i} G_{V_i} - F_{V_i}^2}{M_{V_i}^2} + \frac{F_{A_i}^2}{M_{A_i}^2 - t} \right\}$$

$$\lim_{t \rightarrow \infty} G_A(t) = 0$$



$$\sum_i (2 F_{V_i} G_{V_i} - F_{V_i}^2) / M_{V_i}^2 = 0$$

Weinberg Sum Rules:

$$\Pi_{LR}(t) = -\frac{f^2}{t} + \sum_i \frac{F_{V_i}^2}{M_{V_i}^2 + t} - \sum_i \frac{F_{A_i}^2}{M_{A_i}^2 + t}$$

$$\lim_{t \rightarrow \infty} t \Pi_{LR}(t) = 0$$

$$\lim_{t \rightarrow \infty} t^2 \Pi_{LR}(t) = 0$$



$$\sum_i (F_{V_i}^2 - F_{A_i}^2) = f^2$$

$$\sum_i (M_{V_i}^2 F_{V_i}^2 - M_{A_i}^2 F_{A_i}^2) = 0$$

The axial-form factor and the $a_1: \tau^- \rightarrow (3\pi)^- \nu_\tau$

(Gómez-Dumm, Pich, Portolés '00)

$$\Gamma_\rho(s) = \frac{M_\rho s}{96\pi F^2} \left[\sigma_\pi^3 \Theta(s - 4m_\pi^2) + \frac{1}{2} \sigma_K^3 \Theta(s - 4m_K^2) \right]$$

(This work)

$$\Gamma_{a_1}(Q^2) = \Gamma_{a_1}^{3\pi}(Q^2) + \Gamma_{a_1}^{K\bar{K}\pi}(Q^2) + \Gamma_{a_1}^{(K\pi)^0 K^0}(Q^2),$$

$$\Gamma_{a_1}^{3\pi}(Q^2) = \frac{1}{48(2\pi)^3 M_{a_1}} \left(\frac{Q^2}{M_{a_1}^2} \right)^\alpha \iint ds dt \left(F_1' V_{1\mu} + F_2' V_{2\mu} \right).$$

$$\left(F_1'^\dagger V_{1\mu} + F_2'^\dagger V_{2\mu} \right), \quad F_i' = F_i \frac{M_{a_1}^2 - Q^2}{\sqrt{2} F_A Q^2}$$

HADRONIC τ DECAYS WITHIN R χ T
Pablo Roig (INFN)

CLEO analyses & KS-like models

(Liu '03)

CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

CLEO analyses & ~~KS~~-like models

(Liu '03)

CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

CLEO analyses & ~~KS~~-like models

(Liu '03) (CLEO-III '04)

CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

CLEO analyses & ~~KS~~-like models

(Liu '03) (CLEO-III '04)

CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

$$F_V = -\frac{1}{2\sqrt{2}\pi^2 F^3} \sqrt{R_B} \sum_i B W_i$$

CLEO analyses & ~~KS~~-like models

(Liu '03) (CLEO-III '04)

CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

$$F_V = \underbrace{-\frac{1}{2\sqrt{2}\pi^2 F^3}}_{L^{(4)}_{\chi, WZW}} \sqrt{R_B} \underbrace{\sum_i BW_i}_{\xrightarrow{Q^2 \rightarrow 0} 1}$$

CLEO analyses & ~~KS~~-like models

(Liu '03) (CLEO-III '04)

CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

$$F_V = \underbrace{-\frac{1}{2\sqrt{2}\pi^2 F^3}}_{L^{(4)}_{\chi, WZW}} \sqrt{R_B} \underbrace{\sum_i BW_i}_{\xrightarrow{Q^2 \rightarrow 0} 1}$$
$$BW_{V,A}(x = s_i, Q^2) = \frac{M_{V,A}^2}{M_{V,A}^2 - x - i\sqrt{x}\Gamma_{V,A}(x)}$$

CLEO analyses & ~~KS~~-like models

(Liu '03) (CLEO-III '04)

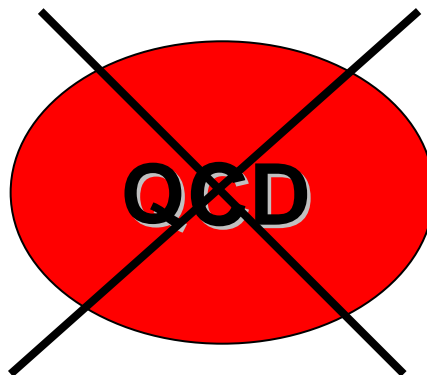
CLEO

$$\tau^- \rightarrow K \bar{K} \pi^- \nu_\tau$$

$$F_V = \underbrace{-\frac{1}{2\sqrt{2}\pi^2 F^3}}_{L^{(4)}_{\chi, WZW}} \sqrt{R_B} \underbrace{\sum_i BW_i}_{\xrightarrow{Q^2 \rightarrow 0} 1}$$

$$BW_{V,A}(x = s_i, Q^2) = \frac{M_{V,A}^2}{M_{V,A}^2 - x - i\sqrt{x}\Gamma_{V,A}(x)}$$

1.80 ± 0.53

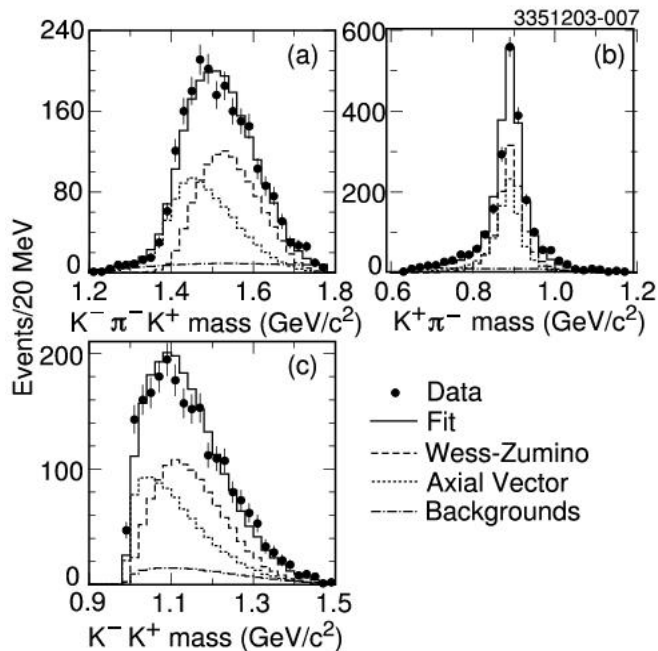


HADRONIC τ DECAYS WITHIN $R_{\chi T}$
 Pablo Roig (INFN)

CLEO analyses & ~~KS~~-like models

(Liu '03) (CLEO-III '04)

CLEO



$$F_V = \underbrace{\frac{1}{2\sqrt{2}\pi^2 F^3}}_{L^{(4)}_{\chi, \text{WZW}}} \sqrt{R_B} \underbrace{\sum_i BW_i}_{\xrightarrow{Q^2 \rightarrow 0} 1}$$

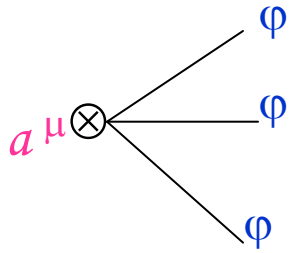
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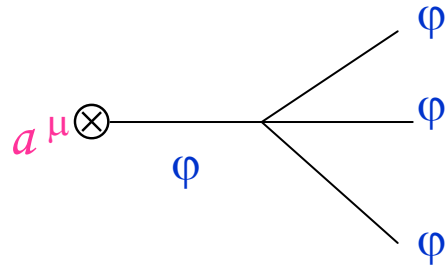
~~QCD~~

HADRONIC τ DECAYS WITHIN $R_{\chi T}$
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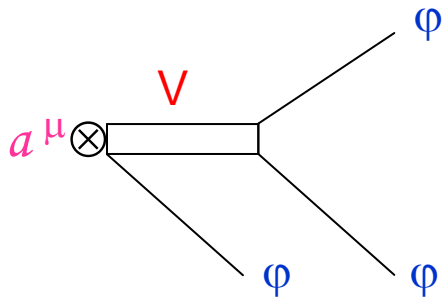
R_χT APPLIED



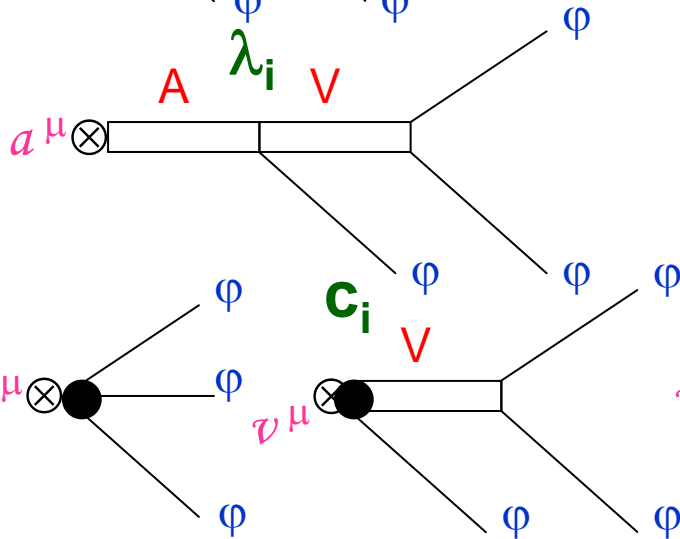
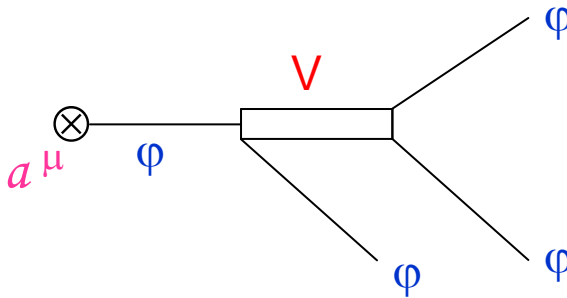
F



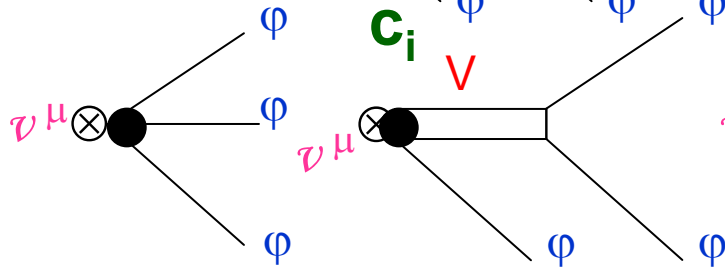
23 unknown couplings



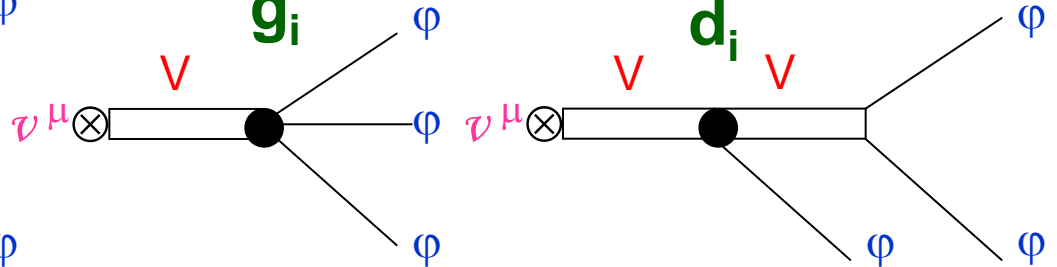
G_V, F_V



C_i



g_i



d_i

HADRONIC τ DECAYS WITHIN R_χT
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YRW 09 Frascati

$K \bar{K} \pi^-$ channels within $R_\chi T$

Axial-vector Current

$$F_V G_V = F^2,$$

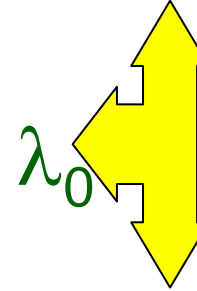
$$F_V^2 - F_A^2 = F^2,$$

$$2G_V = F_V,$$

$$2\lambda' = 1,$$

$$\lambda'' = 0.$$

12 (Gómez-Dumm, Pich, Portolés '04)



1/8 (Cirigliano, Ecker, Eidemüller, Pich, Portolés '04)

Vector Current

Fixed

Free

vector₁:

(This work)

$$c_{125} = c_1 - c_2 + c_5$$

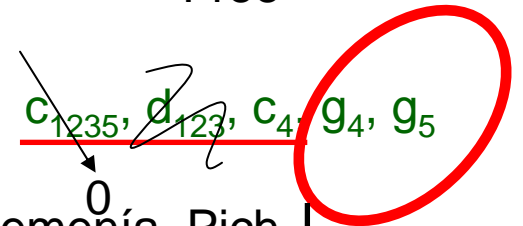
$$c_{1256} = c_1 - c_2 - c_5 + 2c_6$$

$$g_{123} = g_1 + 2g_2 - g_3$$

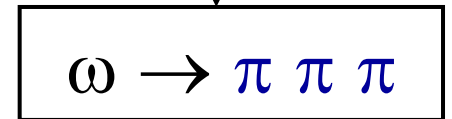
$c_{125}, c_{1256}, d_3, g_{123}, g_2$

$$c_{1235} = c_1 + c_2 + 8c_3 - c_5$$

$$d_{123} = g_1 + 8d_2 - d_3$$



(Ruiz-Femenía, Pich, Portolés '03)



HADRONIC τ DECAYS WITHIN $R_\chi T$

Pablo **Roig** (INFN)

$$\underline{\tau^-} \rightarrow \underline{(2K \pi)^-} \underline{\nu_{\tau}}$$

BaBar has recently (BaBar '07) published very precise data on $e^+e^- \rightarrow KK \pi/\eta$ using **ISR** events. Furthermore, their Dalitz-plot fit has allowed to separate cleanly the $l=0,1$ contributions.

Assuming **CVC** and comparing to **ALEPH '99** allows to derive $(\Gamma_V/\Gamma_{\tau}) = 0.167 \pm 0.024$ in $\tau^- \rightarrow (KK \pi)^- \nu_{\tau}$. Under **CVC** one can relate e^+e^- data to the τ decay.

(Davier, Descotes-Genon, Höcker, Malaescu, Zhang '08)

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Assumptions of this procedure: SU(2) symmetry

$$K^* \gg \rho, \omega, \phi$$

Interferences are negligible


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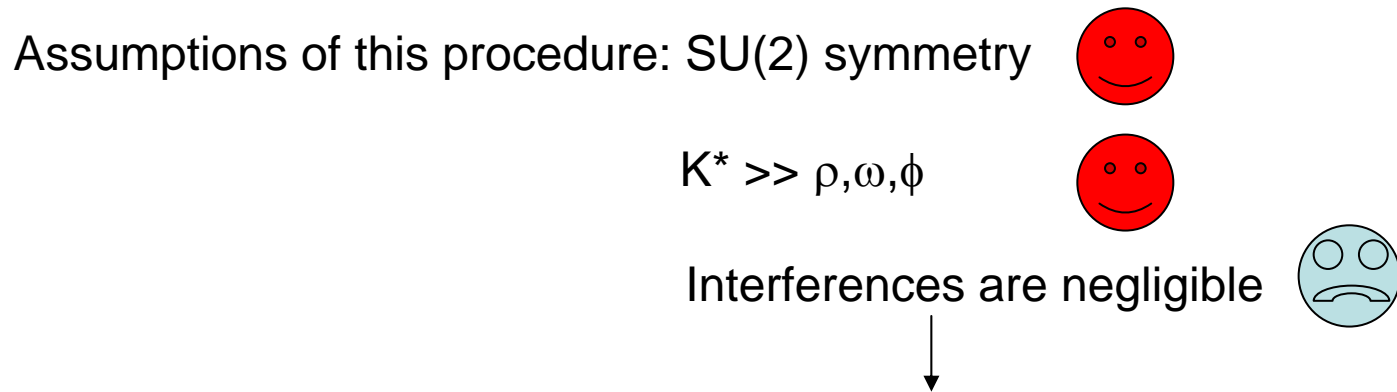
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Error of this simplification $\geq 30\%$ both in **KS** approach and in ours


HADRONIC τ DECAYS WITHIN **R χ T**
Pablo Roig (INFN)


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BaBar has recently (BaBar '07) published very precise data on $e^+e^- \rightarrow KK \pi/\eta$ using **ISR** events. Furthermore, their Dalitz-plot fit has allowed to separate cleanly the $l=0,1$ contributions.

Assuming **CVC** and comparing to **ALEPH '99** allows to derive $(\Gamma_{\nu}/\Gamma_{\tau}) = 0.167 \pm 0.024$ in $\tau^- \rightarrow (KK \pi)^- \nu_{\tau}$. Under **CVC** one can relate e^+e^- data to the τ decay.

(Davier, Descotes-Genon, Höcker, Malaescu, Zhang '08)

Assumptions of this procedure: SU(2) symmetry 

$K^* \gg \rho, \omega, \phi$ 

Interferences are negligible 



Error of this simplification $\geq 30\%$ both in **KS** approach and in ours

(Apart from the error intrinsic to using Breit-Wigner function for resonance exchange)

HADRONIC τ DECAYS WITHIN **R χ T**
Pablo Roig (INFN)

SU(2) AND INTERFERENCES

Until recently, there was some confusion on this issue for the $K\bar{K}\pi$ modes:

(Davier, Descotes-Genon, Höcker, Malaescu, Zhang '08)

1. In the ALEPH analysis of τ decay modes with kaons [12], an estimate of the vector contribution was obtained using the e^+e^- annihilation data from DM1 [13] and DM2 [14] in the $K\bar{K}\pi$ channel, extracted in the $I = 1$ state. This contribution was found to be small, and, using the conserved vector current (CVC), a branching fraction of $\mathcal{B}_{\text{CVC}}(\tau \rightarrow \nu_\tau (K\bar{K}\pi)_V) = (0.26 \pm 0.39) \cdot 10^{-3}$, was found, corresponding to an axial fraction of $f_{A,\text{CVC}}(K\bar{K}\pi) = 0.94^{+0.06}_{-0.08}$.
2. The ALEPH CVC result was corroborated by a partial-wave and lineshape analysis of the a_1 resonance from τ decays in the $\nu_\tau\pi^-2\pi^0$ mode performed by CLEO [15]. The effect of the K^*K decay mode of the a_1 was seen through unitarity and a branching fraction of $\mathcal{B}(a_1 \rightarrow K^*K) = (3.3 \pm 0.5)\%$ was derived. With the known $\tau^- \rightarrow \nu_\tau a_1^-$ branching fraction, this value more than saturates the total branching fraction available for the $K\bar{K}\pi$ channel, yielding an axial fraction of $f_{A,a_1}(K\bar{K}\pi) = 1.30 \pm 0.24$.
3. Another piece of information, also contributed by CLEO [16], but conflicting with the two previous results, is based on a partial-wave analysis in the $K^-K^+\pi^-$ channel using two-body resonance production and including many possible contributing channels. A much smaller axial fraction of $f_{A,K\bar{K}\pi}(K\bar{K}\pi) = 0.56 \pm 0.10$ was found here.

Since the three determinations are inconsistent, the value $f_A = 0.75 \pm 0.25$ has been used previously to account for the discrepancy [1]. This led to a systematic uncertainty in the V, A spectral functions that competed with the purely experimental uncertainties.

Precise cross section measurements for e^+e^- annihilation to $K^+K^-\pi^0$ and to $K^0K^\pm\pi^\mp$ have been recently published by the BABAR Collaboration [7], using the method of radiative return. In the mass range of interest for τ physics they show strong dominance of $K^*(890)K$ dynamics and a fit of the Dalitz plot yields a clean separation of the $I = 0, 1$ contributions. Assuming CVC, the mass distribution of the vector final state in the decays $\tau \rightarrow \nu_\tau K\bar{K}\pi$ can be obtained. The result is shown in Fig. 1 and compared with the full τ spectrum from ALEPH [12] summing up the contributions from the $K^-K^+\pi^-$, $\bar{K}^0K^0\pi^-$, and $K^-K^0\pi^0$ modes. The BABAR results reveal a small vector component. After integration, one obtains

$$f_{A,\text{CVC}}(K\bar{K}\pi) = 0.833 \pm 0.024, \quad (7)$$

which is about 1.3σ lower than the ALEPH determination using the same method (but with much poorer e^+e^- input data) and 2.7σ higher than the CLEO partial-wave-analysis result. The new determination has a precision that exceeds the previously used value by an order of magnitude, thus effectively reducing the uncertainties in the vector and axial-vector spectral functions to the experimental errors only.

HADRONIC τ DECAYS WITHIN $R_{\chi T}$

Pablo Roig (INFN)

SU(2) AND INTERFERENCES

(Davier, Descotes-Genon, Höcker, Malaescu, Zhang '08)

The final state $K^+K^-\pi^0$ can be produced through the intermediate states $K^{*\pm}(892)K^\mp$ or $K_2^{*\pm}(1430)K^\mp$, and we expect a Dalitz plot with a symmetric population density with respect to the exchange $K^+\pi^0(K^{*+}) \leftrightarrow K^-\pi^0(K^{*-})$, see Fig. 13.

The final state $K_s^0K^\pm\pi^\mp$ is obtained via the decays of $K^{*\pm}(892)K^\mp$ and $K^{*0}(892)K_s^0$, or $K_2^{*\pm}(1430)K^\mp$ and $K_2^{*0}(1430)K_s^0$, *i.e.*, both charged $K^{*\pm}(K_s^0\pi^\pm)$ and neutral $K^{*0}(K^\mp\pi^\pm)$ can be produced. The population density of the Dalitz plot is expected to be asymmetric in this case. This effect is clearly seen in Fig. 14.

phase of the isospin components. The analysis described in the following applies only to the $K_s^0K^\pm\pi^\mp$ Dalitz plot, since only in this case, with both charged and neutral K^* contributing, we can separately extract the isoscalar and isovector components. Because the $KK^*(892)$ and

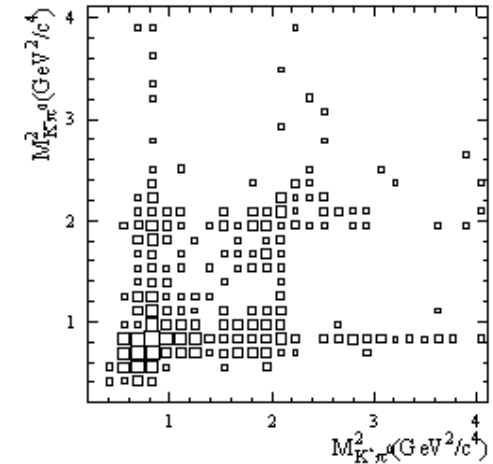


FIG. 13: The Dalitz plot distribution for the $K^+K^-\pi^0$ final state.

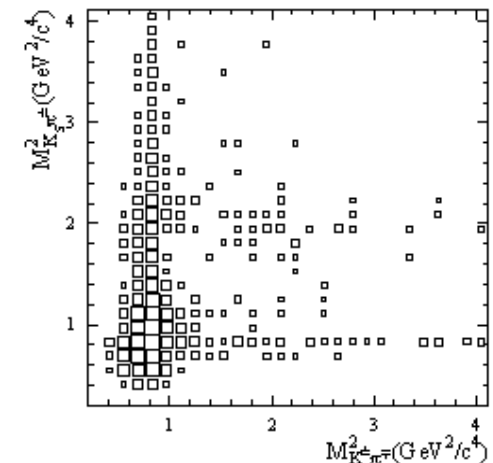


FIG. 14: The Dalitz plot distribution for the $K_s^0K^\pm\pi^\mp$ final state.

HADRONIC τ DECAYS WITHIN $R_{\chi T}$
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SU(2) AND INTERFERENCES

(Davier, Descotes-Genon, Höcker, Malaescu, Zhang '08)

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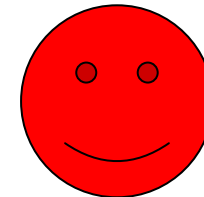
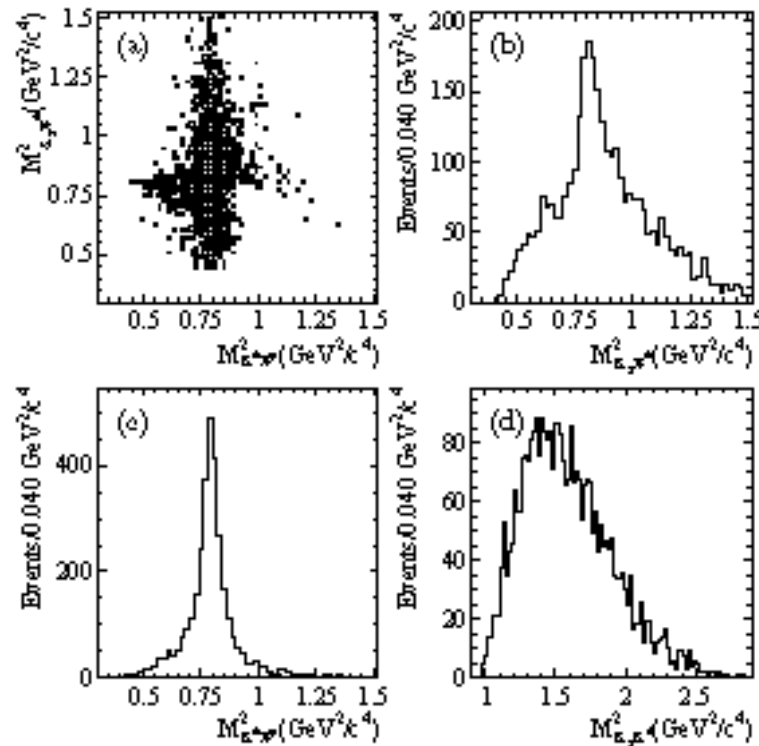


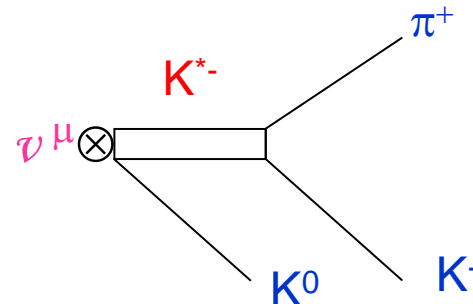
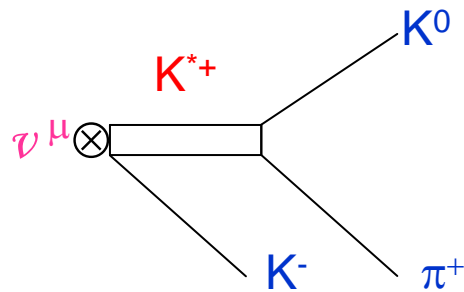
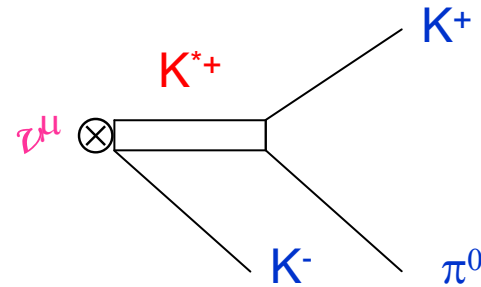
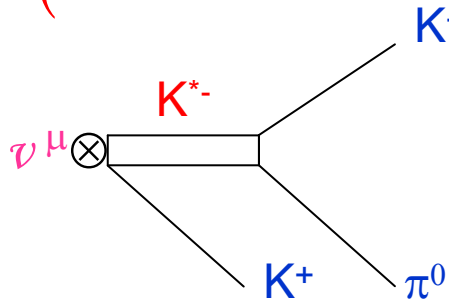
FIG. 15: (a) Dalitz plot distributions for $K_S^0 K^\pm \pi^\mp$ events with an invariant mass $m_{K_S^0 K^\pm} < 2.0 \text{ GeV}/c^2$. (b) $K_S^0 \pi^\pm$ projection, with the broad charged $K^*(892)$ peak, (c) $K^\pm \pi^\mp$ projection, with the narrow neutral $K^*(892)$ peak. (d) $K_S^0 K^\pm$ projection.

SU(2) AND INTERFERENCES

$$\sigma(e^+e^- \rightarrow KK\pi) \stackrel{?}{=} 3 \cdot \sigma(e^+e^- \rightarrow K_s K^\pm \pi^\mp) = 6 \cdot \sigma(e^+e^- \rightarrow K^0 K^- \pi^+)$$

$$\sigma(e^+e^- \rightarrow K^+ K^- \pi^0) \stackrel{?}{=} \sigma(e^+e^- \rightarrow K_s K^\pm \pi^\mp)$$

$$2\sigma(e^+e^- \rightarrow K^0 K^- \pi^+) \stackrel{?}{=} \sigma(e^+e^- \rightarrow K^+ K^- \pi^0)$$



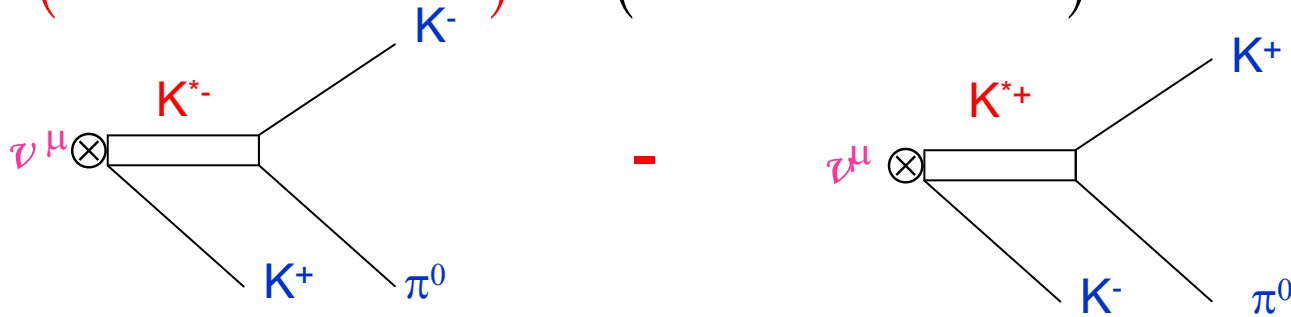
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 Pablo Roig (INFN)

SU(2) AND INTERFERENCES

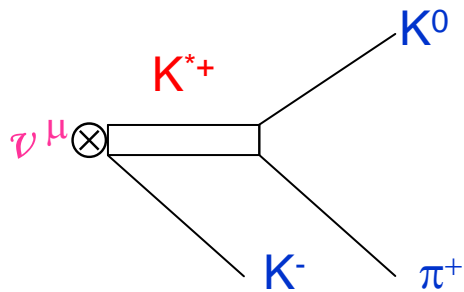
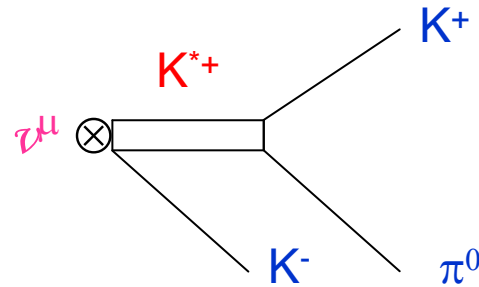
$$\sigma(e^+e^- \rightarrow KK\pi) \stackrel{?}{=} 3 \cdot \sigma(e^+e^- \rightarrow K_s K^\pm \pi^\mp) = 6 \cdot \sigma(e^+e^- \rightarrow K^0 K^- \pi^+)$$

$$\sigma(e^+e^- \rightarrow K^+ K^- \pi^0) \stackrel{?}{=} \sigma(e^+e^- \rightarrow K_s K^\pm \pi^\mp)$$

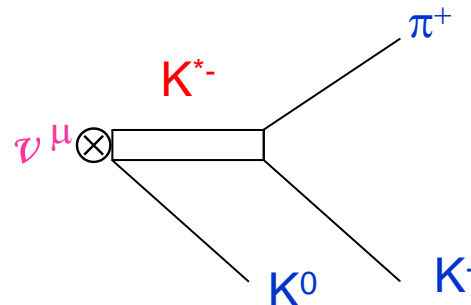
$$2\sigma(e^+e^- \rightarrow K^0 K^- \pi^+) \stackrel{?}{=} \sigma(e^+e^- \rightarrow K^+ K^- \pi^0)$$



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